

# APPROACHES TO FAIR CLASSIFICATION

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CSC 2541

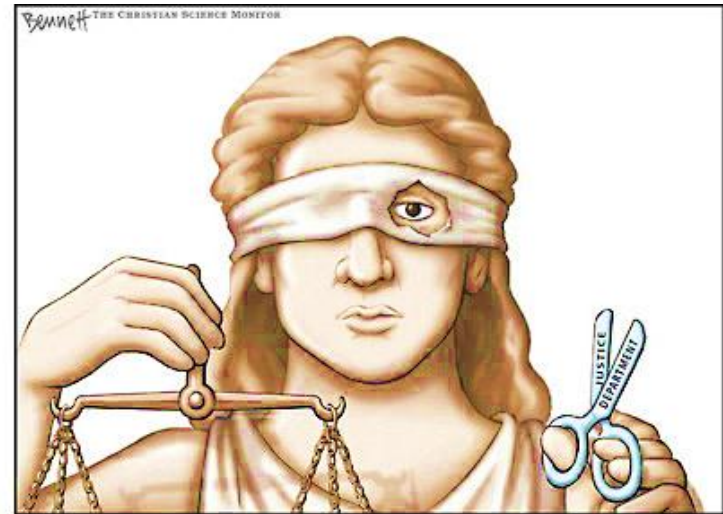
OCTOBER 1, 2019



# FAIRNESS THROUGH AWARENESS

Dwork, Hardt, Pitassi, Reingold, Zemel, 2012

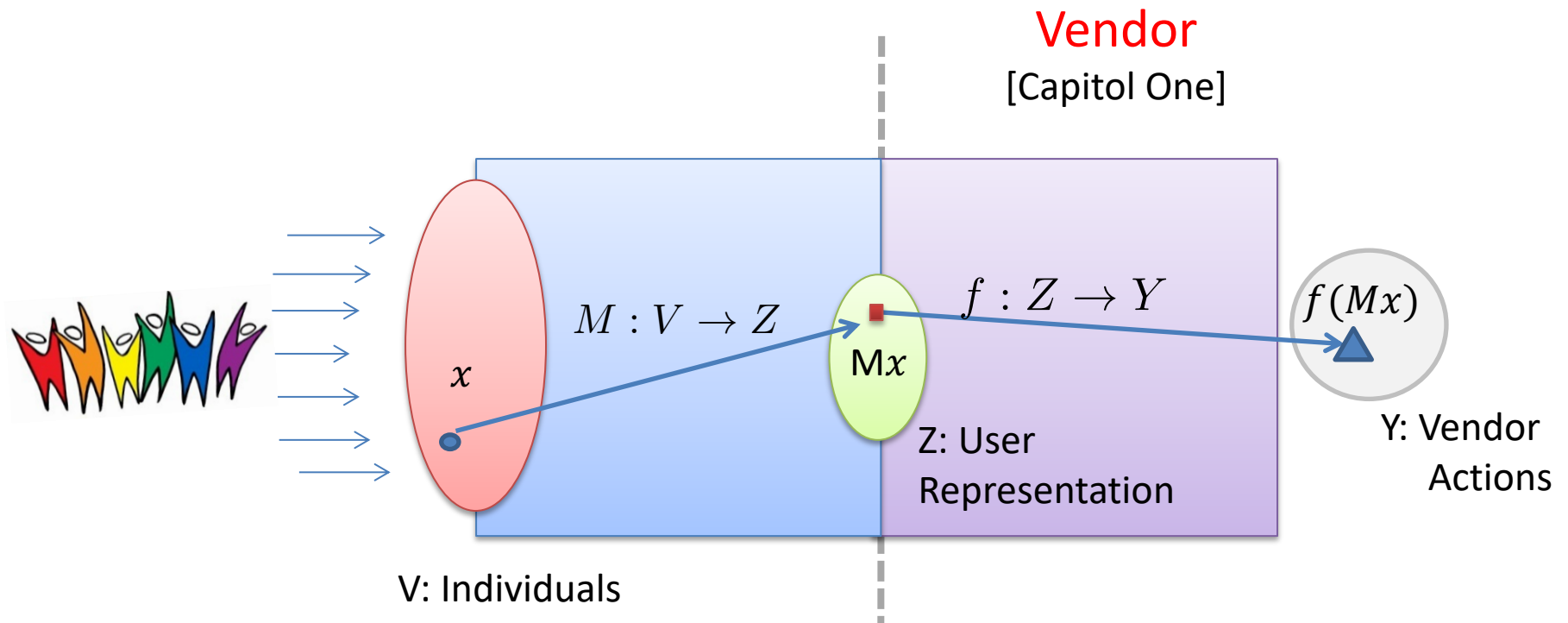
Goal: Assign each individual  
a representation *by being  
aware of membership in  
group A*



(1). **Individual Fairness**: Treat similar individuals similarly

(2). **Group Fairness**: equalize two groups ( $A=1$  = minority;  
 $A=0$  is majority) at the level of outcomes (**statistical parity**)

# General Framework

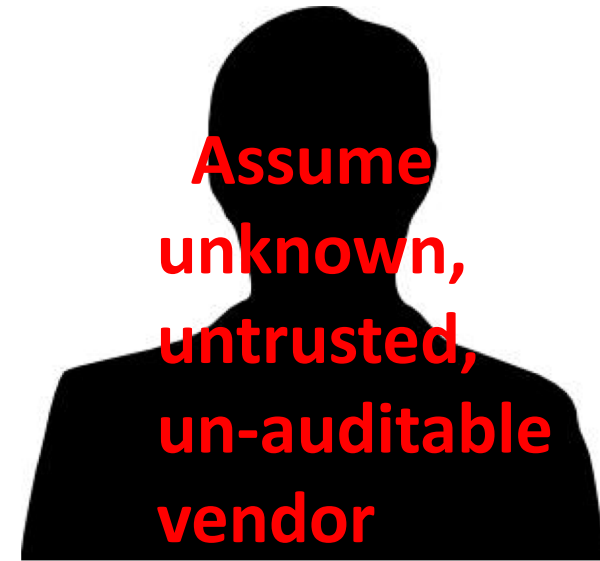
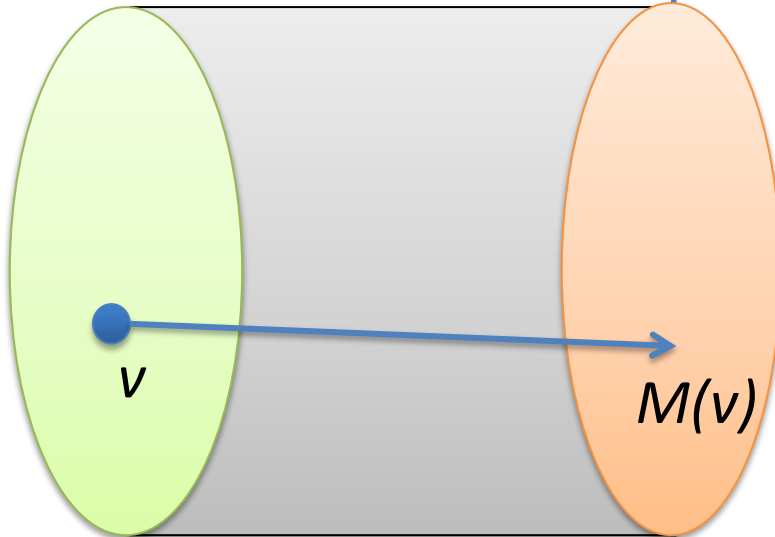


# Our goal:

Achieve Fairness in the representation step

Ad Network (with  
Ad Network  
society oversight)

