Today

- We consider three ideas that have become staples of modern neural net training:
  1. Adaptive gradient methods (RMSprop, Adam, etc.)
  2. Normalization (esp. batch norm)
  3. Weight decay

- Deceptively simple, commonly misunderstood

- Unifying theme: you can figure out quite a lot by just reasoning about the scales of weights, activations, etc.
Adaptive Gradient Methods
Adaptive Gradient Methods

- So far, our algorithms have been forms of SGD, possibly preconditioned by some matrix $C^{-1}$ (Gauss-Newton Hessian, Fisher information, etc.)

$$w \leftarrow w - \alpha C^{-1} \nabla J_B(w)$$

- Another instance of this is the class of adaptive gradient methods, of which RMSprop is the simplest example:

$$g_k \leftarrow \nabla J_k(w_{k-1})$$

$$s_k \leftarrow \beta s_{k-1} + (1 - \beta) g_k^2$$

$$w_k \leftarrow w_{k-1} - \alpha g_k \odot \sqrt{s_k + \epsilon}$$

- **Intuition:** normalize the gradients to have unit variance.
- **Adam** is a similar algorithm which also includes a sort of momentum.
Adaptive Gradient Methods

\[ g_k \leftarrow \nabla J_k(w_{k-1}) \]
\[ s_k \leftarrow \beta s_{k-1} + (1 - \beta) g_k^2 \]
\[ w_k \leftarrow w_{k-1} - \alpha g_k \odot \sqrt{s_k + \epsilon} \]

- Here, \( s_k \) can be interpreted as the diagonal entries of the empirical Fisher matrix:
  \[ F_{\text{emp}} = \mathbb{E}_{x,t \sim p_{\text{data}}} [DwDw^\top] \]

- This is different from the true Fisher matrix. The true Fisher matrix samples \( t \) from the model’s predictions, while the empirical Fisher matrix uses the training labels.

- Since the denominator has a square root, we can view this as preconditioning with a diagonal approximation to \( F_{\text{emp}}^{-1/2} \).
Adaptive Gradient Methods

- We saw in Lecture 3 that the true Fisher matrix is closely related to the Hessian. The empirical Fisher matrix is often justified as an approximation to the Hessian for this reason.
  - It’s more convenient to compute, since you can avoid the additional step of sampling pseudo-gradients.
- But Kunstner et al. (2019) point out the empirical Fisher is often a lousy approximation to the Hessian.

Note: adaptive gradient methods (RMSprop, Adam, etc.) don’t actually behave like this because of the square root.
Adaptive Gradient Methods

- If the model is well-specified and fit well, then the generated labels will look like the training labels. Hence, $F_{\text{emp}}$ will resemble $F$ (and hence $H$, etc.).
- If the model is misspecified or the weights are far from the optimum, then these can look very different.

**Note:** this is not a criticism of adaptive gradient methods, which are based on a fundamentally different set of principles, originally developed for online learning!

Kunstner et al., 2019
I said today’s theme was thinking about algorithms in terms of how the magnitude of one quantity scales with another.

Using an adaptive gradient method rather than SGD changes both the magnitude and the direction of the weight update. Which one is important?

Agarwal et al. (2020) ran an intriguing experiment called grafting, where they use the magnitude from one optimizer and the direction from a different optimizer.
### Grafting

**Algorithm 2** AdaGraft meta-optimizer

1. **Input:** Optimizers $\mathcal{M}, \mathcal{D}$; initializer $w_1$; $\epsilon > 0$.
2. Initialize $\mathcal{M}, \mathcal{D}$ at $w_1$.
3. **for** $t = 1, \ldots, T$ **do**
   4. Receive stochastic gradient $g_t$ at $w_t$.
   5. Query steps from $\mathcal{M}$ and $\mathcal{D}$:
      \[
      w_M := \mathcal{M}(w_t, g_t), \quad w_D := \mathcal{D}(w_t, g_t).
      \]
   6. Update with grafted step:
      \[
      w_{t+1} \leftarrow w_t + \frac{\|w_M - w_t\|}{\|w_D - w_t\| + \epsilon} \cdot (w_D - w_t).
      \]
4. **end for**

---

- In practice, this is done per-layer rather than for the whole weight vector.

---

Agarwal et al., 2020
Grafting

- It’s known to be really hard to train transformers (e.g. BERT) with SGD. But grafting the Adam magnitudes onto SGD works just as well as Adam!

