

# Digital Photography II

## color & image processing pipeline



CSC2529

David Lindell

University of Toronto

[cs.toronto.edu/~lindell/teaching/2529](https://cs.toronto.edu/~lindell/teaching/2529)

\*slides adapted from Gordon Wetzstein, Fredo Durand, Ioannis Gkioulekas, Marc Levoy, Todd Zickler, Michael Brown

# Announcements

- HW 2 is out (due next Friday Sep 27)
- TA office hours (HW2) Wed 1-2pm BA 5256

# Outline

- Review
- Color
- Camera processing pipeline

# Review – “Sensors are Buckets”

collect photons like  
a bucket



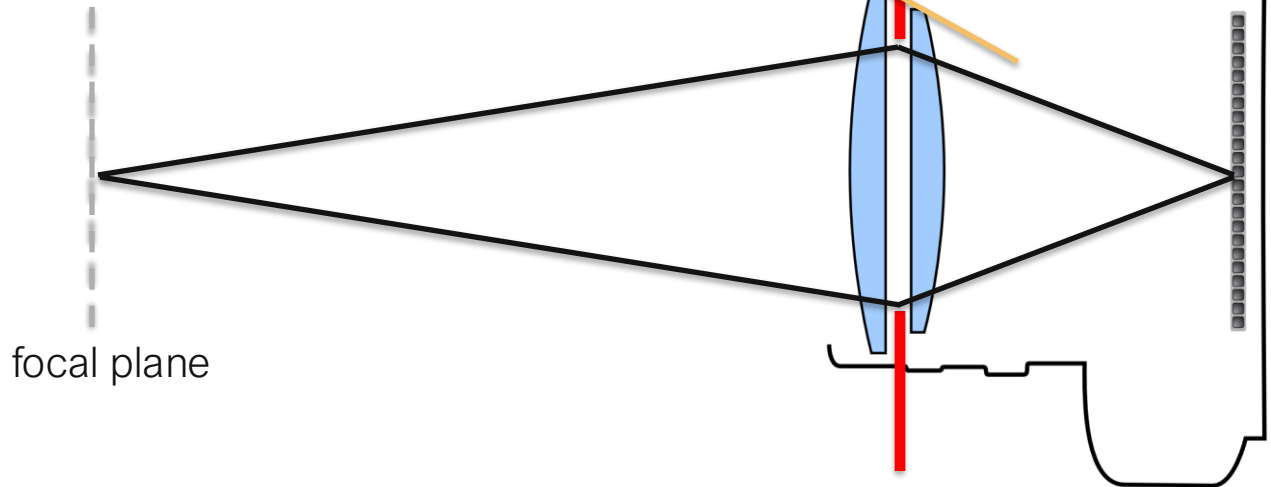
integrate spectrum



integrate incident  
directions

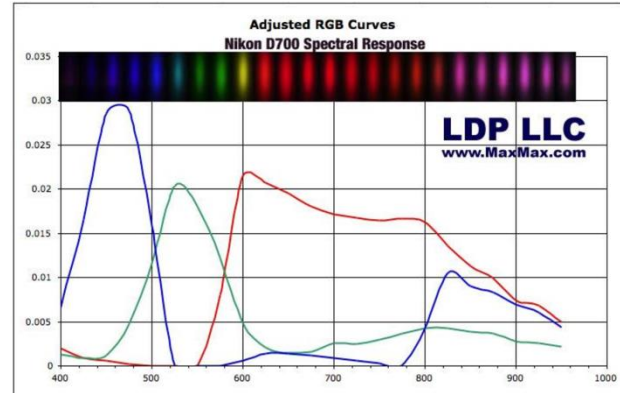
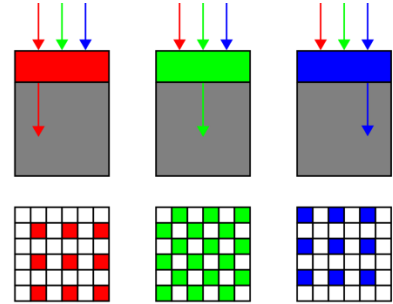
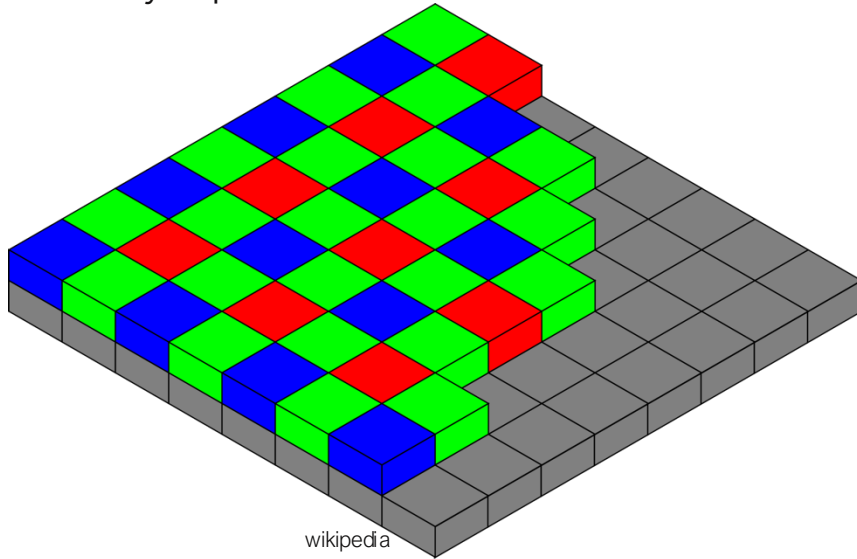


Each pixel sees a point on  
the focal plane from  
different perspectives!



