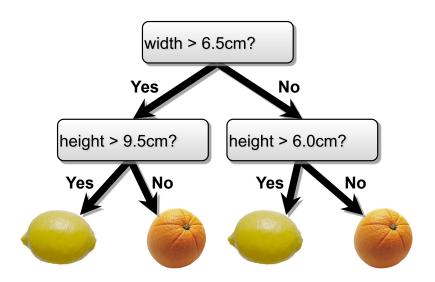
CSC 2515 Lecture 2: Decision Trees and Ensembles

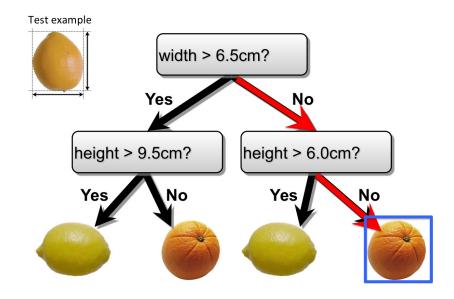
Roger Grosse

University of Toronto

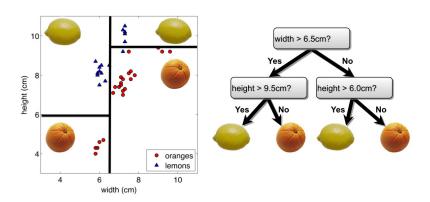
Overview

- Decision Trees
 - ► Simple but powerful learning algorithm
 - ▶ One of the most widely used learning algorithms in Kaggle competitions
- Lets us introduce ensembles, a key idea in ML more broadly
- Useful information theoretic concepts (entropy, mutual information, etc.)





 Decision trees make predictions by recursively splitting on different attributes according to a tree structure.



Example with Discrete Inputs

• What if the attributes are discrete?

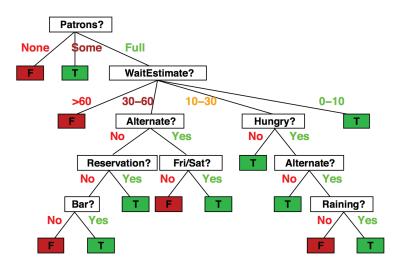
Example Input Attributes						Goal					
- Litempie	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
\mathbf{x}_1	Yes	No	No	Yes	Some	\$\$\$	No	Yes	French	0–10	$y_1 = \textit{Yes}$
\mathbf{x}_2	Yes	No	No	Yes	Full	\$	No	No	Thai	30–60	$y_2 = No$
\mathbf{x}_3	No	Yes	No	No	Some	\$	No	No	Burger	0–10	$y_3 = \textit{Yes}$
\mathbf{x}_4	Yes	No	Yes	Yes	Full	\$	Yes	No	Thai	10-30	$y_4 = \textit{Yes}$
\mathbf{x}_5	Yes	No	Yes	No	Full	\$\$\$	No	Yes	French	>60	$y_5 = No$
\mathbf{x}_6	No	Yes	No	Yes	Some	\$\$	Yes	Yes	Italian	0–10	$y_6 = \textit{Yes}$
\mathbf{x}_7	No	Yes	No	No	None	\$	Yes	No	Burger	0–10	$y_7 = No$
\mathbf{x}_8	No	No	No	Yes	Some	\$\$	Yes	Yes	Thai	0–10	$y_8 = \textit{Yes}$
\mathbf{x}_9	No	Yes	Yes	No	Full	\$	Yes	No	Burger	>60	$y_9 = \mathit{No}$
\mathbf{x}_{10}	Yes	Yes	Yes	Yes	Full	\$\$\$	No	Yes	Italian	10-30	$y_{10} = No$
\mathbf{x}_{11}	No	No	No	No	None	\$	No	No	Thai	0–10	$y_{11} = No$
\mathbf{x}_{12}	Yes	Yes	Yes	Yes	Full	\$	No	No	Burger	30–60	$y_{12} = \textit{Yes}$

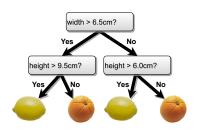
1.	Alternate: whether there is a suitable alternative restaurant nearby.
2.	Bar: whether the restaurant has a comfortable bar area to wait in.
3.	Fri/Sat: true on Fridays and Saturdays.
4.	Hungry: whether we are hungry.
5.	Patrons: how many people are in the restaurant (values are None, Some, and Full).
6.	Price: the restaurant's price range (\$, \$\$, \$\$\$).
7.	Raining: whether it is raining outside.
8.	Reservation: whether we made a reservation.
9.	Type: the kind of restaurant (French, Italian, Thai or Burger).
10.	WaitEstimate: the wait estimated by the host (0-10 minutes, 10-30, 30-60, >60).