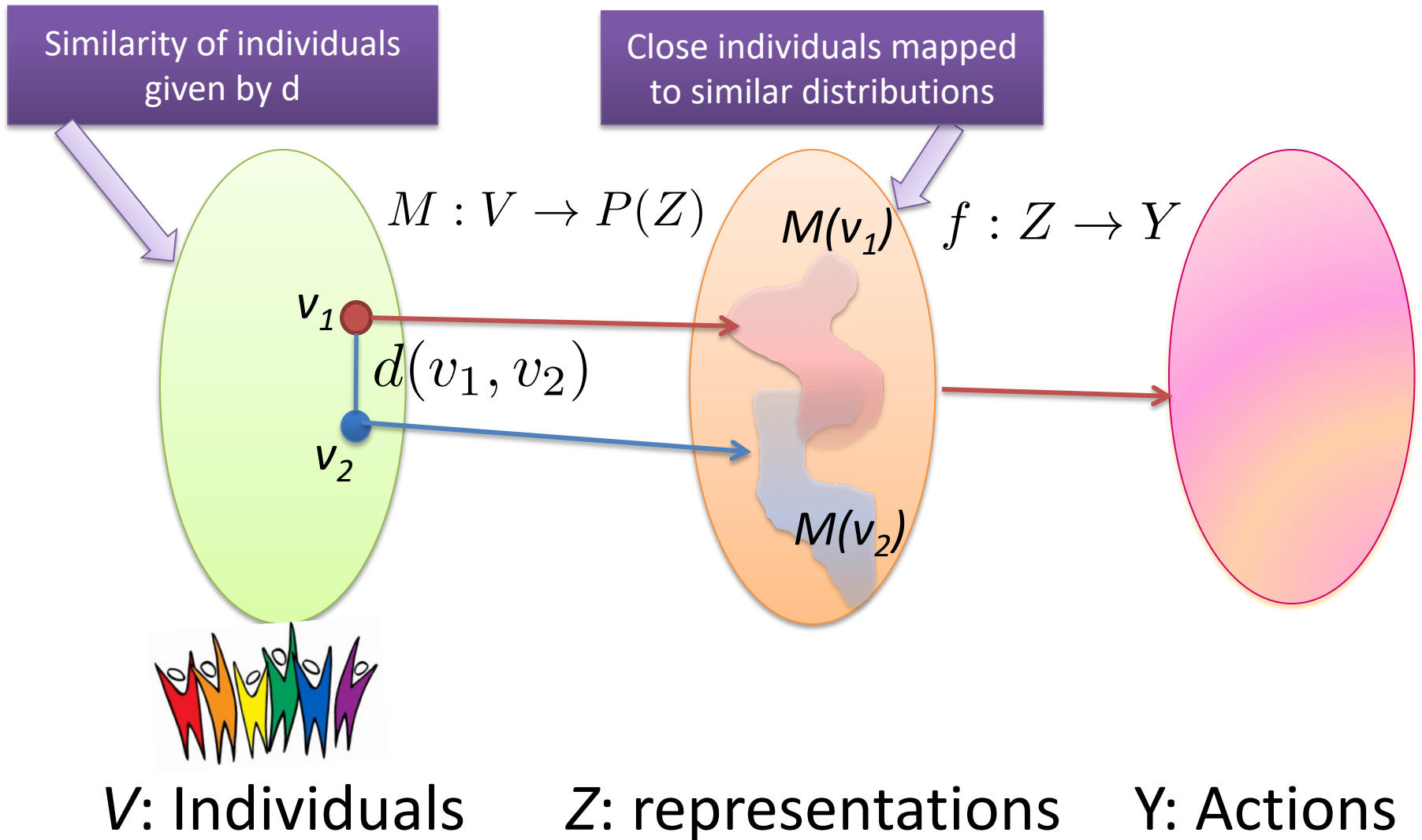
$$M : V \rightarrow Z$$



$V$ : Individuals

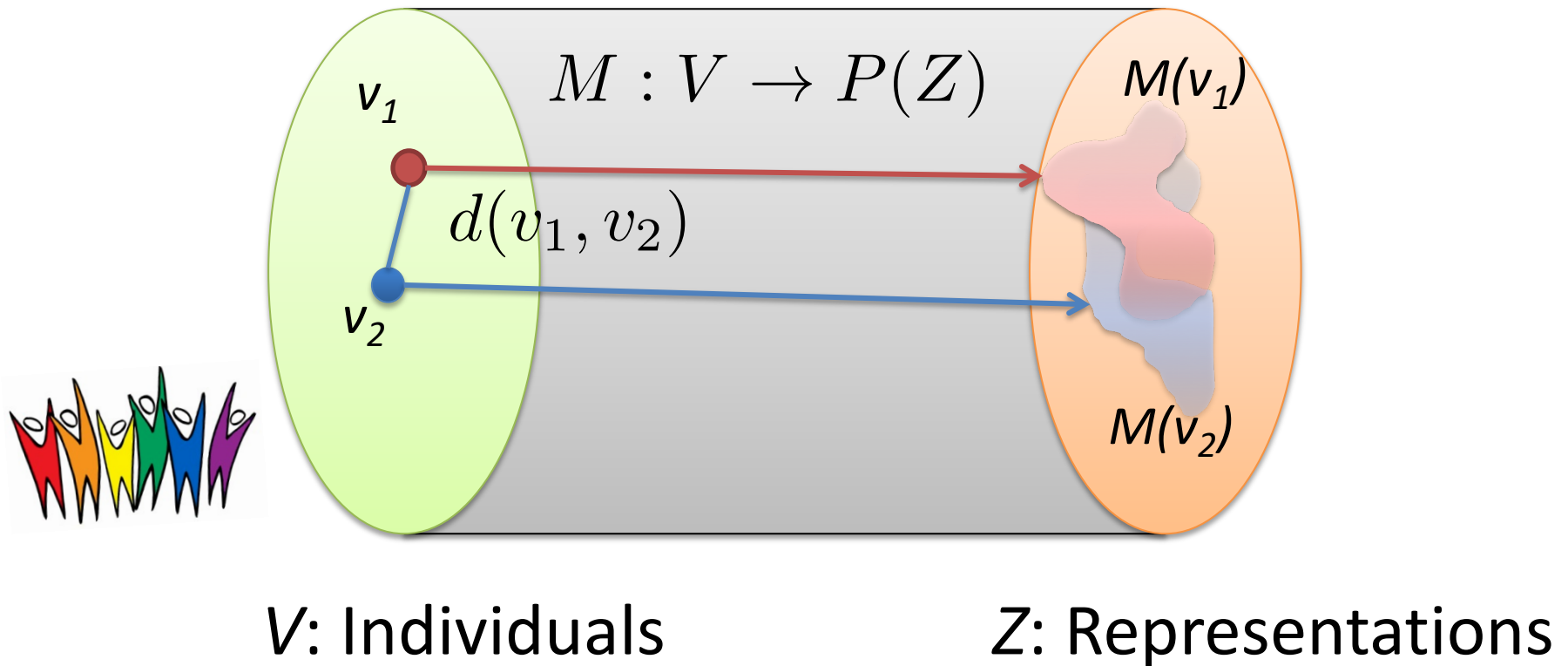
$Z$ : representation

# Our Approach: Define a randomized mapping that “blends people with the crowd”



Metric  $d: V \times V \rightarrow \mathbb{R}$

Lipschitz condition  $\|M(v_1) - M(v_2)\| \leq d(v_1, v_2)$



# The Metric

- Assume *task-specific similarity metric*
  - Extent to which two individuals are similar w.r.t. the classification task at hand
- Ideally captures *ground truth*
  - Or, society's best approximation
- Open to public discussion, refinement

Examples: Financial/insurance risk metrics

- Already widely used (though secret)
- AALIM health care metric
  - health metric for treating similar patients similarly
- Roemer's relative effort metric
  - Well-known approach in economics/political theory

# An Algorithm for Fair Classification



utility  
function  
 $U: V \times Z \rightarrow R$



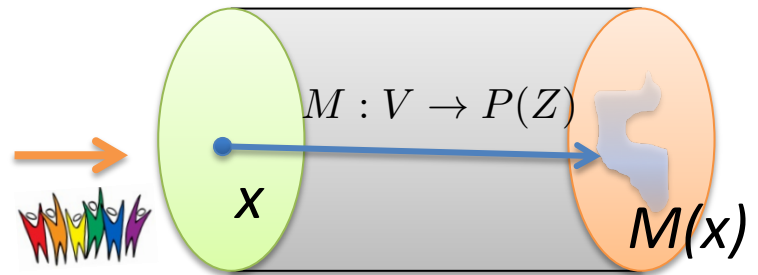
Metric

$d: V \times V \rightarrow R$



Efficient  
Procedure

$d$ -fair mapping  $M$



V: Individuals

Z: Encodings

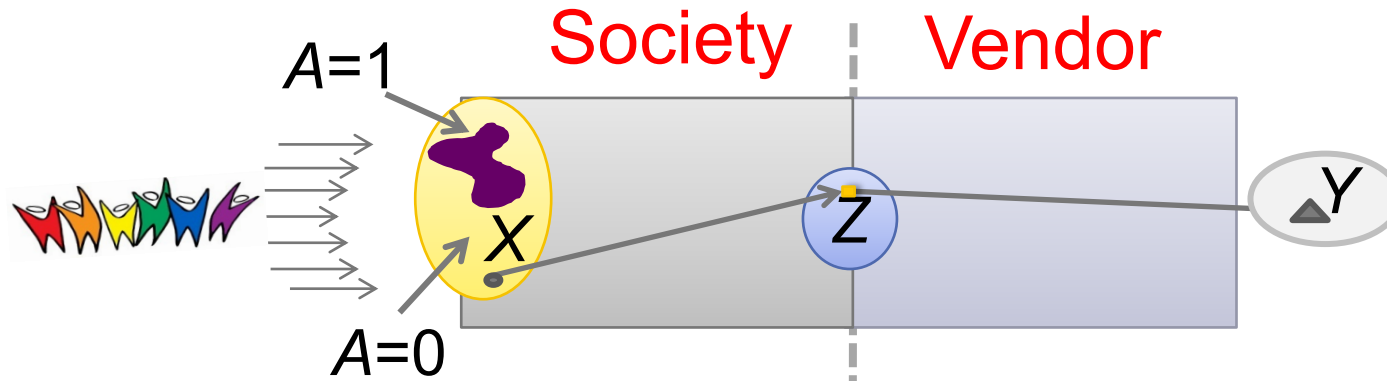
LP maximizes vendor's expected utility  
subject to fairness conditions





# FAIR REPRESENTATION LEARNING: FRAMEWORK

Zemel. Wu, Swersky, Pitassi, Dwork, 2013



Goal: Learn a mapping from  $X$  to distributions over representations  $Z$  *that is fair*

## Aims for $Z$ :

1. Lose information about  $A$ :

$$P[Z=k | A=1] = P[Z=k | A=0]$$

2. Retain information about  $X$
3. Preserve information for classification so vendor can max utility [decisions  $Y = g(Z)$ ]

# INITIAL FORMULATION

Difficult to jointly optimize:

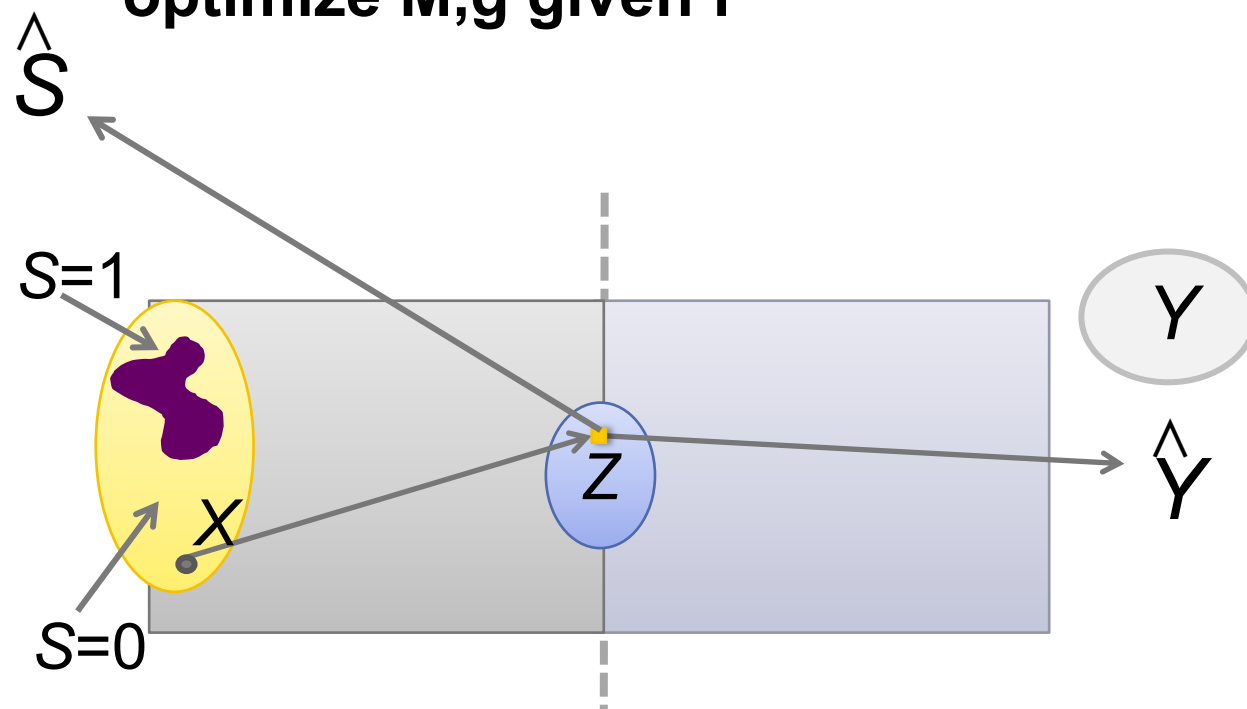
$$\min. |f(\mathbf{Z}) - \mathbf{Y}|; \quad \max. |g(\mathbf{Z}) - \mathbf{S}| \quad (\text{thwart adversary})$$