# Review – Color Filter Arrays

Bayer pattern



# Image Formation

- high-dimensional integration over angle, wavelength, time

plenoptic function

$$i(x) \approx \int \int \int \overset{\downarrow}{l}(x, q, l, t) dq dl dt$$

$W_{q,l,t}$

plenoptic function:  
[Adelson 1991]

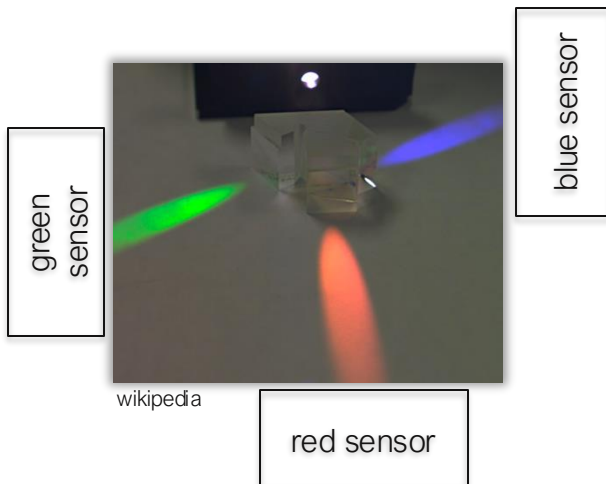
# More Ways to Capture Color

field sequential

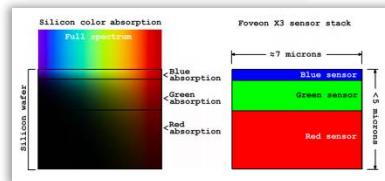
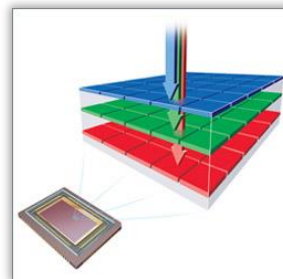


Prokudin-Gorsky

multiple sensors



vertically stacked



Foveon X3



# More Ways to Capture Color



Sergei  
Prokudin-Gorsky



Alim Khahn, Emir of Bukhara, 1911



# More Ways to Capture Color



Gabriel Lippmann

- notable French inventor
- Nobel price for color photography in 1908  
= volume emulsion capturing interference
- today, this process is most similar to volume holography!
- also invented integral imaging (will hear more...)

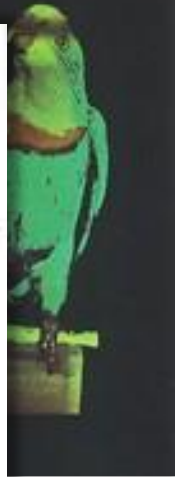
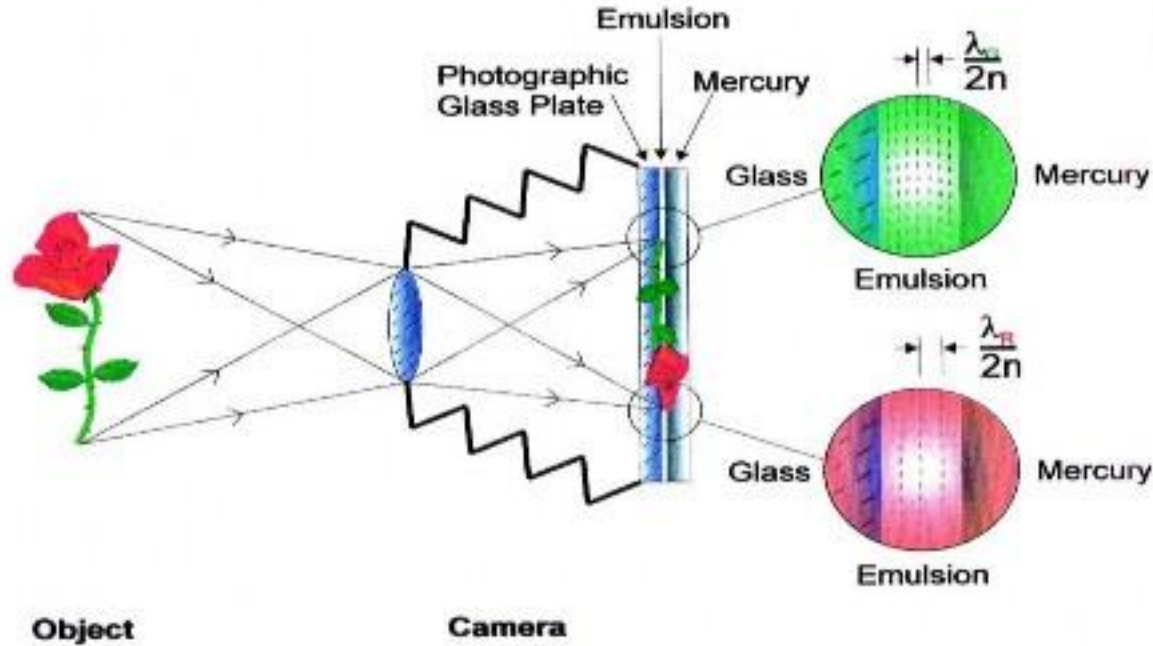