Attributes:

Decision Tree: Example with Discrete Inputs

• The tree to decide whether to wait (T) or not (F)

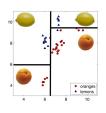




- Internal nodes test attributes
- Branching is determined by attribute value
- Leaf nodes are outputs (predictions)

Decision Tree: Classification and Regression

- Each path from root to a leaf defines a region R_m of input space
- Let $\{(x^{(m_1)}, t^{(m_1)}), \dots, (x^{(m_k)}, t^{(m_k)})\}$ be the training examples that fall into R_m



Classification tree:

- discrete output
- ▶ leaf value y^m typically set to the most common value in $\{t^{(m_1)}, \dots, t^{(m_k)}\}$

Regression tree:

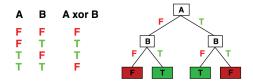
- continuous output
- ▶ leaf value y^m typically set to the mean value in $\{t^{(m_1)}, \ldots, t^{(m_k)}\}$

Note: We will focus on classification

[Slide credit: S. Russell]

Expressiveness

- Discrete-input, discrete-output case:
 - Decision trees can express any function of the input attributes
 - ightharpoonup E.g., for Boolean functions, truth table row ightarrow path to leaf:



- Continuous-input, continuous-output case:
 - Can approximate any function arbitrarily closely
- Trivially, there is a consistent decision tree for any training set w/ one path
 to leaf for each example (unless f nondeterministic in x) but it probably
 won't generalize to new examples

[Slide credit: S. Russell]

How do we Learn a DecisionTree?

• How do we construct a useful decision tree?

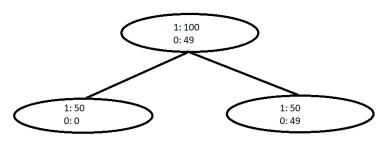
Learning Decision Trees

Learning the simplest (smallest) decision tree is an NP complete problem [if you are interested, check: Hyafil & Rivest'76]

- Resort to a greedy heuristic:
 - Start from an empty decision tree
 - ▶ Split on the "best" attribute
 - Recurse
- Which attribute is the "best"?
 - Choose based on accuracy?

Choosing a Good Split

• Why isn't accuracy a good measure?



- Is this split good? Zero accuracy gain.
- Instead, we will use techniques from information theory

Idea: Use counts at leaves to define probability distributions, so we can measure uncertainty

Choosing a Good Split

- Which attribute is better to split on, X_1 or X_2 ?
 - Deterministic: good (all are true or false; just one class in the leaf)
 - Uniform distribution: bad (all classes in leaf equally probable)
 - ▶ What about distributons in between?

Note: Let's take a slight detour and remember concepts from information theory

[Slide credit: D. Sontag]

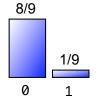
We Flip Two Different Coins

```
Sequence 1:
00010000000000100...?
Sequence 2:
010101110100110101...?
    16
                          10
                      8
             versus
     0
```

Quantifying Uncertainty

Entropy is a measure of expected "surprise":

$$H(X) = -\sum_{x \in X} p(x) \log_2 p(x)$$







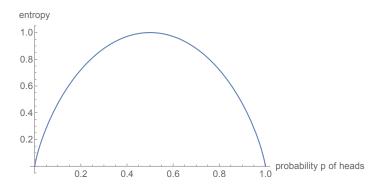
$$-\frac{8}{9}\log_2\frac{8}{9} - \frac{1}{9}\log_2\frac{1}{9} \approx \frac{1}{2}$$

$$-\frac{4}{9}\log_2\frac{4}{9} - \frac{5}{9}\log_2\frac{5}{9} \approx 0.99$$

- Measures the information content of each observation
- Unit = bits
- A fair coin flip has 1 bit of entropy

Quantifying Uncertainty

$$H(X) = -\sum_{x \in X} p(x) \log_2 p(x)$$



Entropy

• "High Entropy":

- Variable has a uniform like distribution
- Flat histogram
- Values sampled from it are less predictable

"Low Entropy"