Agarwal et al., 2020
On the flip side, adaptive gradient methods are often seen to underperform SGD on image classification tasks (e.g. ImageNet). Grafting the magnitudes from SGD partly closes this gap.

So maybe the difference between SGD and adaptive gradient methods largely comes down to layerwise learning rate schedules?
Normalization
Batch Norm

From Ali Rahimi’s classic NeurIPS 2017 Test of Time talk (emphasis mine):

Batch Norm is a technique that speeds up gradient descent on deep nets. You sprinkle it between your layers and gradient descent goes faster. I think it’s ok to use techniques we don’t understand. I only vaguely understand how an airplane works, and I was fine taking one to this conference. But it’s always better if we build systems on top of things we do understand deeply? This is what we know about why batch norm works well. But don’t you want to understand why reducing internal covariate shift speeds up gradient descent? Don’t you want to see evidence that Batch Norm reduces internal covariate shift? Don’t you want to know what internal covariate shift is? Batch Norm has become a foundational operation for machine learning. It works amazingly well. But we know almost nothing about it.
Be careful about saying “nothing” is known!

Why should we expect “Why does batch norm help?” to have a simple answer that holds in all cases?

Some arguments made in the original 2015 paper (and often ignored by critics):

- Internal covariate shift leads to unstandardized activations, which hurts the conditioning
  - BN fixes this problem (by removing the ICS?)
- Prevent dead/saturated units
- Stochastic regularization effect caused by noisy estimates of the statistics
  - Maintain stability at high learning rates

A more recently discovered learning rate schedule effect
Internal Covariate Shift

- **Recall from Lecture 1:** for linear regression, uncentered activations create a large outlier eigenvalue, dramatically slowing down gradient descent
- For linear regression, we can solve this by explicitly centering the features
- For neural nets, the hidden activations can become uncentered, and there’s no straightforward fix
  - Pointed out by LeCun (1991)
  - The BN authors refer to this problem as **Internal Covariate Shift** (not a great name!)
- **Classical recommendation:** use tanh instead of logistic activations
Internal Covariate Shift

- We can make this reasoning more precise using more recent ideas.
- Recall the K-FAC approximation (Lecture 4):
  \[ \hat{G}_{\ell \ell} = A_{\ell-1} \otimes S_\ell \]

- Uncentered activations cause an outlier eigenvalue in \( A_{\ell-1} \)
- Recall (Lecture 4):
  - Spectral decomposition for symmetric \( A = Q_A D_A Q_A^T \) and \( B = Q_B D_B Q_B^T \)
  - Therefore, if the eigenvalues of \( A \) are \( \lambda_i \) and the eigenvalues of \( B \) are \( \nu_j \), then the eigenvalues of \( A \otimes B \) are the products \( \lambda_i \nu_j \)
  - If the corresponding eigenvectors of \( A \) are \( r_i \) and for \( B \) are \( s_j \), then the eigenvectors of \( A \otimes B \) are \( r_i \otimes s_j \)
This leads to:

**ICS Conditioning Hypothesis.** For a network with output dimension $M$, if $m = \mathbb{E}[a_{\ell-1}]$ is far from zero, we’d expect $G_{\ell\ell}$ to have as many as $M$ large eigenvalues, namely $\nu \lambda_i$ for each eigenvalue $\lambda_i$ of $S_{\ell}$, where $\nu = \|m\|^2 + 1$. The corresponding eigenvectors are of the form $m \otimes v$ for some vector $v$. 
ICS and Invariance

- Good scientific practice: change one thing at a time
- How can we eliminate the ill-conditioning effects of ICS while changing almost nothing else?
- **Idea:** standardize the activations using an affine transformation of the parameters

\[
\begin{align*}
a_\ell &= \phi(W_\ell a_{\ell-1} + b_\ell) \\
\tilde{a}_{\ell-1} &= \Sigma^{-1/2}(a_{\ell-1} - m)
\end{align*}
\]

- Transforming the weights so that the network computes the same function:

\[
\tilde{W}_\ell \tilde{a}_{\ell-1} + \tilde{b}_\ell = W_\ell a_{\ell-1} + b_\ell,
\]
achieved by

\[
\tilde{W}_\ell = W_\ell \Sigma^{1/2} \quad \tilde{b}_\ell = b_\ell + W_\ell m
\]