Lippmann's  
stuffed parrot

# More Ways to Capture Color



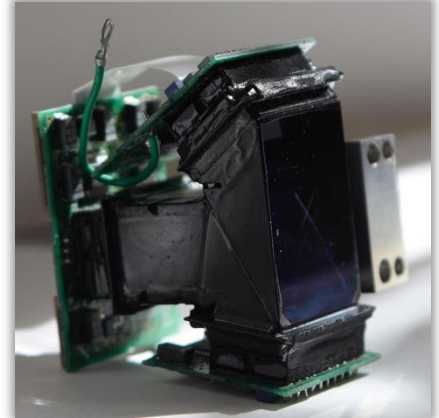
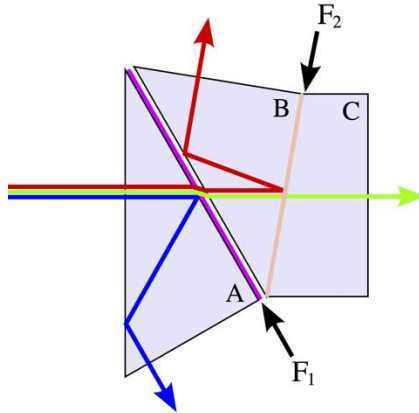
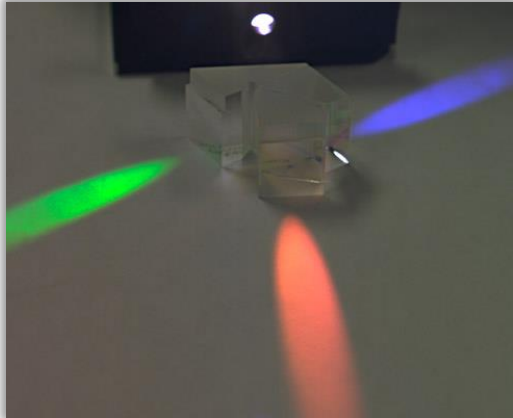
Gabriel Lipman



Lipman's  
color photograph

# Three-CCD Camera

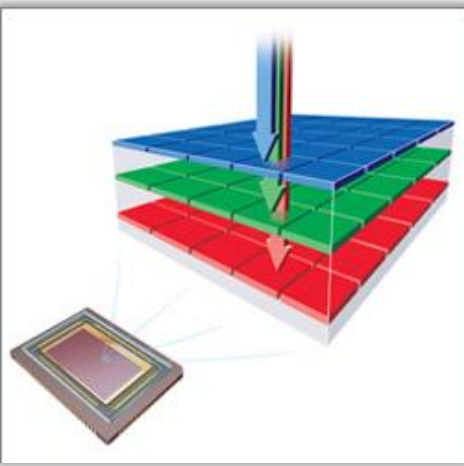
beam splitter prism



Philips / wikipedia



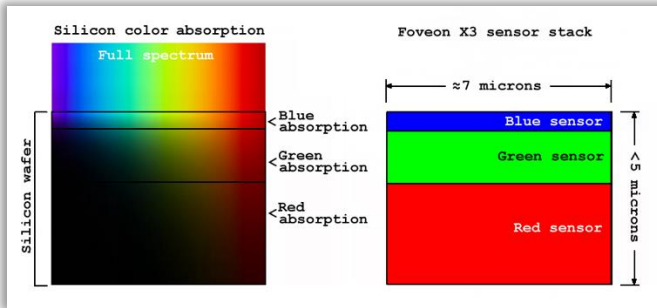
# Stacked Sensor



Foveon X3

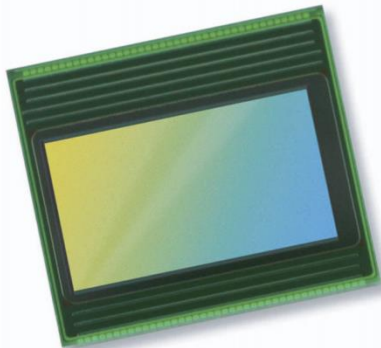


Sigma SD9




# Other Wavelengths

- OmniVision:  
RGB + near IR!