- Distribution of variable has many peaks and valleys
- Histogram has many lows and highs
- Values sampled from it are more predictable

[Slide credit: Vibhav Gogate]

Entropy of a Joint Distribution

• Example: $X = \{\text{Raining, Not raining}\}, Y = \{\text{Cloudy, Not cloudy}\}$

	Cloudy	Not Cloudy
Raining	24/100	1/100
Not Raining	25/100	50/100

$$H(X,Y) = -\sum_{x \in X} \sum_{y \in Y} p(x,y) \log_2 p(x,y)$$

$$= -\frac{24}{100} \log_2 \frac{24}{100} - \frac{1}{100} \log_2 \frac{1}{100} - \frac{25}{100} \log_2 \frac{25}{100} - \frac{50}{100} \log_2 \frac{50}{100}$$

$$\approx 1.56 \text{bits}$$

Specific Conditional Entropy

 $\bullet \ \, \mathsf{Example:} \ \, X = \{ \mathsf{Raining}, \, \mathsf{Not} \, \, \mathsf{raining} \}, \, \, Y = \{ \mathsf{Cloudy}, \, \mathsf{Not} \, \, \mathsf{cloudy} \}$

	Cloudy	Not Cloudy
Raining	24/100	1/100
Not Raining	25/100	50/100

• What is the entropy of cloudiness Y, given that it is raining?

$$H(Y|X = x) = -\sum_{y \in Y} p(y|x) \log_2 p(y|x)$$

$$= -\frac{24}{25} \log_2 \frac{24}{25} - \frac{1}{25} \log_2 \frac{1}{25}$$

$$\approx 0.24 \text{bits}$$

• We used: $p(y|x) = \frac{p(x,y)}{p(x)}$, and $p(x) = \sum_{y} p(x,y)$ (sum in a row)

Conditional Entropy

	Cloudy	Not Cloudy
Raining	24/100	1/100
Not Raining	25/100	50/100

The expected conditional entropy:

$$H(Y|X) = \sum_{x \in X} p(x)H(Y|X = x)$$
$$= -\sum_{x \in X} \sum_{y \in Y} p(x,y)\log_2 p(y|x)$$

Conditional Entropy

• Example: $X = \{\text{Raining, Not raining}\}, Y = \{\text{Cloudy, Not cloudy}\}$

	Cloudy	Not Cloudy
Raining	24/100	1/100
Not Raining	25/100	50/100

• What is the entropy of cloudiness, given the knowledge of whether or not it is raining?

$$H(Y|X) = \sum_{x \in X} p(x)H(Y|X = x)$$

$$= \frac{1}{4}H(\text{cloudy}|\text{is raining}) + \frac{3}{4}H(\text{cloudy}|\text{not raining})$$

$$\approx 0.75 \text{ bits}$$

Conditional Entropy

- Some useful properties:
 - ▶ *H* is always non-negative
 - Chain rule: H(X, Y) = H(X|Y) + H(Y) = H(Y|X) + H(X)
 - ▶ If X and Y independent, then X doesn't tell us anything about Y: H(Y|X) = H(Y)
 - ▶ But Y tells us everything about Y: H(Y|Y) = 0
 - ▶ By knowing X, we can only decrease uncertainty about Y: $H(Y|X) \le H(Y)$

Information Gain

	Cloudy	Not Cloudy
Raining	24/100	1/100
Not Raining	25/100	50/100

• How much information about cloudiness do we get by discovering whether it is raining?

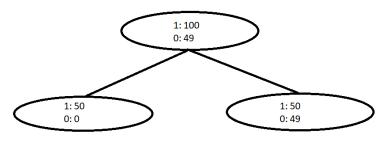
$$IG(Y|X) = H(Y) - H(Y|X)$$

 $\approx 0.25 \text{ bits}$

- This is called the information gain in Y due to X, or the mutual information of Y and X
- If X is completely uninformative about Y: IG(Y|X) = 0
- If X is completely informative about Y: IG(Y|X) = H(Y)

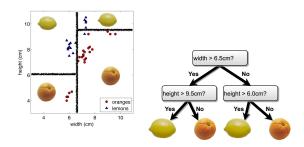
Revisiting Our Original Example

- Information gain measures the informativeness of a variable, which is exactly what we desire in a decision tree attribute!
- What is the information gain of this split?



