

1. What is the condition number of the problem of evaluating

$$\tanh(cx) = \frac{\exp(cx) - \exp(-cx)}{\exp(cx) + \exp(-cx)} \quad (1)$$

as a function of $c > 0$?

2. (a) Show that

$$\ln(x - \sqrt{x^2 - 1}) = -\ln(x + \sqrt{x^2 - 1}) \quad (2)$$

(b) Which of the two formulas is more suitable for numerical computation?

3. The IEEE standard specifies 15 bits for the exponent in a 128-bit (quadruple precision) floating point system.

- (a) What is the length of the fraction?
- (b) What is the rounding unit?
- (c) How many significant decimal digits does this word have?
- (d) Why is quadruple precision more than twice as accurate as double precision (64 bits), which is in turn more than twice as accurate as single-precision (32 bits)?