Can alternate:

optimize  $M, f$  given  $g$ ;

optimize  $M, g$  given  $f$

But unstable



# INSTANTIATING THE MODEL

Key: min.  $MI(Z, S)$  by forcing  $P(Z|S+) = P(Z|S-)$

$$P(Z|S) = \int_X P(Z|X, S)P(X|S)dX$$

$$P(Z|S = 1) \approx \frac{1}{N^+} \sum_{n=1}^{N^+} P(Z|X, S = 1)$$

$$P(Z|S = 1) = P(Z|S = 0) = P(Z) \Rightarrow$$

Simple tractable formulation:

$$MI(Z, S) = 0$$

**Z is a discrete latent variable**

# FULL OBJECTIVE FUNCTION

Learn mapping  $M(X)$  to minimize  $L$

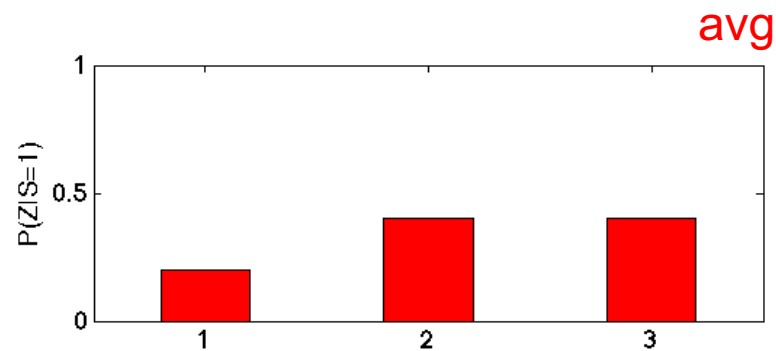
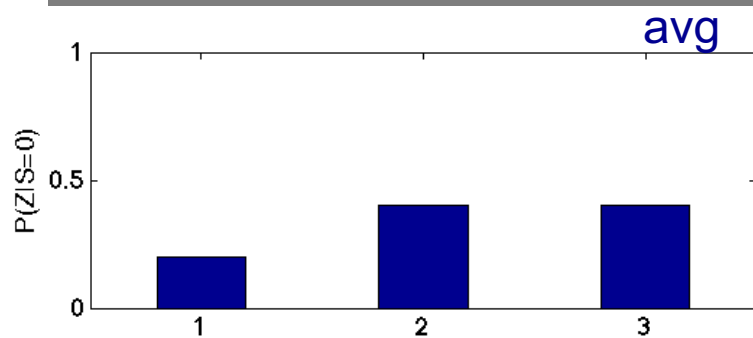
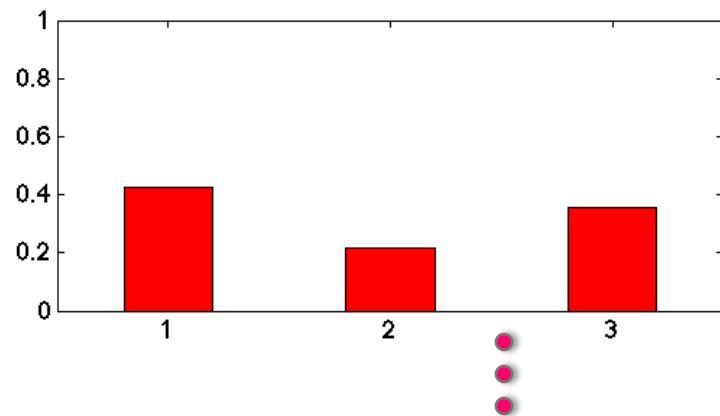
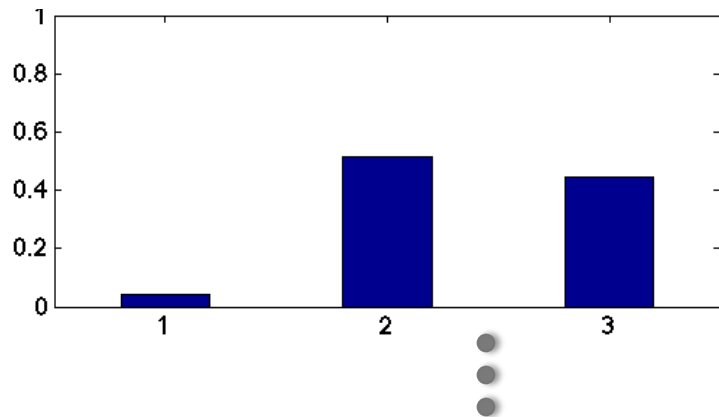
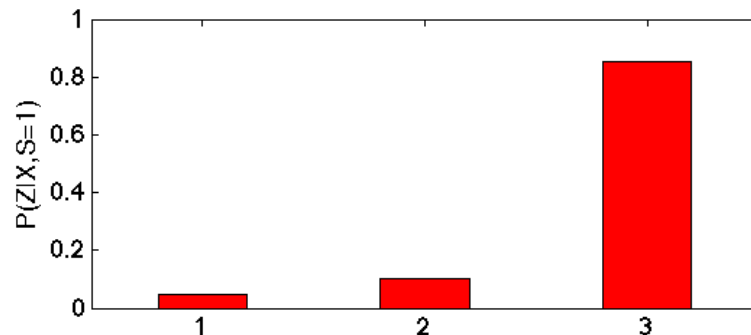
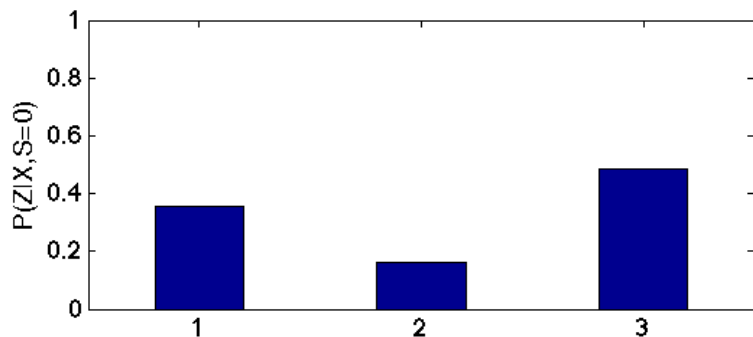
$$P_{n,k}^+ = P(Z = k | \mathbf{x}, S = 1) = \frac{\exp(\mathbf{x}_n^T \mathbf{w}_k^+)}{\sum_{k'} \exp(\mathbf{x}_n^T \mathbf{w}_{k'}^+)}$$

$$L = A_y \cdot L_y + A_z \cdot L_z$$

$$L_z = \sum_k |P_k^+ - P_k^-| \quad P_k^+ = P(Z = k | S = 1)$$

$$L_y = \sum_{n=1}^N -y_n \log \hat{y}_n - (1 - y_n) \log(1 - \hat{y}_n) \quad \hat{y}_n = \sum_k P_{n,k} u_k$$

# OBFUSCATING MEMBERSHIP



$$P(Z|S^z = 1) = P(Z|S = 0) \Rightarrow MI(Z, S) = 0$$

# EXPERIMENTS

## 1. German Credit

**Size:** 1000 instances, 20 attributes

**Task:** classify as good or bad credit

**Sensitive feature:** Age

## 2. Adult Income

**Size:** 45,222 instances, 14 attributes

**Task:** predict whether or not annual income > 50K

**Sensitive feature:** Gender

## 3. Heritage Health

**Size:** 147,473 instances, 139 attributes

**Task:** predict whether patient spends any nights in hospital

**Sensitive feature:** Age

# PERFORMANCE METRICS

- **Accuracy**

$$yAcc = 1 - \frac{1}{N} \sum_{n=1}^N |y_n - \hat{y}_n|$$

- **Discrimination**

$$yDiscrim = \left| \frac{\sum_{n:s_n=1} \hat{y}_n}{\sum_{n:s_n=1} 1} - \frac{\sum_{n:s_n=0} \hat{y}_n}{\sum_{n:s_n=0} 1} \right|$$

# ALTERNATIVE APPROACHES

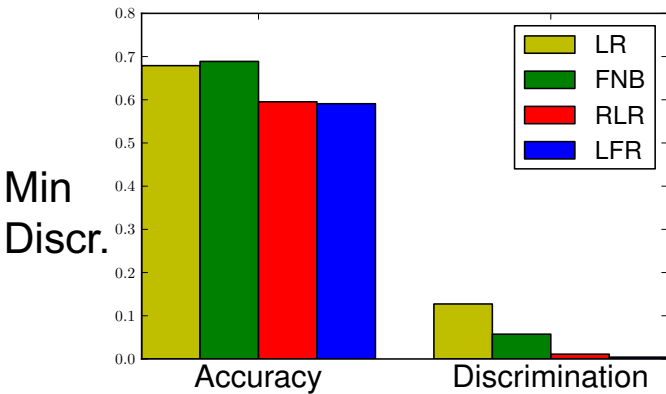
Build fair classifier and force vendor to use it:

- Message labels to achieve proportional access (FNB) [Kamiran & Calders, 2009]
- Trade off classification error vs. discrimination (RLR) [Kamishima et al, 2011]