- Root entropy: $H(Y) = -\frac{49}{149}\log_2(\frac{49}{149}) \frac{100}{149}\log_2(\frac{100}{149}) \approx 0.91$
- Leafs entropy: H(Y|left) = 0, $H(Y|right) \approx 1$.
- $IG(split) \approx 0.91 (\frac{1}{3} \cdot 0 + \frac{2}{3} \cdot 1) \approx 0.24 > 0$

Constructing Decision Trees



- At each level, one must choose:
 - 1. Which variable to split.
 - 2. Possibly where to split it.
- Choose them based on how much information we would gain from the decision! (choose attribute that gives the highest gain)

Decision Tree Construction Algorithm

- Simple, greedy, recursive approach, builds up tree node-by-node
- 1. pick an attribute to split at a non-terminal node
- 2. split examples into groups based on attribute value
- 3. for each group:
 - ▶ if no examples return majority from parent
 - else if all examples in same class return class
 - else loop to step 1

Back to Our Example

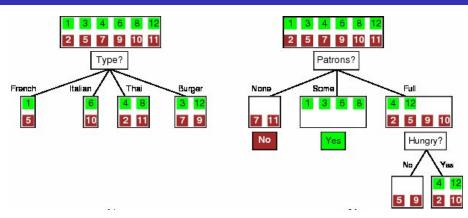
Example	Input Attributes									
Litempie	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est
\mathbf{x}_1	Yes	No	No	Yes	Some	\$\$\$	No	Yes	French	0–10
\mathbf{x}_2	Yes	No	No	Yes	Full	\$	No	No	Thai	<i>30–60</i>
\mathbf{x}_3	No	Yes	No	No	Some	\$	No	No	Burger	0–10
\mathbf{x}_4	Yes	No	Yes	Yes	Full	\$	Yes	No	Thai	10–30
\mathbf{x}_5	Yes	No	Yes	No	Full	\$\$\$	No	Yes	French	>60
\mathbf{x}_6	No	Yes	No	Yes	Some	\$\$	Yes	Yes	Italian	0–10
\mathbf{x}_7	No	Yes	No	No	None	\$	Yes	No	Burger	0–10
\mathbf{x}_8	No	No	No	Yes	Some	\$\$	Yes	Yes	Thai	0–10
\mathbf{x}_9	No	Yes	Yes	No	Full	\$	Yes	No	Burger	>60
\mathbf{x}_{10}	Yes	Yes	Yes	Yes	Full	\$\$\$	No	Yes	Italian	10-30
\mathbf{x}_{11}	No	No	No	No	None	\$	No	No	Thai	0–10
\mathbf{x}_{12}	Yes	Yes	Yes	Yes	Full	\$	No	No	Burger	30–60

Goal					
WillV	Vait				
$y_1 =$	Yes				
$y_2 =$	No				
$y_3 =$	Yes				
$y_4 =$	Yes				
$y_5 =$	No				
$y_6 =$	Yes				
$y_7 =$	No				
$y_8 =$	Yes				
$y_9 =$	No				
$y_{10} =$	No				
$y_{11} =$	No				
$y_{12} =$	Yes				

1.	Alternate: whether there is a suitable alternative restaurant nearby.
2.	Bar: whether the restaurant has a comfortable bar area to wait in.
3.	Fri/Sat: true on Fridays and Saturdays.
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10.	WaitEstimate: the wait estimated by the host (0-10 minutes, 10-30, 30-60, >60).

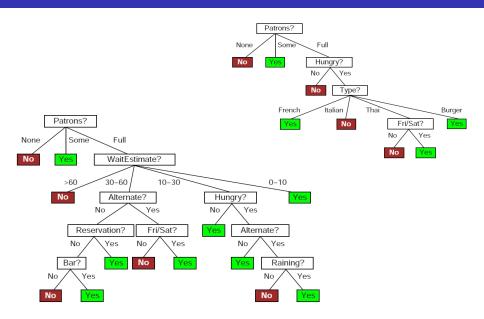
[from: Russell & Norvig]

Attribute Selection



$$\begin{split} \textit{IG}(Y) &= \textit{H}(Y) - \textit{H}(Y|X) \\ \textit{IG}(\textit{type}) &= 1 - \left[\frac{2}{12} \textit{H}(Y|\text{Fr.}) + \frac{2}{12} \textit{H}(Y|\text{It.}) + \frac{4}{12} \textit{H}(Y|\text{Thai}) + \frac{4}{12} \textit{H}(Y|\text{Bur.}) \right] = 0 \\ \textit{IG}(\textit{Patrons}) &= 1 - \left[\frac{2}{12} \textit{H}(0,1) + \frac{4}{12} \textit{H}(1,0) + \frac{6}{12} \textit{H}(\frac{2}{6},\frac{4}{6}) \right] \approx 0.541 \end{split}$$

Which Tree is Better?