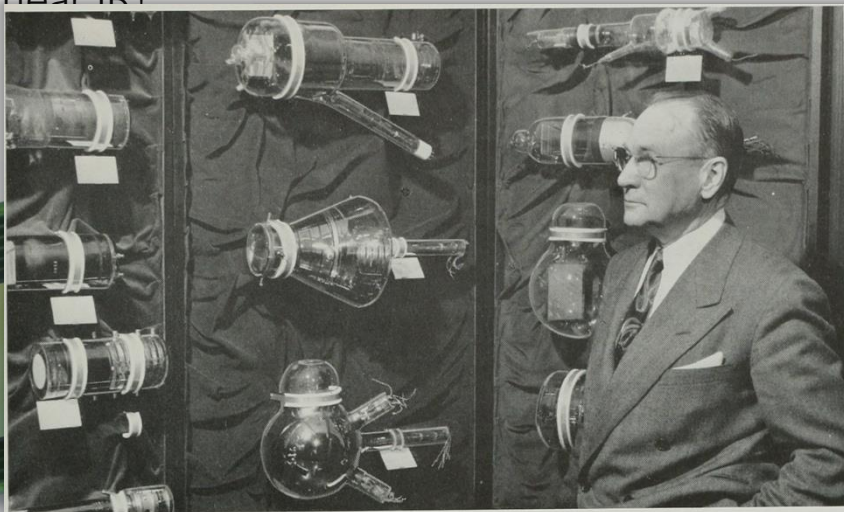
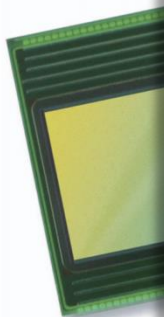
## Product Specifications

<b>Part Number</b>	<b>OV4682-G04A</b>
<b>Resolution</b>	4MP
<b>Chroma</b>	Color
<b>Analog / Digital</b>	Digital
<b>Power Requirement</b>	Active: 163 mA (261 mW) Standby: 1 mA XSHUTDOWN: <10 $\mu$ A
<b>Temperature Range</b>	Operating: -30°C to +85°C junction temperature Stable image: 0°C to +60°C junction temperature
<b>Output Format</b>	10-bit RAW data
<b>Optical Format</b>	1/3"
<b>Frame Rate</b>	Full @ 90 fps 1080p @ 120 fps 672x380: 330 fps 720p @ 180 fps
<b>Pixel Size</b>	2.0 $\mu$ m
<b>Image Area</b>	5440 x 3072 $\mu$ m
<b>Package</b>	COB
<b>Package Dimensions</b>	6600 x 5800 $\mu$ m
<b>Product Brief</b>	 Product Brief

# Other Wavelengths

## Product Specifications

- OmniVision:  
RGB + near IR



**Part Number**

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junction temperature

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junction temperature

10-bit RAW data

1/3"

Full @ 90 fps

1080p @ 120 fps

672x380: 330 fps

720p @ 180 fps

2.0  $\mu$ m


5440 x 3072  $\mu$ m

COB

6600 x 5800  $\mu$ m

**Package Dimensions**

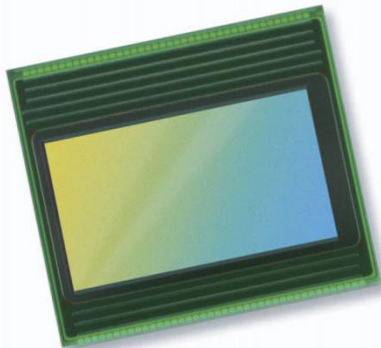
**Product Brief**

 Product Brief




# Other Wavelengths

- OmniVision:  
RGB + near IR!



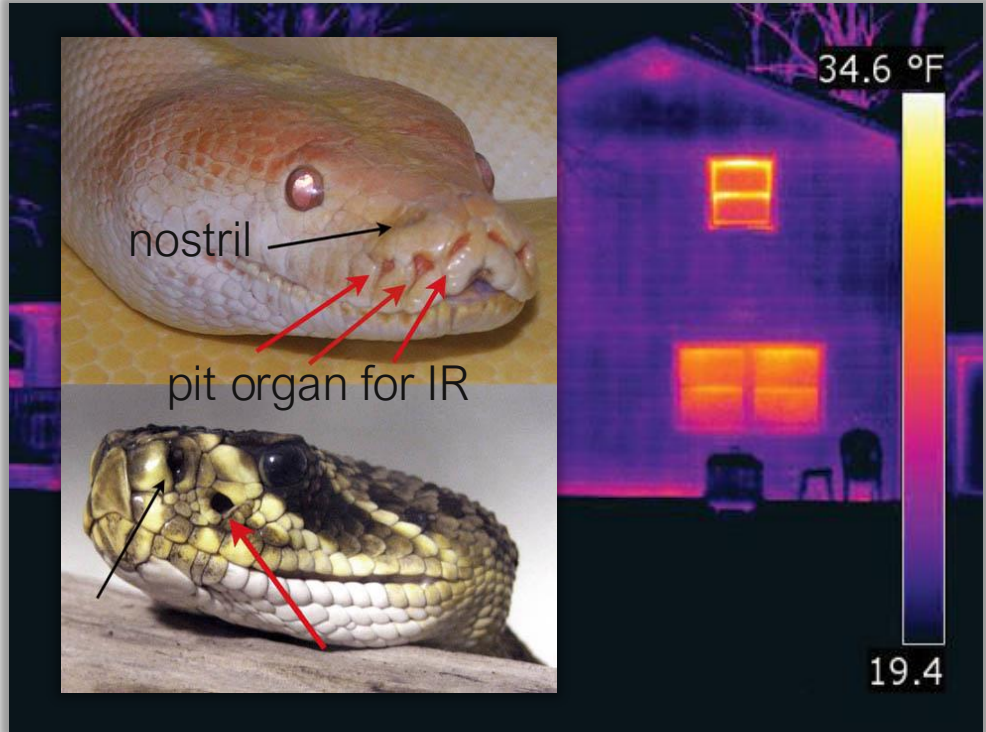
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# Other Wavelengths

