CS 448/2405

Automata and Formal Languages ASSIGNMENT # 1

NEW DUE DATE: Monday, February 6

- 1. Give deterministic finite automata accepting the following languages over $\{0, 1\}$.
 - a. The set of all strings not containing the substring 111.
 - b. The set of all strings of length at least four, and such that every block of four consecutive symbols contains at least 2 0's.
 - c. The set of all strings with at least three symbols such that the third symbol from the right end is 1.
- 2. Prove of disprove the following for regular expressions r, s and t.

a.
$$(rs + r)^* = r(sr + r)^*$$

b.
$$s(rs+s)^* = rr^*s(rr^*s)^*$$

c.
$$(r+s)^* = r^* + s^*$$

3. Are the following languages regular? Prove or disprove your answer.

a.
$$L = \{ w \mid w = w^R \}$$

b.
$$L = \{0^n \mid n \text{ is prime}\}$$

c.
$$L = \{0^n \mid n \text{ is even}\}$$

d.
$$L = \{0^n 1^m 0^n \mid m, n \ge 0\}$$

4. Sipser, Problem 1.57