What Makes a Good Tree?

- Not too small: need to handle important but possibly subtle distinctions in data
- Not too big:
 - Computational efficiency (avoid redundant, spurious attributes)
 - Avoid over-fitting training examples
 - Human interpretability
- "Occam's Razor": find the simplest hypothesis that fits the observations
 - Useful principle, but hard to formalize (how to define simplicity?)
 - See Domingos, 1999, "The role of Occam's razor in knowledge discovery"
- We desire small trees with informative nodes near the root

Decision Tree Miscellany

- Problems:
 - You have exponentially less data at lower levels
 - Too big of a tree can overfit the data
 - Greedy algorithms don't necessarily yield the global optimum
- Handling continuous attributes
 - ▶ Split based on a threshold, chosen to maximize information gain
- Decision trees can also be used for regression on real-valued outputs. Choose splits to minimize squared error, rather than maximize information gain.

Comparison to k-NN

Advantages of decision trees over KNN

- Good when there are lots of attributes, but only a few are important
- Good with discrete attributes
- Easily deals with missing values (just treat as another value)
- Robust to scale of inputs
- Fast at test time
- More interpretable

Advantages of KNN over decision trees

- Few hyperparameters
- Able to handle attributes/features that interact in complex ways (e.g. pixels)
- Can incorporate interesting distance measures (e.g. shape contexts)
- Typically make better predictions in practice
 - As we'll see next lecture, ensembles of decision trees are much stronger. But they lose many of the advantages listed above.

Ensembles and Bagging

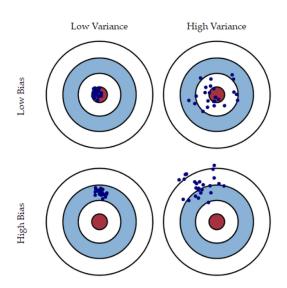
Ensemble methods: Overview

- An ensemble of predictors is a set of predictors whose individual decisions are combined in some way to classify new examples
 - ► E.g., (possibly weighted) majority vote
- For this to be nontrivial, the classifiers must differ somehow, e.g.
 - ▶ Different algorithm
 - Different choice of hyperparameters
 - Trained on different data
 - Trained with different weighting of the training examples
- Ensembles are usually trivial to implement. The hard part is deciding what kind of ensemble you want, based on your goals.

Ensemble methods: Overview

- This lecture: bagging
 - ► Train classifiers independently on random subsets of the training data.
- Later lecture: boosting
 - ► Train classifiers sequentially, each time focusing on training examples that the previous ones got wrong.
- Bagging and boosting serve very different purposes. To understand this, we need to take a detour to understand the bias and variance of a learning algorithm.

Bias and Variance



Loss Functions

- A loss function L(y, t) defines how bad it is if the algorithm predicts y, but the target is actually t.
- Example: 0-1 loss for classification

$$L_{0-1}(y,t) = \begin{cases} 0 & \text{if } y = t \\ 1 & \text{if } y \neq t \end{cases}$$

- ► Averaging the 0-1 loss over the training set gives the training error rate, and averaging over the test set gives the test error rate.
- Example: squared error loss for regression

$$L_{\rm SE}(y,t) = \frac{1}{2}(y-t)^2$$

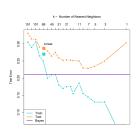
► The average squared error loss is called mean squared error (MSE).

Bias-Variance Decomposition

 Recall that overly simple models underfit the data, and overly complex models overfit



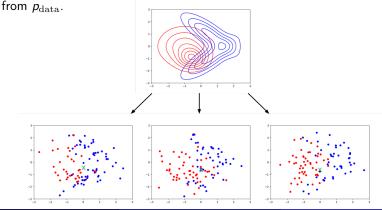




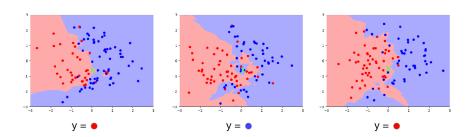
- We can quantify this effect in terms of the bias/variance decomposition.
 - ▶ Bias and variance of what?