FLIR Systems

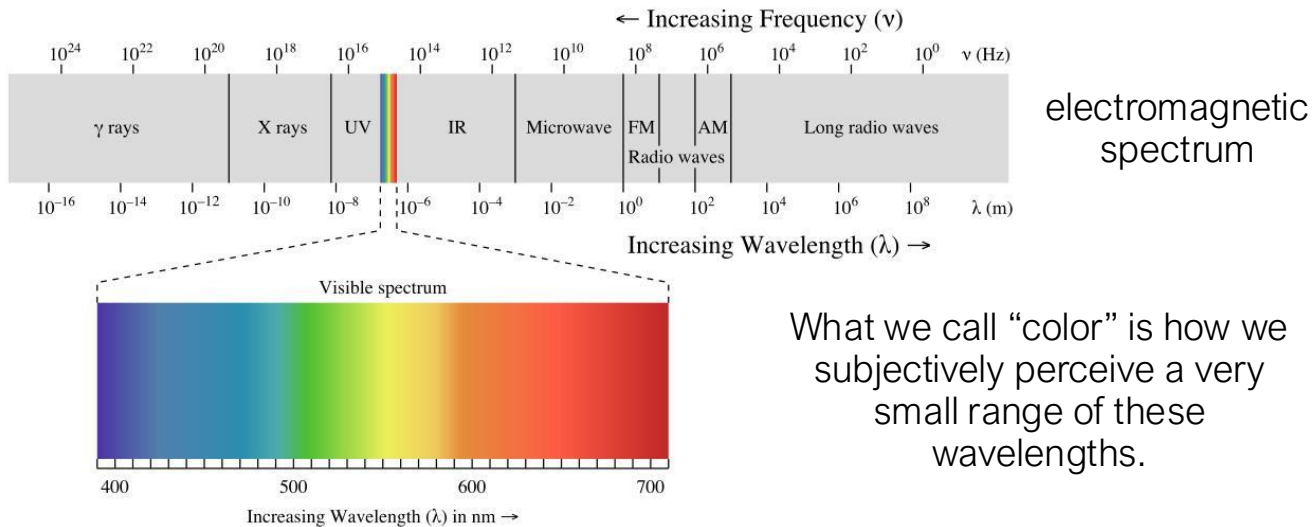
- thermal IR
- often use Germanium optics (transparent IR)



- sensors don't use silicon: indium, mercury, lead, etc.

# Color is an artifact of human perception

- “Color” is not an objective physical property of light (electromagnetic radiation).
- Instead, light is characterized by its wavelength.



# Spectral Sensitivity Function (SSF)

- Any light sensor (digital or not) has different sensitivity to different wavelengths.
- This is described by the sensor's spectral sensitivity function  $f(\lambda)$
- When measuring light of some SPD  $\Phi(\lambda)$  the sensor produces a scalar response:

$$\text{sensor response} \longrightarrow R = \int_{\lambda} \overset{\substack{\text{light SPD} \\ \downarrow}}{\Phi(\lambda)} \overset{\substack{\text{sensor SSF} \\ \downarrow}}{f(\lambda)} d\lambda$$

Weighted combination of light's SPD: light contributes more at wavelengths where the sensor has higher sensitivity.

# Spectral Sensitivity Function of Human Eye

- The human eye is a collection of light sensors called cone cells.
- There are three types of cells with different spectral sensitivity functions.
- Human color perception is three-dimensional (tristimulus color).

“short”

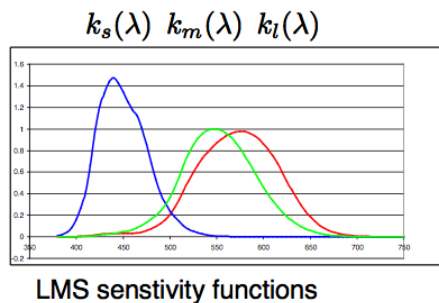
$$S = \int_{\lambda} \Phi(\lambda) S(\lambda) d\lambda$$

“medium”

$$M = \int_{\lambda} \Phi(\lambda) M(\lambda) d\lambda$$

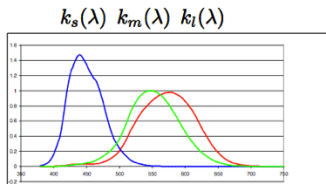
“long”

$$L = \int_{\lambda} \Phi(\lambda) L(\lambda) d\lambda$$

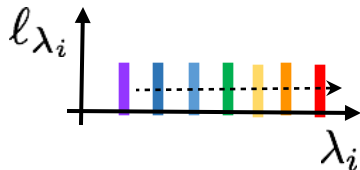
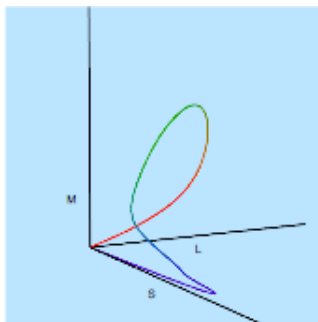