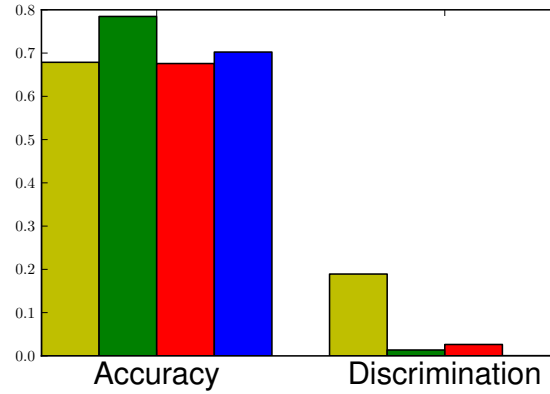


# EXPERIMENTAL RESULTS

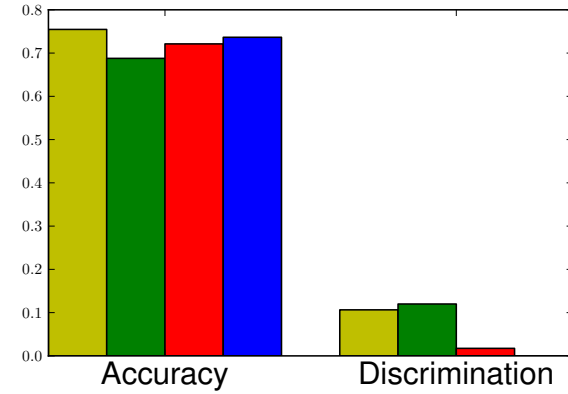
## German



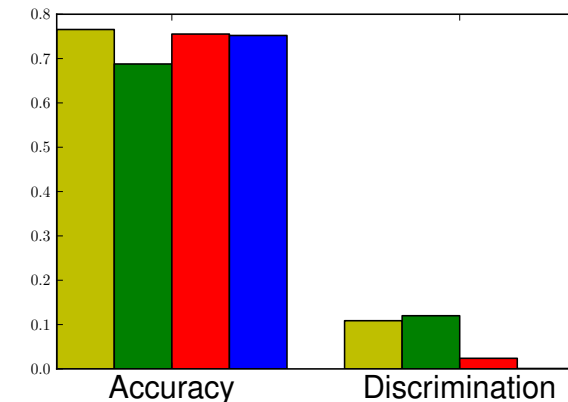
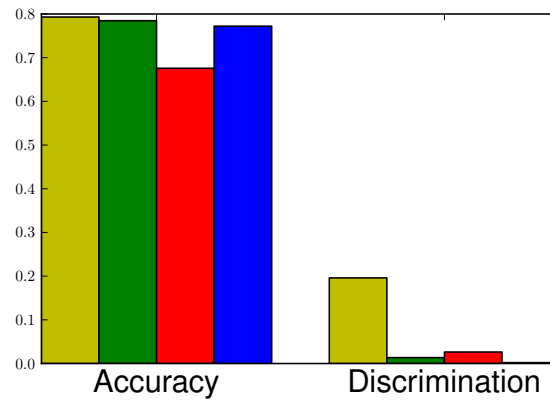
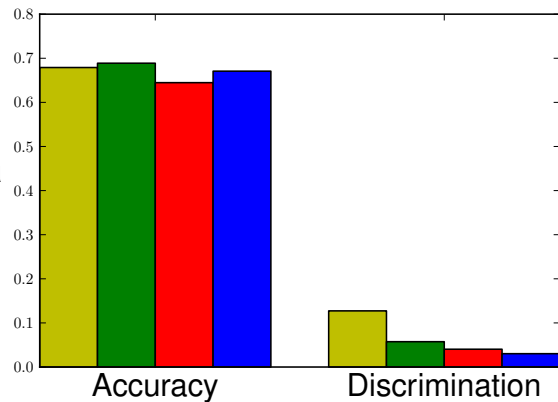
## Adult



## Health



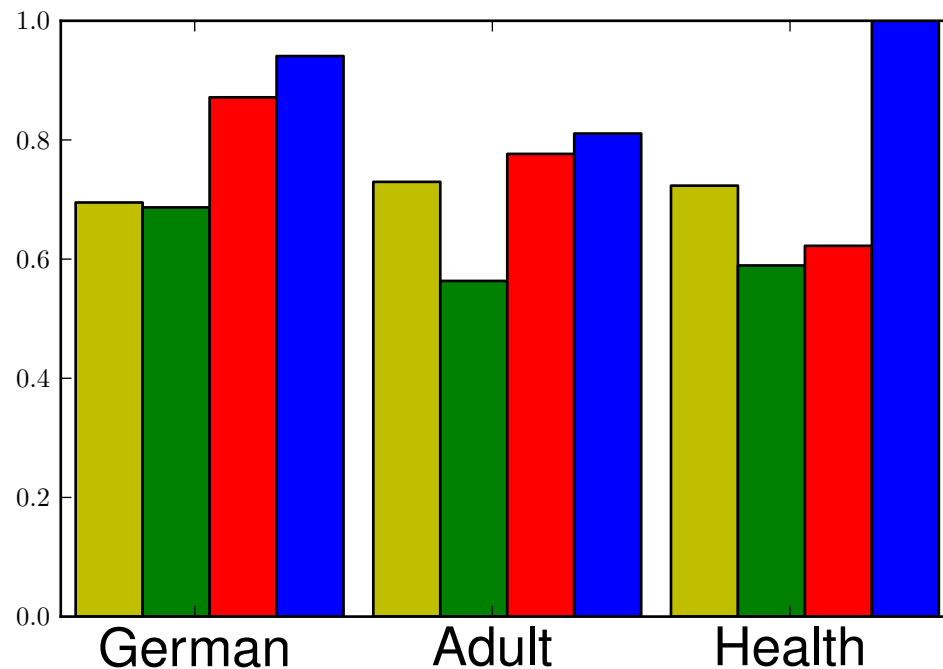
Max Delta



# RESULTS: INDIVIDUAL FAIRNESS

## Consistency:

$$y_{NN} = 1 - \frac{1}{N} \sum_n |\hat{y}_n - \frac{1}{k} \sum_{j \in kNN(\mathbf{x}_n)} \hat{y}_j|$$



# EXAMPLE DOMAINS

1. Targeted search/advertising: How do different groups see internet content?
  - Males/females with equal interest, equal  $p(\text{ad})$ ?
  - (leisure interests; lower paying jobs; credit card rates)
2. Medical testing/diagnosis: decision-making based on tests, that affect  $p(\text{diagnosis})$ 
  - Applied uniformly to different groups
  - Medical tests for conditions that vary widely between groups
3. Recidivism: risk tools assess  $p(\text{future-arrest})$  given history
  - Used in decisions about bail, sentencing, parole
  - Claims of bias based on race against COMPAS risk tool

Common:

1. Algorithm input to decision-maker
2. Attempting to classify individual possesses property: interest; condition; risk
3. Output is a probability

# FAIR CLASSIFICATION

Explosion of fairness research over last five years

Fair classification is the most common setup, involving:

- $X$ , some data
- $Y$ , a label to predict
- $\hat{Y}$ , the model prediction
- $A$ , a sensitive attribute (race, gender, age, socio-economic status)

We want to learn a classifier that is:

- accurate
- fair with respect to  $A$

# REPRESENTATIONS BEYOND CLUSTERS

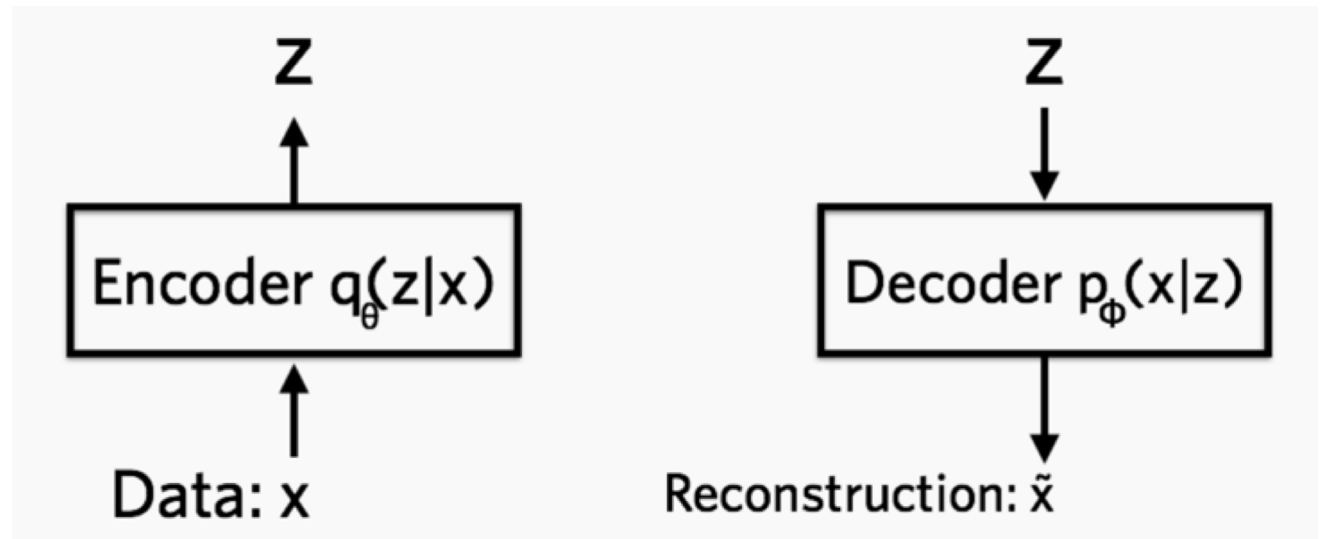
Aim: Replace discrete representation with continuous, multi-dimensional  $Z$

Allow more flexible, nuanced representations

Bring ML arsenal to bear: powerful methods for mapping, embedding in vector spaces: Variational Auto Encoders (VAE)

How to maintain statistical parity in learned representations?

# VAE



Re-formulation of autoencoders:

- Each input encoded into a distribution in latent space
- Output prediction obtained by sampling from distribution, mapping through decoder

Allows maximum-likelihood based density modelling:

$$\log p_{\theta}(\mathbf{x}) \geq \mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})} [\log p_{\theta}(\mathbf{x}|\mathbf{z})] - D_{KL} \left( q_{\phi}(\mathbf{z}|\mathbf{x}) \parallel p(\mathbf{z}) \right)$$

# MMD

- Suppose we have access to samples from two probability distributions  $X \sim P_A$  and  $Y \sim P_B$ , how can we tell if  $P_A = P_B$ ?
- **Maximum Mean Discrepancy (MMD)** is a measure of distance between two distributions given only samples from each. [Gretton 2010]

$$\begin{aligned} & \left\| \frac{1}{N} \sum_{n=1}^N \phi(X_n) - \frac{1}{M} \sum_{m=1}^M \phi(Y_m) \right\|^2 \\ &= \frac{1}{N^2} \sum_{n=1}^N \sum_{n'=1}^N \phi(X_n)^\top \phi(X_{n'}) + \frac{1}{M^2} \sum_{m=1}^M \sum_{m'=1}^M \phi(Y_m)^\top \phi(Y_{m'}) - \frac{2}{NM} \sum_{n=1}^N \sum_{m=1}^M \phi(X_n)^\top \phi(Y_m) \\ &= \frac{1}{N^2} \sum_{n=1}^N \sum_{n'=1}^N k(X_n, X_{n'}) + \frac{1}{M^2} \sum_{m=1}^M \sum_{m'=1}^M k(Y_m, Y_{m'}) - \frac{2}{MN} \sum_{n=1}^N \sum_{m=1}^M k(X_n, Y_m) \end{aligned}$$