- Suppose the training set \mathcal{D} consists of pairs (\mathbf{x}_i, t_i) sampled independent and identically distributed (i.i.d.) from a single data generating distribution p_{data} .
- Pick a fixed query point x (denoted with a green x).

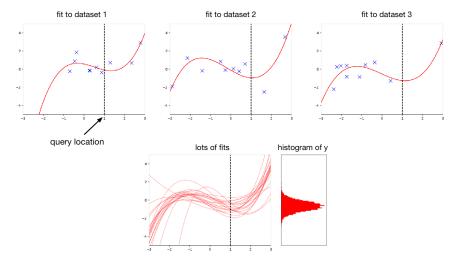
• Consider an experiment where we sample lots of training sets independently



- Let's run our learning algorithm on each training set, and compute its prediction *y* at the query point **x**.
- We can view y as a random variable, where the randomness comes from the choice of training set.
- The classification accuracy is determined by the distribution of y.

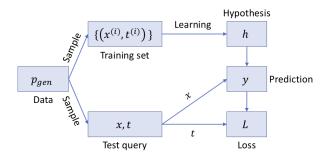


Here is the analogous setup for regression:



Since y is a random variable, we can talk about its expectation, variance, etc.

• Recap of basic setup:



- Notice: y is independent of t. (Why?)
- This gives a distribution over the loss at \mathbf{x} , with expectation $\mathbb{E}[L(y,t) \,|\, \mathbf{x}]$.
- For each query point ${\bf x}$, the expected loss is different. We are interested in minimizing the expectation of this with respect to ${\bf x} \sim p_{\rm data}$.

- For now, focus on squared error loss, $L(y, t) = \frac{1}{2}(y t)^2$.
- A first step: suppose we knew the conditional distribution $p(t | \mathbf{x})$. What value y should we predict?
 - \blacktriangleright Here, we are treating t as a random variable and choosing y.
- Claim: $y_* = \mathbb{E}[t \mid \mathbf{x}]$ is the best possible prediction.
- Proof:

$$\mathbb{E}[(y-t)^2 \mid \mathbf{x}] = \mathbb{E}[y^2 - 2yt + t^2 \mid \mathbf{x}]$$

$$= y^2 - 2y\mathbb{E}[t \mid \mathbf{x}] + \mathbb{E}[t^2 \mid \mathbf{x}]$$

$$= y^2 - 2y\mathbb{E}[t \mid \mathbf{x}] + \mathbb{E}[t \mid \mathbf{x}]^2 + \mathsf{Var}[t \mid \mathbf{x}]$$

$$= y^2 - 2yy_* + y_*^2 + \mathsf{Var}[t \mid \mathbf{x}]$$

$$= (y - y_*)^2 + \mathsf{Var}[t \mid \mathbf{x}]$$

$$\mathbb{E}[(y-t)^2 \,|\, \mathbf{x}] = (y-y_*)^2 + \mathsf{Var}[t \,|\, \mathbf{x}]$$

- The first term is nonnegative, and can be made 0 by setting $y = y_*$.
- The second term corresponds to the inherent unpredictability, or noise, of the targets, and is called the Bayes error.
 - ► This is the best we can ever hope to do with any learning algorithm. An algorithm that achieves it is Bayes optimal.
 - ▶ Notice that this term doesn't depend on y.
- This process of choosing a single value y_* based on $p(t | \mathbf{x})$ is an example of decision theory.

- Now return to treating y as a random variable (where the randomness comes from the choice of dataset).
- We can decompose out the expected loss (suppressing the conditioning on x for clarity):

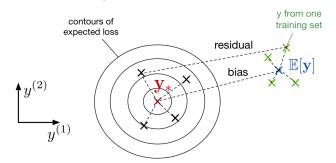
$$\begin{split} \mathbb{E}[(y-t)^2] &= \mathbb{E}[(y-y_*)^2] + \mathsf{Var}(t) \\ &= \mathbb{E}[y_*^2 - 2y_*y + y^2] + \mathsf{Var}(t) \\ &= y_*^2 - 2y_*\mathbb{E}[y] + \mathbb{E}[y^2] + \mathsf{Var}(t) \\ &= y_*^2 - 2y_*\mathbb{E}[y] + \mathbb{E}[y]^2 + \mathsf{Var}(y) + \mathsf{Var}(t) \\ &= \underbrace{(y_* - \mathbb{E}[y])^2}_{\text{bias}} + \underbrace{\mathsf{Var}(y)}_{\text{variance}} + \underbrace{\mathsf{Var}(t)}_{\text{Bayes error}} \end{split}$$

$$\mathbb{E}[(y-t)^2] = \underbrace{(y_* - \mathbb{E}[y])^2}_{\text{bias}} + \underbrace{\text{Var}(y)}_{\text{variance}} + \underbrace{\text{Var}(t)}_{\text{Bayes error}}$$