# The retinal color space

$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$



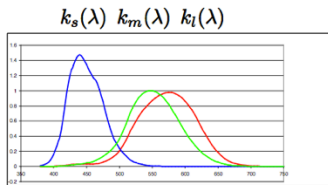
LMS sensitivity functions



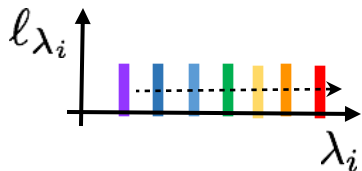
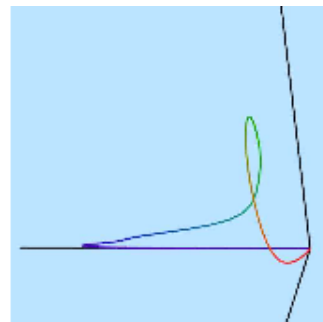
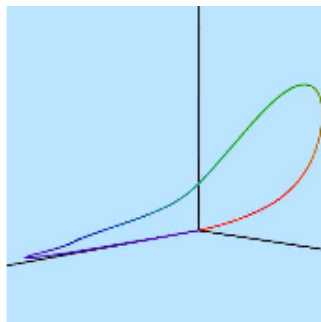
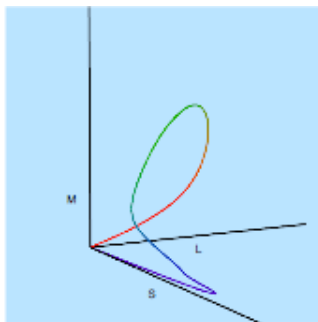
“pure beam” (laser)

# The retinal color space

$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$



LMS sensitivity functions



“pure beam” (laser)

- “lasso curve”
- contained in positive octant
- parameterized by wavelength
- starts and ends at origin
- never comes close to M axis



why?



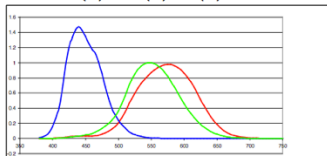
why?

# The retinal color space

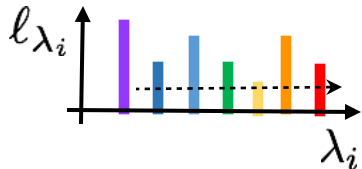
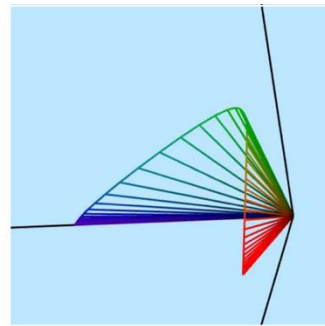
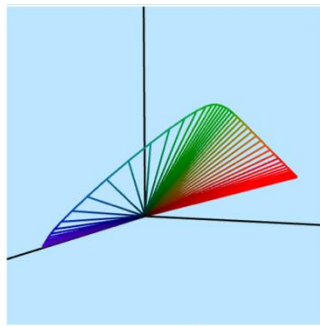
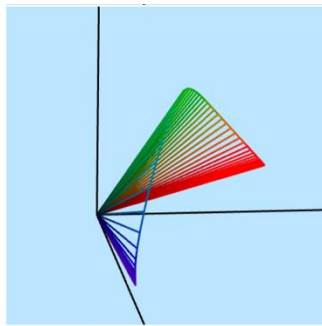
$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$



$k_s(\lambda)$   $k_m(\lambda)$   $k_l(\lambda)$



LMS sensitivity functions



“pure beam” (laser)

if we also consider variations in the strength of the laser this “lasso” turns into (convex!) radial cone with a “horse-shoe shaped” radial cross-section

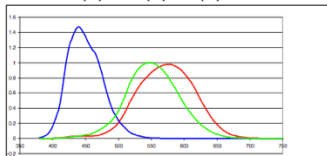


# The retinal color space

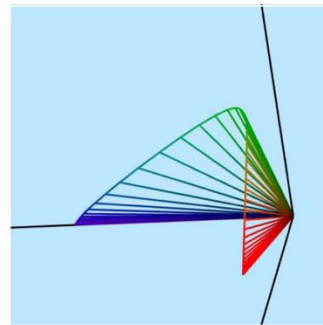
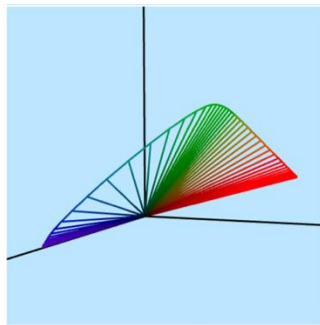
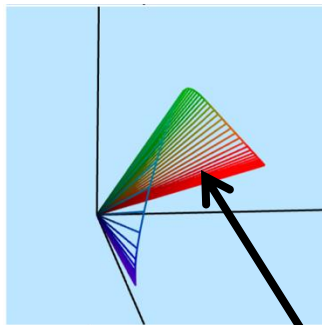
$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$