- Updates in this coordinate system are immune to ICS
ICS and Invariance

- Equivalent to pre-multiplying by $\mathbf{RR}^\top$, where

$$
\mathbf{R}^{-1} = \begin{pmatrix}
\Sigma^{1/2} \otimes \mathbf{I} & 0 \\
\mathbf{m}^\top \otimes \mathbf{I} & 1
\end{pmatrix}
$$

$$
[\mathbf{RR}^\top]^{-1} = \begin{pmatrix}
(\Sigma + \mathbf{mm}^\top) \otimes \mathbf{I} & \mathbf{m} \otimes \mathbf{I} \\
\mathbf{m}^\top \otimes \mathbf{I} & 1
\end{pmatrix}
$$

- The matrix $[\mathbf{RR}^\top]^{-1}$ is supposed to approximate $\mathbf{H}$.
- This matrix is “almost” diagonal, so preconditioners of this form are called quasi-diagonal
- Minimal overhead relative to ordinary neural net operations, just like diagonal preconditioning
Another way to arrive at quasi-diagonal preconditioners is to reason about invariance:

If the parameters are chosen such that these two networks compute the same function, then the same should be true after running the algorithm.

- Quasi-diagonal natural gradient is invariant to affine transformations of individual units (e.g. tanh vs. logistic)
- K-FAC is invariant to affine transformations of the layer as a whole
Batch Normalization
Batch Normalization

- Naïve motivation: if the architecture explicitly normalizes every unit, this eliminates ICS and improves the conditioning. Right?
- Batch normalization (BN):

\[ \tilde{X} = \text{BN}(X) = (X - 1\mu(X)\top) \odot 1\sigma(X)\top \]

- **Training time:** Statistics are estimated from the current batch
- **Test time:** Use averages of training statistics
- Typically apply BN to pre-activations rather than activations
- **Note:** in practice, we fit additional parameters for the mean and variance after normalization, but I’ll ignore these for this lecture
Batch Normalization

- Main difference from our preconditioning-based solution: BN is part of the architecture, so we differentiate through it.
- The computation graph contains a direct path and a statistics path:

```
... → X → \tilde{X} → ...
```

- Another difference: the statistics are estimated from the current batch, which injects noise.
Batch Normalization

- Preconditioning changes the conditioning of the cost function, and nothing else
- BN also changes the effective initialization, adds stochastic regularization, completely changes the scales of the gradients, ...
- Motivations from the original paper:
  - Ameliorating the optimization effects of ICS
  - Preventing dead or saturated units
  - Maintaining stability at higher learning rates
  - Stochastic regularization
- Additionally, there’s an important *implicit learning rate decay* effect which I believe the authors weren’t aware of
A Wrinkle
We argued that ICS creates outlier eigenvalues in the Hessian due to uncentered activations.

“ICS Conditioning Hypothesis”: BN helps by removing the outlier eigenvalues.

We can also formulate:

ICS Removal Hypothesis: BN improves optimization by centering and/or normalizing the previous layer’s activations.

These hypotheses are logically independent.

BN could remove the outlier eigenvalues through some means other than preventing ICS.

Preventing ICS could have some optimization benefit other than improving conditioning.
Two pieces of evidence against the ICS Removal Hypothesis:

- It generally works better to apply BN before the activation function, rather than after.

- Santurkar et al. (2018) ran a sort of knockout experiment where they added ICS back in and tested if BN still improved training:
  - I.e., after BN, linearly transform the activations to have some other mean and variance.
  - The network still trained just as efficiently.
Key insight: consider what happens when BN is applied in the next layer, before the activation function

\[ A_\ell = f_\ell(A_{\ell-1}, W_\ell) = \phi_\ell(BN(A_{\ell-1}W_{\ell}^T)) \]

This function is invariant to rescaling and shifting \( a_{\ell-1} \)

If the activations are shifted, the network still computes the same function (for any particular \( w \)), so the optimization trajectories are identical.

- The outlier eigenvalues of have no effect!