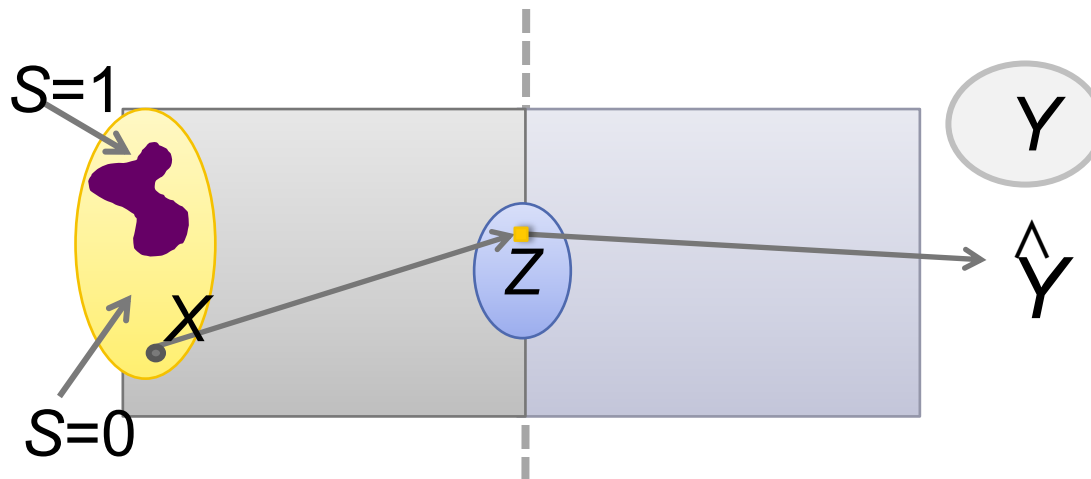
- Our idea: **learn to make two distributions indistinguishable**  
→ **small MMD!**

# VARIATIONAL FAIR AUTOENCODER

VAE with regularizer on latent representations

Match higher-order moments, continuous  $Z$ :

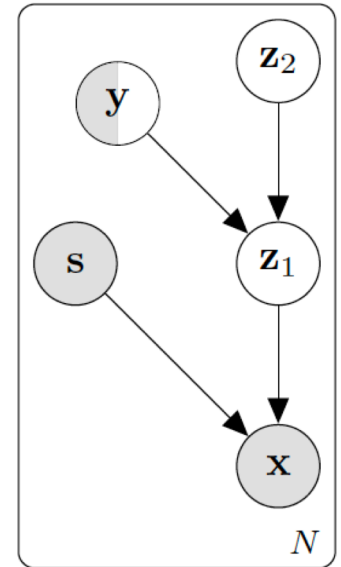
$$\ell_{\text{MMD}}(\mathbf{Z}_{1s=0}, \mathbf{Z}_{1s=1}) = \left\| \mathbb{E}_{\tilde{p}(\mathbf{x}|s=0)} [\mathbb{E}_{q(\mathbf{z}_1|\mathbf{x},s=0)} [\psi(\mathbf{z}_1)]] - \mathbb{E}_{\tilde{p}(\mathbf{x}|s=1)} [\mathbb{E}_{q(\mathbf{z}_1|\mathbf{x},s=1)} [\psi(\mathbf{z}_1)]] \right\|^2$$





# VARIATIONAL FAIR AUTOENCODER

Extend VAE to include some labels  $y$  (semi-supervised VAE [Kingma & Welling, 2014]) and “nuisance variable”  $s$



Objective -- maximize:

$$\sum_{n=1}^{N_s} \mathbb{E}_{q_{\phi}(\mathbf{z}_{1n} | \mathbf{x}_n, \mathbf{s}_n)} [-KL(q_{\phi}(\mathbf{z}_{2n} | \mathbf{z}_{1n}, \mathbf{y}_n) || p(\mathbf{z}_2)) + \log p_{\theta}(\mathbf{x}_n | \mathbf{z}_{1n}, \mathbf{s}_n)] +$$

$$+ \mathbb{E}_{q_{\phi}(\mathbf{z}_{2n} | \mathbf{z}_{1n}, \mathbf{y}_n)} [-KL(q_{\phi}(\mathbf{z}_{1n} | \mathbf{x}_n, \mathbf{s}_n) || p_{\theta}(\mathbf{z}_{1n} | \mathbf{z}_{2n}, \mathbf{y}_n))]$$

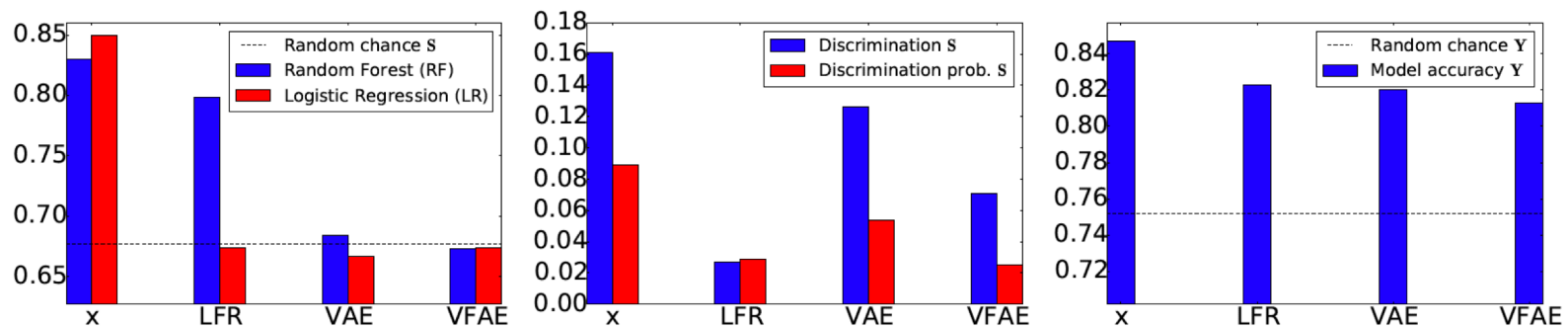
Add for labeled set:

$$\sum_{n=1}^N \mathbb{E}_{q(\mathbf{z}_{1n} | \mathbf{x}_n, \mathbf{s}_n)} [-\log q_{\phi}(\mathbf{y}_n | \mathbf{z}_{1n})]$$

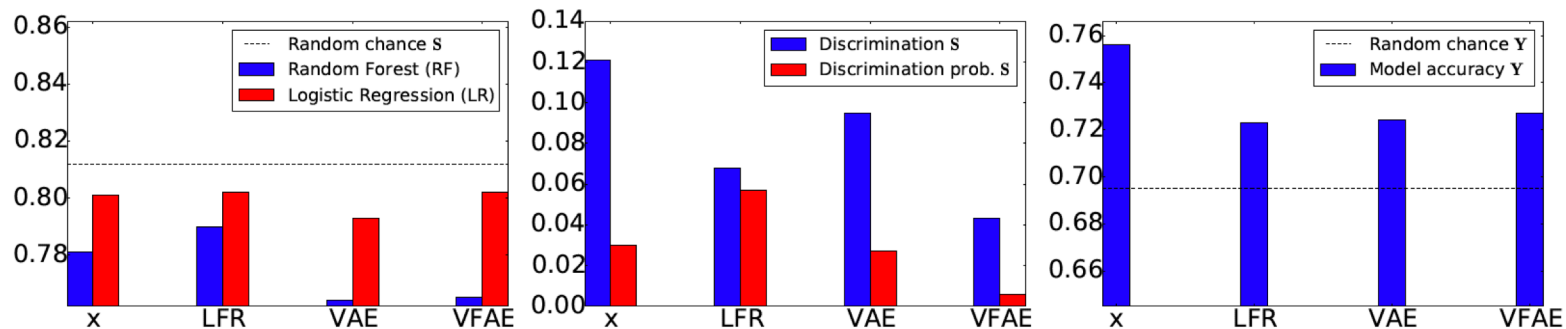
unlabeled set:

$$\sum_{m=1}^M \mathbb{E}_{q_{\phi}(\mathbf{z}_{1m} | \mathbf{x}_m, \mathbf{s}_m)} [-KL(q(\mathbf{y}_m | \mathbf{z}_{1m}) || p(\mathbf{y}_m))]$$

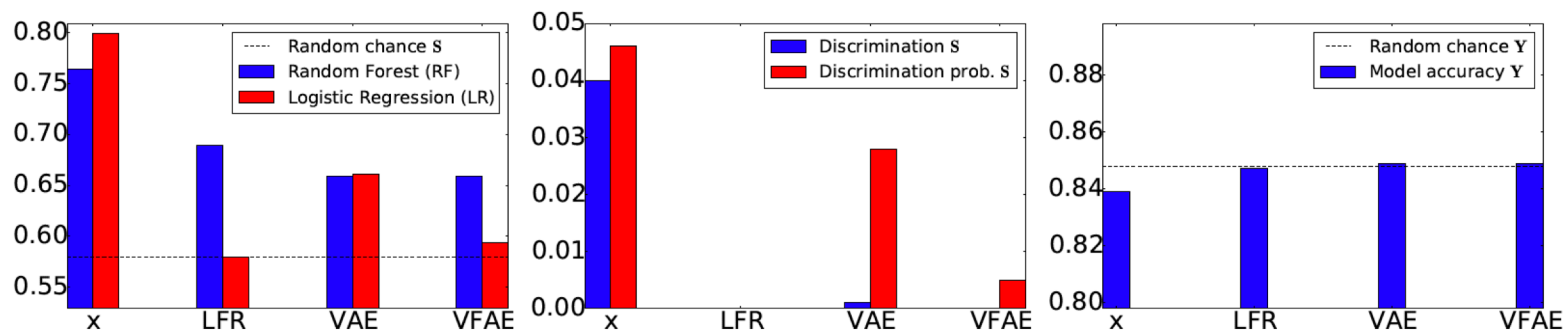
# RESULTS



(a) Adult dataset



(b) German dataset



(c) Health dataset

# RESULTS

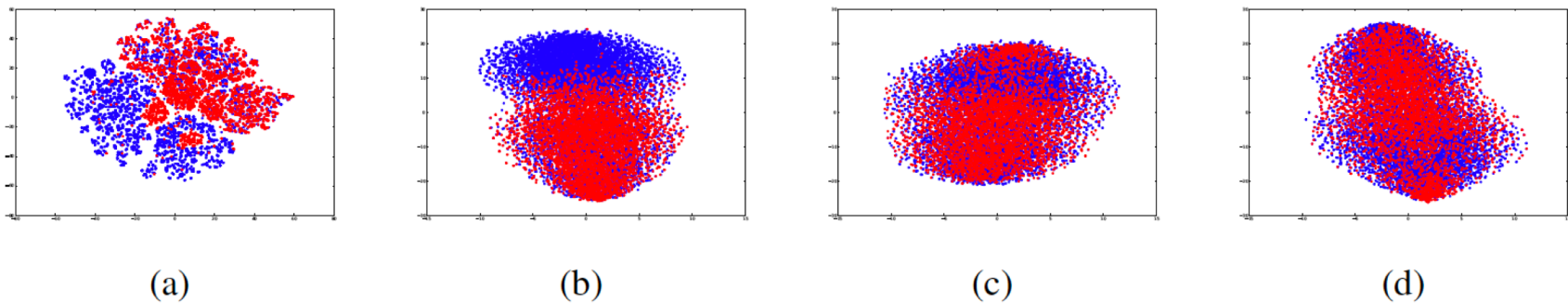


Figure 4: t-SNE (van der Maaten, 2013) visualizations from the Adult dataset on: (a): original  $x$ , (b): latent  $z_1$  without  $s$  and MMD, (c): latent  $z_1$  with  $s$  and without MMD, (d): latent  $z_1$  with  $s$  and MMD. Blue colour corresponds to males whereas red colour corresponds to females.