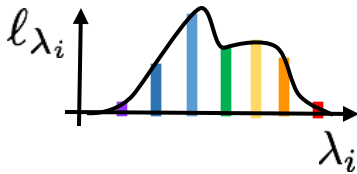
$k_s(\lambda)$   $k_m(\lambda)$   $k_l(\lambda)$



LMS sensitivity functions



colors of mixed beams are at the interior of the convex cone with boundary the surface produced by monochromatic lights

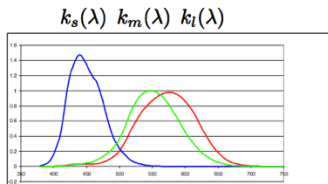


"mixed beam"

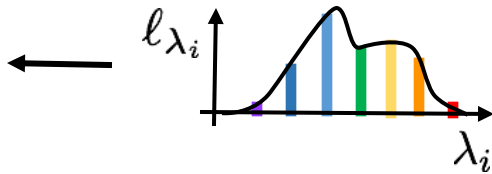
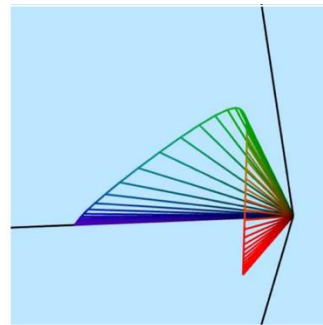
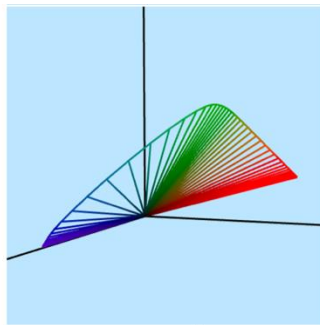
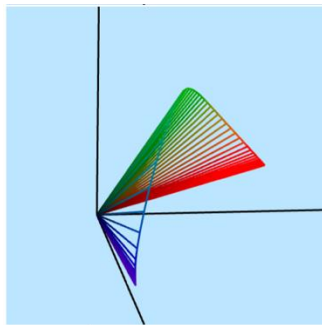
= convex combination of pure colors

# The retinal color space

$$\mathbf{c}(\ell_{\lambda_i}) = (c_s, c_m, c_l)$$



LMS sensitivity functions

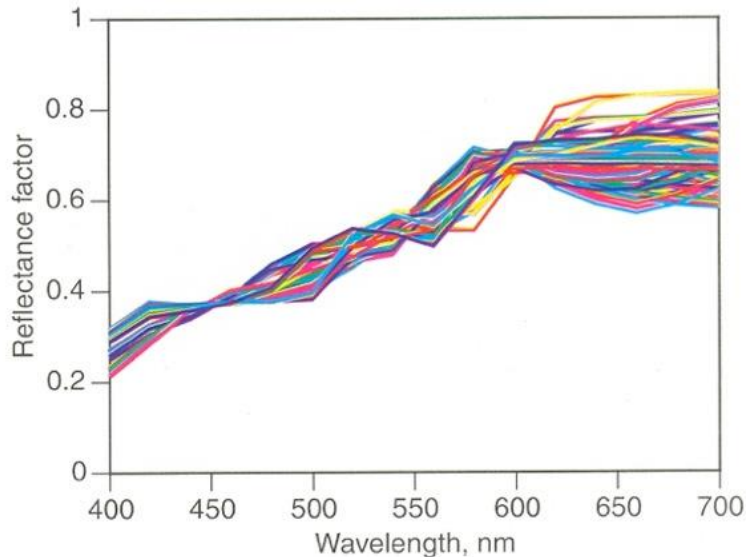


“mixed beam”

= convex combination of pure colors

- distinct mixed beams can produce the same retinal color
- these beams are called metamers

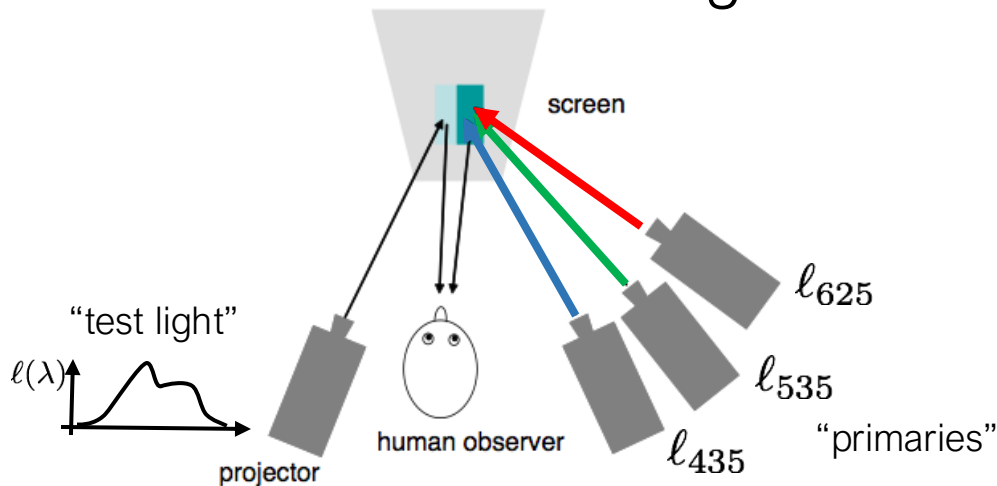
# There is an infinity of metamers



Ensemble of spectral reflectance curves corresponding to three chromatic-pigment recipes all matching a tan material when viewed by an average observer under daylight illumination. [Based on Berns (1988b).]