So the ICS Conditioning hypothesis could still be correct, even though the ICS Removal hypothesis appears to be incorrect

- Good class project to test this
A Wrinkle

- The same result can be derived by analyzing the mechanics of backprop through the BN operation.
- Consider *batch centering*, which centers but doesn’t scale the activations.
- It turns out (derivation in the readings):

\[
\overline{W} = \bar{S}^\top A \quad \text{(without BC)}
\]
\[
\overline{W} = \bar{S}^\top \tilde{A} \quad \text{(with BC)}
\]

where \( \tilde{A} \) are the centered activations.
- It’s the statistics path that’s responsible for this effect.
Implicit Learning Rate Decay
Implicit Learning Rate Decay

- Batch norm and other normalizers create an implicit learning rate decay effect
  - Even if you use a fixed learning rate, the training behaves as if you are gradually decaying the learning rate
- For this most part, this is probably beneficial — learning rate decay is very useful in stochastic optimization (Lecture 7)
- But it’s a major gotcha, since you probably aren’t expecting it, e.g.
  - Why does weight decay speed up optimization on the training set?
  - Different optimization algorithms can have different implicit decay schedules
  - This explains a significant fraction of confusing neural net phenomena
Implicit Learning Rate Decay

- The BN operation is invariant to rescaling the vector $w_j$ of incoming weights to a unit $j$ by a scalar $\gamma > 0$:
  \[
  \text{BN}(AW^\top) = \text{BN}(AW^\top \Gamma) \quad \text{for any diagonal matrix } \Gamma \succ 0.
  \]

- Therefore, each layer’s computations, and the network as a whole, are invariant to this rescaling:
  \[
  f_\ell(A, W) = f_\ell(A, \Gamma W)
  \]

- **Scale invariant** cost function:
A function $g$ is **homogeneous of degree** $k$ if

$$g(\gamma x) = \gamma^k g(x) \quad \text{for any } x$$

- Scale invariant = homogeneous of degree 0
- Euler showed that if $g$ is homogeneous of degree $k$, then
  $$\nabla g(\gamma x) = \gamma^{k-1} \nabla g(x)$$
- Since BN is scale invariant, its gradient is homogeneous of degree -1:
  $$\nabla J(\gamma w_j) = \gamma^{-1} \nabla J(w_j)$$
Implicit Learning Rate Decay

- Since the scale of $\mathbf{w}_j$ doesn’t matter, we can **canonicalize** it to a unit vector:
  \[ \hat{\mathbf{w}}_j = \frac{\mathbf{w}_j}{\|\mathbf{w}_j\|} \]

- Approximating the update to $\hat{\mathbf{w}}_j$:
  \[
  \hat{\mathbf{w}}^{(k+1)}_j \approx \frac{\mathbf{w}^{(k)}_j - \alpha \nabla \mathcal{J}(\mathbf{w}^{(k)}_j)}{\|\mathbf{w}^{(k)}_j - \alpha \nabla \mathcal{J}(\mathbf{w}^{(k)}_j)\|}
  \]
  \[
  \approx \mathbf{w}^{(k)}_j - \alpha \mathbf{w}^{(k)}_j \mathcal{J}(\mathbf{w}^{(k)}_j)
  \]
  \[
  = \hat{\mathbf{w}}^{(k)}_j - \alpha \|\mathbf{w}^{(k)}_j\|^{-1} \nabla \mathcal{J}(\mathbf{w}^{(k)}_j)
  \]
  \[
  = \hat{\mathbf{w}}^{(k)}_j \quad \text{effective LR}
  \]
  \[
  = \hat{\mathbf{w}}^{(k)}_j - \alpha \|\mathbf{w}^{(k)}_j\|^{-2} \nabla \mathcal{J}(\hat{\mathbf{w}}^{(k)}_j)
  \]
  \[
  \quad \text{effective gradient}
  \]
Implicit Learning Rate Decay

- Observe that $\|w_j\|$ increases monotonically.
- Since $w_j \perp \nabla J(w_j)$, we can apply the Pythagorean Theorem:

$$\|w_j^{(k+1)}\|^2 = \|w_j^{(k)} + \alpha \nabla J(w_j^{(k)})\|^2$$

$$= \|w_j^{(k)}\|^2 + \alpha^2 \|\nabla J(w_j^{(k)})\|^2$$

$$= \|w_j^{(k)}\|^2 + \frac{\alpha^2 \|\nabla J(\hat{w}_j^{(k)})\|^2}{\|w_j^{(k)}\|^2}$$
Implicit Learning Rate Decay

- If \( \| \nabla J(\hat{w}_j^{(k)}) \| \) is constant throughout training (admittedly a bad assumption), then the weight norm grows roughly as:
  \[
  \| w_j^{(k)} \|^2 \propto \sqrt{1 + k/k_0}
  \]
  for some \( k_0 \)

- This translates into an effective learning rate schedule:
  \[
  \hat{\alpha}_k = \frac{\hat{\alpha}_0}{\sqrt{1 + k/k_0}}
  \]

- The explicit learning rate hyperparameter \( \alpha \) gives you surprisingly little control over the effective learning rate.