# ADAPTING THE FRAMEWORK

The same idea has many other useful applications, e.g.,

- Eliminating demographic discrimination in deciding who should get transplant surgery
- Removing confounds, such as which scanner produced a medical image

**Key: Learning to make two (or more) distributions indistinguishable**

# DOMAIN ADAPTATION

Natural fit: **domain adaptation**

Make feature representations for source and target domain data indistinguishable

Sentiment classification

- Product reviews (text, tf-idf on words & bigrams)
- Labeled data from source domain, unlabeled data from target domain

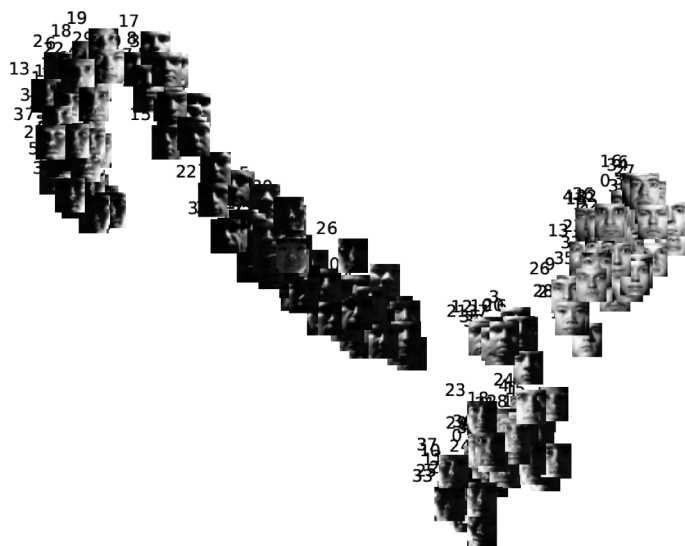
Source - Target	S		Y	
	RF	LR	VFAE	DANN
books - dvd	0.535	0.564	<b>0.799</b>	0.784
books - electronics	0.541	0.562	<b>0.792</b>	0.733
books - kitchen	0.537	0.583	<b>0.816</b>	0.779
dvd - books	0.537	0.563	<b>0.755</b>	0.723
dvd - electronics	0.538	0.566	<b>0.786</b>	0.754
dvd - kitchen	0.543	0.589	<b>0.822</b>	0.783
electronics - books	0.562	0.590	<b>0.727</b>	0.713
electronics - dvd	0.556	0.586	<b>0.765</b>	0.738
electronics - kitchen	0.536	0.570	0.850	<b>0.854</b>
kitchen - books	0.560	0.593	<b>0.720</b>	0.709
kitchen - dvd	0.561	0.599	0.733	<b>0.740</b>
kitchen - electronics	0.533	0.565	0.838	<b>0.843</b>

# LEARNING INVARIANT FEATURES

If we have labeled data from all domains, factoring out unwanted domain bias still leads to better generalization.

Make the learned representations invariant to unwanted transformation / variation / bias.

Example: Face identification under different lighting conditions



# ADVERSARIAL FAIR LEARNING

Rather than using MMD to ensure learned representation is fair, can use adversarial approach

Adversary takes latent representation (here  $R$ ) as input and attempts to predict  $S$ , then model minimizes:

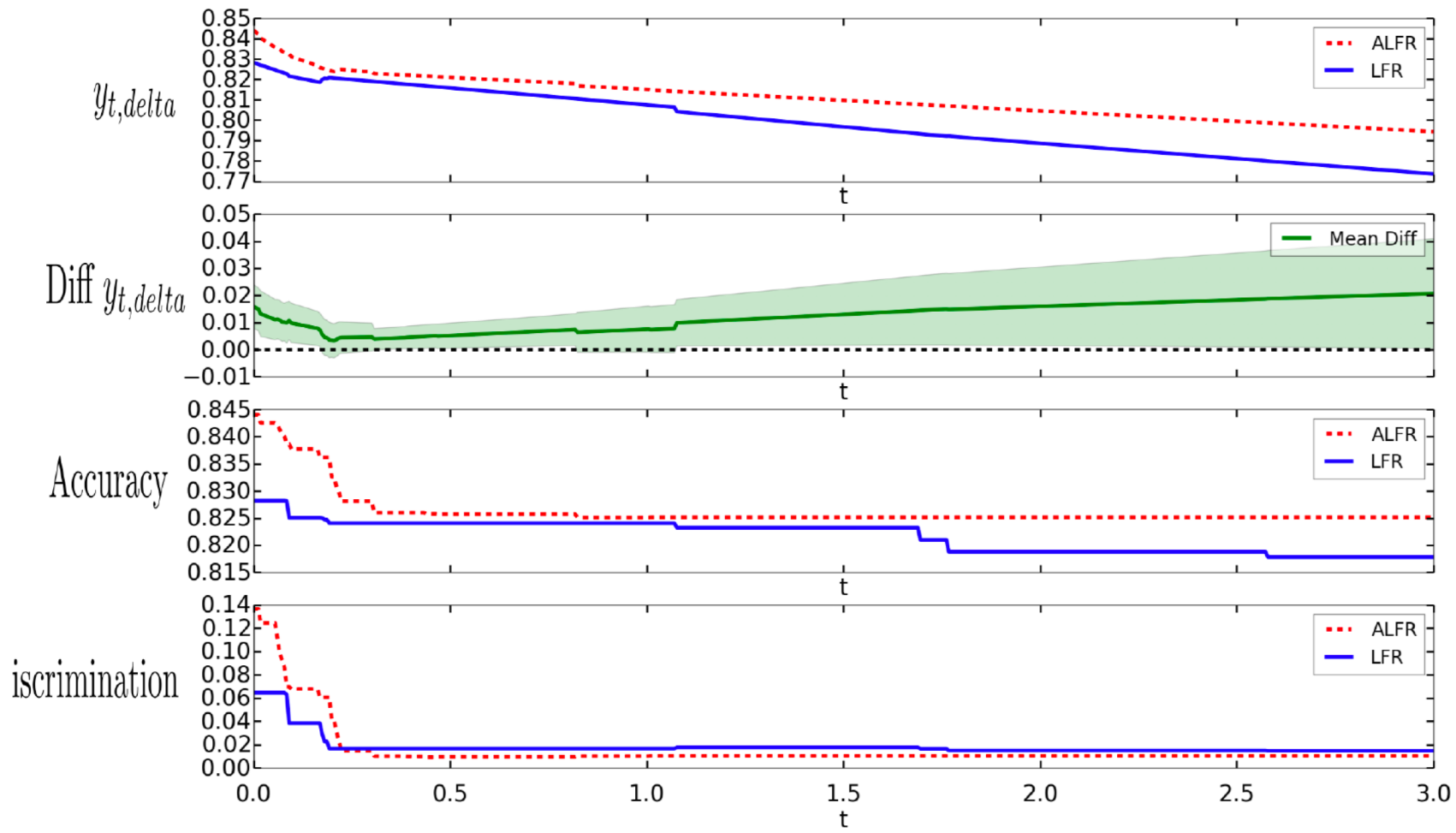
$$D_{\theta, \phi}(R, S) = \mathbb{E}_{X, S} S \cdot \log(\text{Adv}(R)) + (1 - S) \cdot \log(1 - \text{Adv}(R))$$

Combine with reconstruction and classification losses to ensure representation retains info about  $X, Y$

$$C_{\theta}(X, R) = \mathbb{E}_X \|X - \text{Dec}(R)\|_2^2$$

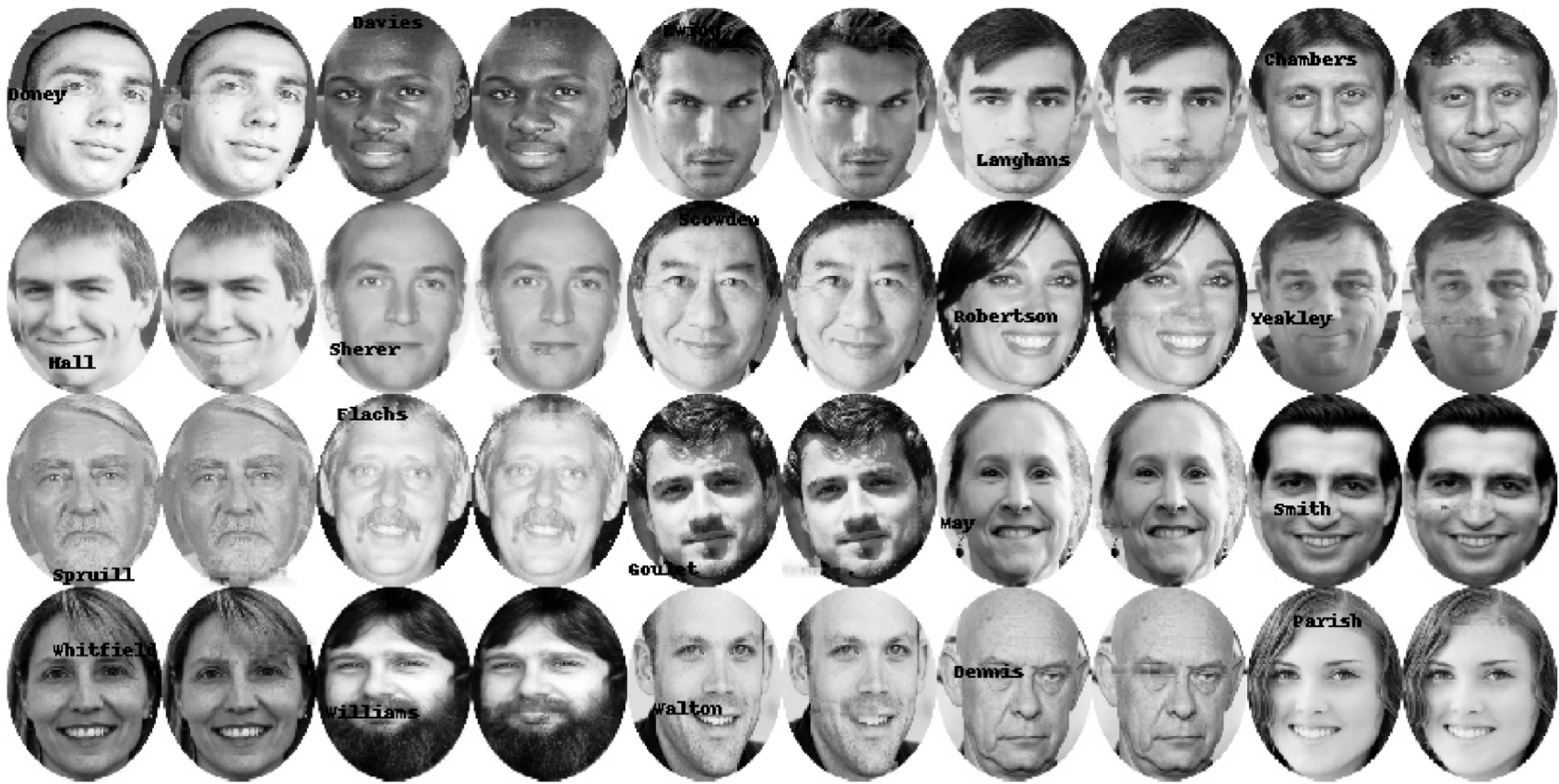
$$E_{\theta}(R, S) = - \mathbb{E}_{X, Y} Y \cdot \log(\text{Pred}(R)) + (1 - Y) \cdot \log(1 - \text{Pred}(R))$$