- We just split the expected loss into three terms:
 - bias: how wrong the expected prediction is (corresponds to underfitting)
 - variance: the amount of variability in the predictions (corresponds to overfitting)
 - Bayes error: the inherent unpredictability of the targets
- Even though this analysis only applies to squared error, we often loosely use "bias" and "variance" as synonyms for "underfitting" and "overfitting".

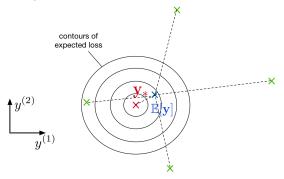
Bias/Variance Decomposition: Another Visualization

- We can visualize this decomposition in output space, where the axes correspond to predictions on the test examples.
- If we have an overly simple model (e.g. KNN with large k), it might have
 - high bias (because it's too simplistic to capture the structure in the data)
 - low variance (because there's enough data to get a stable estimate of the decision boundary)



Bias/Variance Decomposition: Another Visualization

- If you have an overly complex model (e.g. KNN with k=1), it might have
 - low bias (since it learns all the relevant structure)
 - high variance (it fits the quirks of the data you happened to sample)



Bagging

Now, back to bagging!

Bagging: Motivation

- Suppose we could somehow sample m independent training sets from p_{data} .
- We could then compute the prediction y_i based on each one, and take the average $y = \frac{1}{m} \sum_{i=1}^{m} y_i$.
- How does this affect the three terms of the expected loss?
 - ▶ Bayes error: unchanged, since we have no control over it
 - ▶ Bias: unchanged, since the averaged prediction has the same expectation

$$\mathbb{E}[y] = \mathbb{E}\left[\frac{1}{m}\sum_{i=1}^{m}y_i\right] = \mathbb{E}[y_i]$$

▶ Variance: reduced, since we're averaging over independent samples

$$\operatorname{Var}[y] = \operatorname{Var}\left[\frac{1}{m} \sum_{i=1}^{m} y_i\right] = \frac{1}{m^2} \sum_{i=1}^{m} \operatorname{Var}[y_i] = \frac{1}{m} \operatorname{Var}[y_i].$$

Bagging: The Idea

- In practice, running an algorithm separately on independently sampled datasets is very wasteful!
- Solution: bootstrap aggregation, or bagging.
 - ▶ Take a single dataset \mathcal{D} with n examples.
 - Generate m new datasets, each by sampling n training examples from \mathcal{D} , with replacement.
 - ▶ Average the predictions of models trained on each of these datasets.
- The bootstrap is one of the most important ideas in all of statistics!

Bagging: The Idea

- Problem: the datasets are not independent, so we don't get the 1/m variance reduction.
 - Possible to show that if the sampled predictions have variance σ^2 and correlation ρ , then

$$\operatorname{Var}\left(\frac{1}{m}\sum_{i=1}^{m}y_{i}\right)=\frac{1}{m}(1-\rho)\sigma^{2}+\rho\sigma^{2}.$$

- Ironically, it can be advantageous to introduce additional variability into your algorithm, as long as it reduces the correlation between samples.
 - Intuition: you want to invest in a diversified portfolio, not just one stock.
 - Can help to use average over multiple algorithms, or multiple configurations of the same algorithm.

Random Forests

- Random forests = bagged decision trees, with one extra trick to decorrelate the predictions
- When choosing each node of the decision tree, choose a random set of d input features, and only consider splits on those features
- Random forests are probably the best black-box machine learning algorithm — they often work well with no tuning whatsoever.
 - one of the most widely used algorithms in Kaggle competitions

Summary

- Bagging reduces overfitting by averaging predictions.
- Used in most competition winners
 - Even if a single model is great, a small ensemble usually helps.
- Limitations:
 - Does not reduce bias.
 - There is still correlation between classifiers.
- Random forest solution: Add more randomness.