![Graphs showing weight norm and effective learning rate over iterations for different values of alpha.](image)
Implicit Learning Rate Decay

- **Bengio (2012):**
  
  *The [learning rate] is often the single most important hyperparameter and one should always make sure that it has been tuned (up to approximately a factor of 2)… If there is only time to optimize one hyper-parameter and one uses stochastic gradient descent, then this is the hyper-parameter that is worth tuning.*

- **Today: not a big deal**

- **Aside:** Cohen et al., “Gradient descent in neural networks typically occurs at the edge of stability” showed that even in non-BN networks, for full-batch gradient descent, the network’s curvature adapts to compensate for the learning rate, through a completely different mechanism!
Counteracting the implicit LR effect:

- Exponentially increasing LR schedule (Li and Arora, 2020)
- Use weight decay (up next!)
- Explicitly normalize each $w_j$ to unit norm
  - Then the effective LR is just $\alpha$
  - This is not common practice, but I expect it could eliminate a lot of experimental confounds
The above argument suggests that BN implements a $O(1/\sqrt{k})$ decay schedule.

Some reasons this is not exactly true:

- Above analysis assumes $\|\nabla J(\hat{w}_j^{(k)})\|$ is constant, which is hopefully not the case (if you succeeded in learning anything!)
- Separate learning rate for each unit (so features that have already changed a lot get slowed down more) — maybe a sort of feedback control
- Effect doesn’t apply to the output layer, which doesn’t feed into BN — therefore, the output layer trains faster later in training
- Different algorithms can have different decay schedules
  - E.g. K-FAC is invariant to affine transformations, and therefore immune to this effect
Weight Decay
Weight Decay as $L^2$ Regularization

Weight decay is one of the oldest tricks in the book. It was traditionally understood as $L^2$ regularization, or Tikhonov regularization.

- We can encourage the weights to be small by choosing as our regularizer the $L^2$ penalty.

\[
\mathcal{R}(w) = \frac{1}{2} \|w\|^2 = \frac{1}{2} \sum_j w_j^2.
\]

- Gradient descent update:

\[
w \leftarrow w - \alpha \nabla_w \left( J(w) + \frac{\lambda}{2} \|w\|^2 \right) = (1 - \alpha \lambda)w - \alpha \nabla J(w)
\]
Weight Decay as $L^2$ Regularization

- If this interpretation were correct, then if we used a different optimizer, we’d compute the update on the same ($L^2$ regularized) objective.

- Update rule if we precondition by a matrix $C$:

$$ w \leftarrow w - \alpha C^{-1} \nabla_w \left( J(w) + \frac{\lambda}{2} \|w\|^2 \right) $$

$$ = (I - \alpha \lambda C^{-1})w - \alpha C^{-1} \nabla J(w) $$

- However, we could also just apply “literal weight decay”:

$$ w \leftarrow (1 - \alpha \lambda)w - \alpha C^{-1} \nabla J(w) $$
But for various optimization algorithms, it works much better to literally apply weight decay, even though this appears to be optimizing a different function!

**Algorithm 2** Adam with $L_2$ regularization and Adam with decoupled weight decay (AdamW)

1: **given** $\alpha = 0.001, \beta_1 = 0.9, \beta_2 = 0.999, \epsilon = 10^{-8}, \lambda \in \mathbb{R}$
2: **initialize** time step $t \leftarrow 0$, parameter vector $\theta_{t=0} \in \mathbb{R}^n$, first moment vector $m_{t=0} \leftarrow \theta$, second moment vector $v_{t=0} \leftarrow \theta$, schedule multiplier $\eta_{t=0} \in \mathbb{R}$
3: **repeat**
   
4:   $t \leftarrow t + 1$
5:   $\nabla f_t(\theta_{t-1}) \leftarrow \text{SelectBatch}(\theta_{t-1})$
6:   $g_t \leftarrow \nabla f_t(\theta_{t-1}) + \lambda \theta_{t-1}$
7:   $m_t \leftarrow \beta_1 m_{t-1} + (1 - \beta_1) g_t$
8:   $v_t \leftarrow \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$
9:   $\tilde{m}_t \leftarrow m_t / (1 - \beta_1^t)$
10:  $\tilde{v}_t \leftarrow v_t / (1 - \beta_2^t)$
11:  $\eta_t \leftarrow \text{SetScheduleMultiplier}(t)$
12:  $\theta_t \leftarrow \theta_{t-1} - \eta_t \left( \frac{\tilde{m}_t}{\sqrt{\tilde{v}_t} + \epsilon} \right) + \lambda \theta_{t-1}$
13: **until** stopping criterion is met
14: **return** optimized parameters $\theta_t$

Loschilov and Hutter, 2019
Literal weight decay works much better than $L^2$ regularization in the context of KFAC as well.