# RESULTS





# RESULTS



# EQUALIZED ODDS / OPPORTUNITY

Both VFAE and AFLR define fairness as statistical parity

Problems with demographic/statistical parity:

- Coarse measure, not about individuals
- May entail large loss in accuracy

Alternative definition: **equal opportunity** [Hardt, Price, Srebro, 2016]

- Encourage perfect prediction
- But ensure that the prediction errors are balanced between the groups

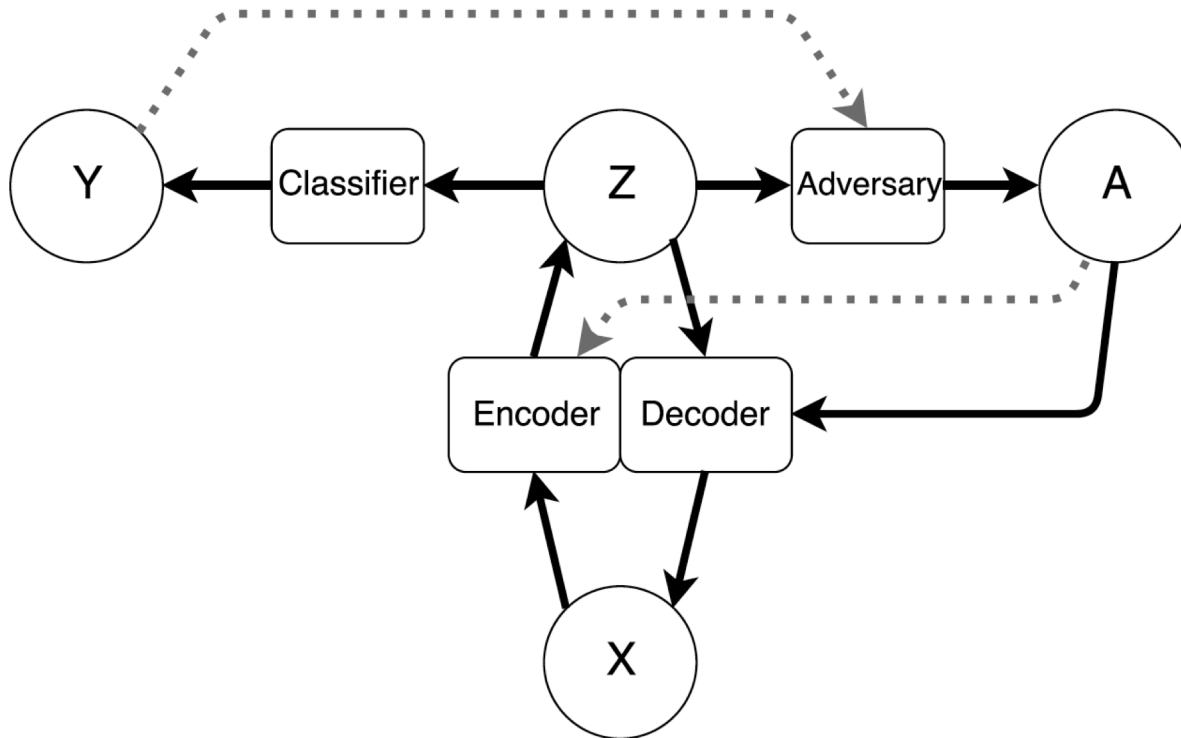
$$\Pr\{\widehat{Y} = 1 \mid A = 0, Y = y\} = \Pr\{\widehat{Y} = 1 \mid A = 1, Y = y\}, \quad y \in \{0, 1\}$$

# BACK TO FAIR REPRESENTATIONS

- Minimize unfair targeting of disadvantaged groups by vendors (worse lines of credit, lower paying jobs)
- Aim: form a data representation that ensures fair classifications downstream
- Consider two types of unfair vendors:
  1. The **indifferent** vendor: does not care about fairness, only maximizes utility
  2. The **malicious** vendor: doesn't care about utility, discriminates unfairly
- Good fit to adversarial learning scheme

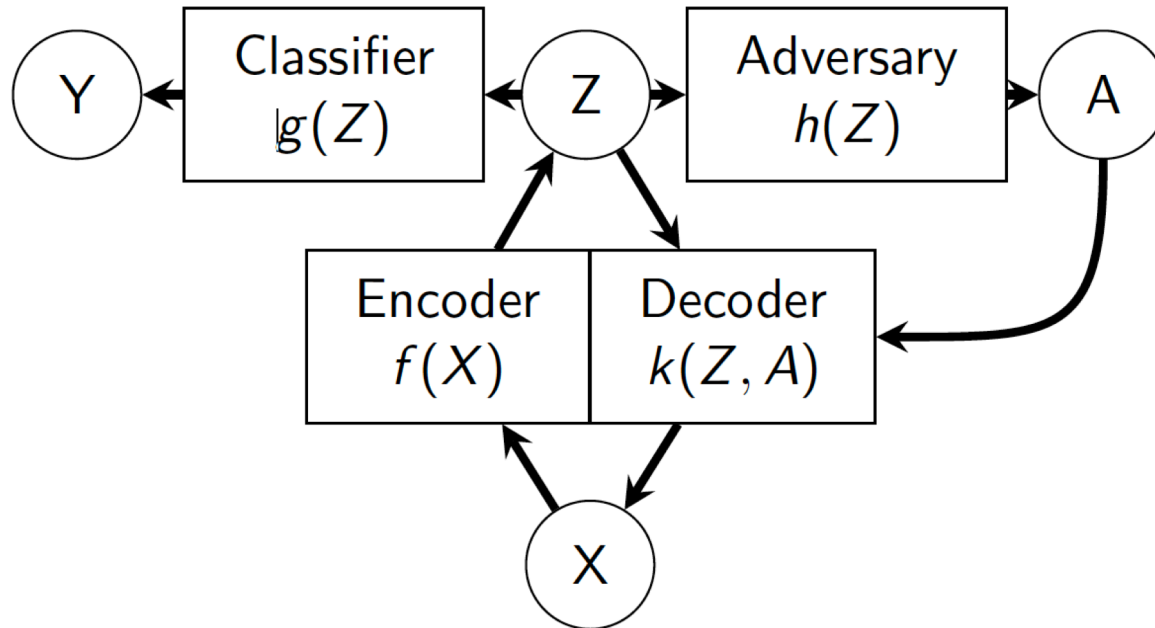
# LEARNING ADVERSARIALLY FAIR TRANSFERABLE REPRESENTATIONS

Madras, Creager, Pitassi, Zemel, 2018



- The classifier is indifferent vendor, forcing the encoder to make the representations useful
- The adversary is the malicious vendor, forcing the encoder to hide the sensitive attributes in the representations

# ADVERSARIAL LEARNING IN LAFTR

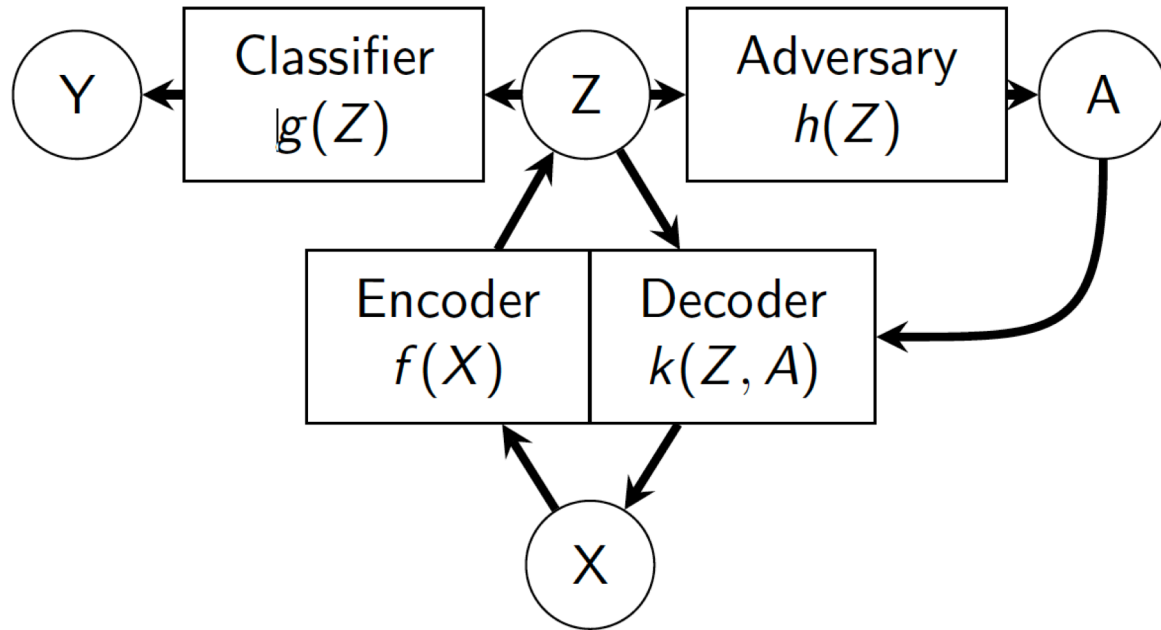


- Our game: encoder-decoder-classifier vs. adversary
- Aim: Learn fair encoder

$$\underset{f, g, k}{\text{minimize}} \underset{h}{\text{maximize}} \mathbb{E}_{X, Y, A} [\mathcal{L}(f, g, h, k)]$$

$$\mathcal{L}(f, g, h, k) = \alpha \mathcal{L}_{Class} + \beta \mathcal{L}_{Dec} - \gamma \mathcal{L}_{Adv}$$

# ADVERSARIAL OBJECTIVES



Choice of adversarial objective depends on fairness desideratum

- Demographic parity:  $\mathcal{L}_{DP}(h) = \sum_{i \in \{0,1\}} \frac{1}{|\mathcal{D}_i|} \sum_{(x,a) \in \mathcal{D}_i} |h(f(x)) - a|$
- Equalized odds:  $\mathcal{L}_{EO}(h) = \sum_{i,j \in \{0,1\}^2} \frac{1}{|\mathcal{D}_i^j|} \sum_{(x,a,y) \in \mathcal{D}_i^j} |h(f(x), y) - a|$
- Equal Opportunity:  $\mathcal{L}_{EOpp}(h) = \sum_{i \in \{0,1\}} \frac{1}{|\mathcal{D}_i^1|} \sum_{(x,a) \in \mathcal{D}_i^1} |h(f(x)) - a|$

# FROM ADVERSARIAL OBJECTIVES TO FAIRNESS DEFINITIONS

In general: pick the right adversarial loss, encourage the right conditional independencies

- Demographic parity encourages  $Z \perp A$  to fool adversary
- Equalized odds encourages  $Z \perp A \mid Y$  to fool adversary
- Equal opportunity encourages  $Z \perp A \mid Y = 1$  to fool adversary

Note that independencies of  $Z = f(x)$  also hold for predictions  $\hat{Y} = g(Z)$

**We show:** In the adversarial limit, these objectives guarantee these fairness metrics!

- The key is to connect predictability of  $A$  by the adversary  $h(Z)$  to unfairness in the classifier  $g(Z)$

# EXPERIMENTS

## Datasets

### 1. Adult Income

**Size:** 45,222 instances, 14 attributes

**Task:** predict whether or not annual income > 50K

**Sensitive feature:** Gender

### 2. Heritage Health

**Size:** 147,473 instances, 139 attributes

**Task:** predict patient's Charlson Index (co-morbidity)

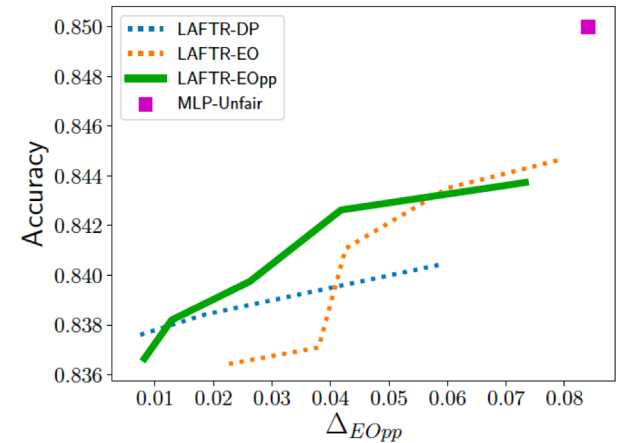
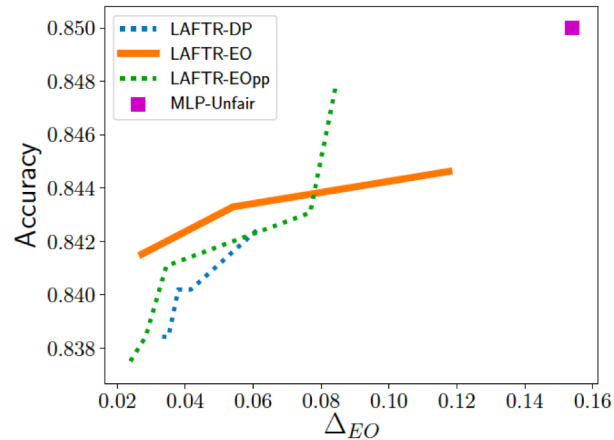
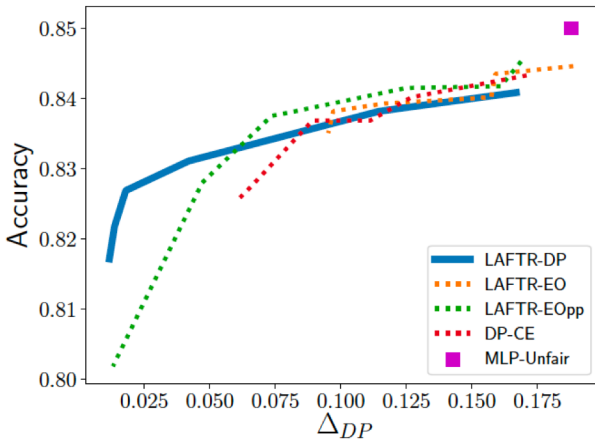
**Sensitive feature:** Age

## Models

Encoder, classifier, adversary: each single hidden-layer MLP (8; 20 hidden units)



# RESULTS: FAIR CLASSIFICATION



- Train with 2-step process to simulate owner  $\rightarrow$  vendor framework
- Tradeoffs between accuracy and fairness metrics produced by different LAFTR loss functions
- Achieves best solutions, wrt fairness-accuracy tradeoff

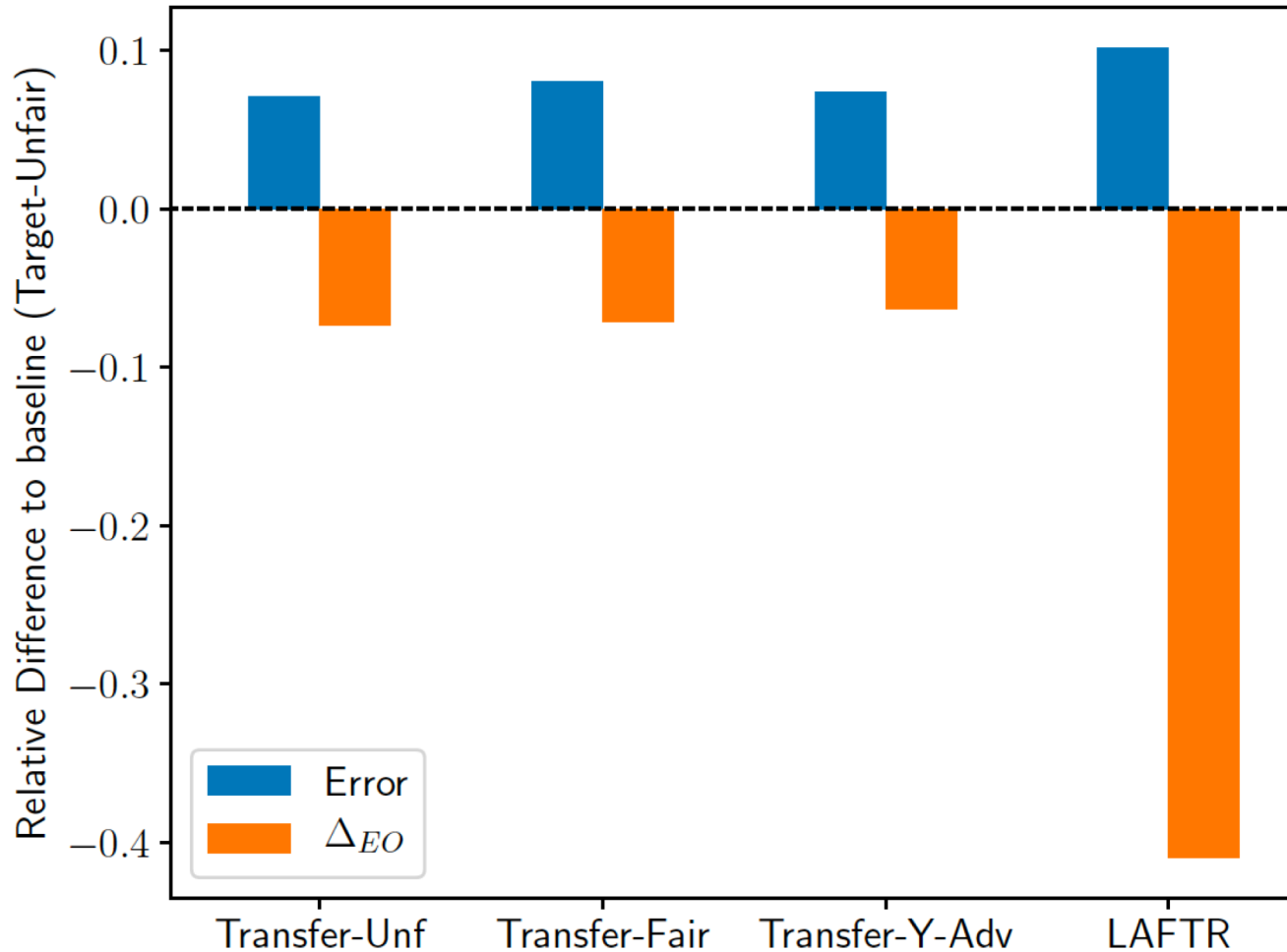
# RESULTS: FAIRNESS METRICS

METHOD	$\Delta_{DP}$	$\Delta_{EO}$	$\Delta_{EO_{pp}}$	ACC.
MLP (UNFAIR)	0.381	0.476	0.231	<b>0.785</b>
LAFTR-EO	0.152	<b>0.050</b>	0.036	0.763
	0.143	<b>0.052</b>	0.032	0.752
LAFTR-EO <sub>PP</sub>	0.087	0.092	<b>0.010</b>	0.742
	0.113	0.063	<b>0.024</b>	0.735
LAFTR-DP	<b>0.041</b>	0.140	0.025	0.731
	<b>0.002</b>	0.196	0.031	0.728

# SETUP: FAIR TRANSFER LEARNING

- Downstream vendors will have unknown prediction tasks
- Does fairness transfer?
- We test this as follows:
  - ① Train encoder  $f$  on data  $X$ , with label  $Y$
  - ② Freeze encoder  $f$
  - ③ On new data  $X'$ , train classifier on top of  $f(X')$ , with new task label  $Y'$
  - ④ Observe fairness and accuracy of this new classifier on new task  $Y'$
- Compare LAFTR encoder  $f$  to other encoders
- We use Heritage Health dataset
  - $Y$  is Charlson comorbidity index  $> 0$
  - $Y'$  is whether or not a certain type of insurance claim was made
  - Check for fairness w.r.t. age

# RESULTS : FAIR TRANSFER LEARNING



Fair transfer learning on Health dataset. Down is better in both metrics.

# ALTERNATIVE FORMULATIONS

Rather than an (un)fairness regularizer, can set up as constrained optimization problem

$$\max_{\phi \in \Phi} I_q(\mathbf{x}; \mathbf{z} | \mathbf{u}) \quad \text{s.t.} \quad I_q(\mathbf{z}; \mathbf{u}) < \epsilon$$

Learning Controllable Fair Representations (2018) by Song et al.

- Hard to compute and optimize these mutual information terms
- Propose tractable approximations, bounds to optimize
- Solve the dual

# ALTERNATIVE FORMULATIONS

Another popular approach is to adjust the input data, by removing features or pre-processing

- Data preprocessing techniques for classification without discrimination (2011), Kamiran & Calders
- Certifying and removing disparate impact (2015), Feldman et al.
- Optimized data pre-processing for discrimination prevention, Calmon et al.
- The case for process fairness in learning: Feature selection for fair decision making, Grgić-Hlača et al.