Zhang et al., 2019
Batch Norm is scale-invariant, so rescaling the weights of any layer which feeds into batch norm results in an equivalent network.

Therefore, $L^2$ regularization should not affect the capacity of a batch norm network. You can make the penalty arbitrarily small just by rescaling the weights.

Yet, it seems to matter a lot.

My student Guodong produced experimental results that seemed to contradict every theory we had for what weight decay is doing.

After much frustration, we realized the reason things were so confusing was that weight decay was improving generalization through (at least) 3 completely different mechanisms, depending on the situation!
Three Mechanisms

Mechanism 1: Implicit learning rates.

- We saw earlier that when SGD is used as the optimizer, batch norm creates an implicit learning rate decay schedule.
  - Weights get smaller over time ⇒ implicit learning rate decay
- Weight decay keeps the weights small, preventing the learning rate from decaying too much.
- Assuming unit norm of the gradient, it can be shown that the effective learning rate asymptotes to $\alpha \lambda$ (see readings).
Three Mechanisms

- We can test this explanation with **norm grafting**:
  - Train networks both with and without WD
  - After each iteration, rescale the weights of the non-WD network so that their norms match the WD network.
  - Note: This is done only for layers that feed into batch norm.
- By scale invariance, this manipulation affects only the implicit learning rate.
- This nearly closes the generalization gap.
Three Mechanisms

- This mechanism doesn’t apply to KFAC because KFAC is “nearly” invariant to affine transformations.
  - Rescaling the weights is an affine transformation, so KFAC is immune to the implicit learning rate decay.
  - I say “nearly” because the damping term is not invariant.
Mechanism 2: Jacobian regularization.

We can “reverse engineer” the regularizer that a preconditioned WD update is minimizing:

\[ w \leftarrow (1 - \alpha \lambda) w - \alpha C^{-1} \nabla J(w) \]

\[ = w - \alpha C^{-1} \nabla_w \left[ J(w) + \frac{\lambda}{2} w^\top C w \right] \]

Note: this derivation is only approximate, because it is treating \( C \) as fixed, whereas for algorithms like KFAC, it depends on \( w \).
Three Mechanisms

- Surprisingly, when $C$ is the KFAC approximation $\hat{G}$ to the Gauss-Newton matrix, this regularizer is closely related to the norm of the network Jacobian $J$.

- This holds exactly for linear networks with no biases and whitened inputs:
  \[ w^\top \hat{G} w = (L + 1) \| J \|^2_F, \]
  where $L$ is the number of layers.

- There is a pretty good empirical fit even for nonlinear networks!
Three Mechanisms

- **Mechanism 3: Damping strength.**
  - For KFAC, the approximate curvature matrix $\hat{G}$ is replaced with $\hat{G} + \gamma I$ before inversion.
  - The smaller $\hat{G}$ is, the stronger the effect of the damping, and the more KFAC behaves like a first-order optimizer (SGD).
    - When the curvature is the Fisher information $F$, it gets smaller over the course of optimization, and KFAC reduces to SGD. Weight decay attenuates this effect.
    - When the curvature is the Gauss-Newton matrix, this doesn’t happen.
Three Mechanisms: Discussion

- Why do we find neural nets so hard to understand?
- It’s tempting to assume there’s some fundamental insight we’re missing.
- But in situations like the ones covered today (BN, WD), the mechanisms are straightforward once you know where to look.
  - What makes it hard is that different principles may apply in different situations, making it hard to find a one-size-fits-all explanation.
  - Imagine asking an organic chemist, “What does nitrogen do?”
- Much of what makes science challenging is determining what observations deserve to be studied as a single phenomenon.
  - The pipeline of “practitioners notice things, then theorists explain them” doesn’t really work. You need a good mental model of what’s going on even to know what experiments to run.