# Color matching

# CIE color matching

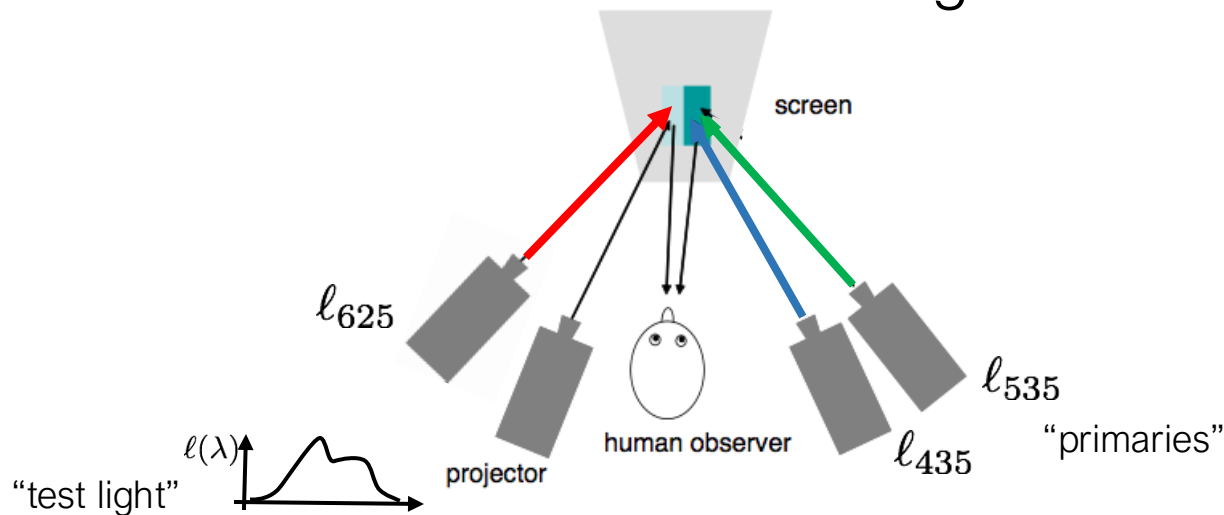


Adjust the strengths of the primaries until they re-produce the test color. Then:

$$\mathbf{c}(\ell(\lambda)) = \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535}) + \gamma \mathbf{c}(\ell_{625})$$

↖ equality symbol means "has the same retinal color as" or "is metameric to"

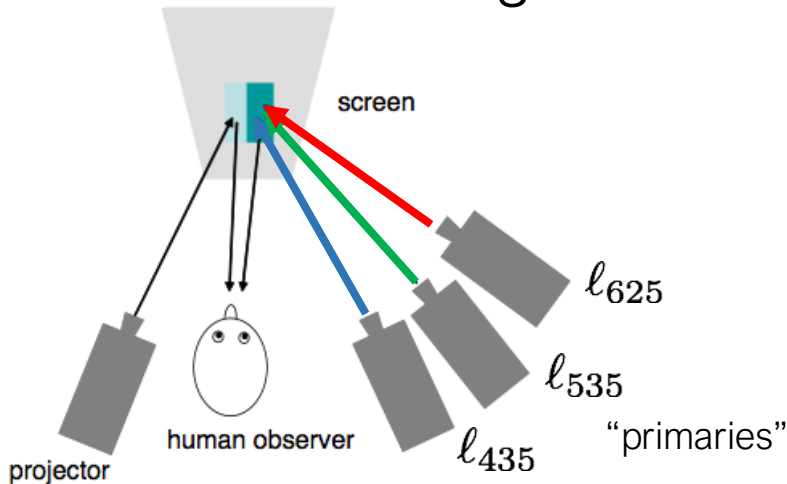
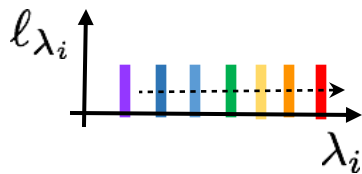
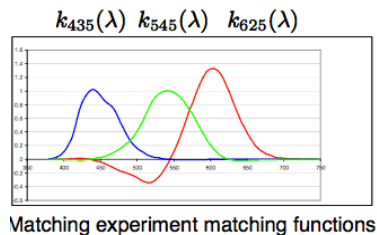
# CIE color matching



To match some test colors, you need to add some primary beam on the left (same as "subtracting light" from the right)

$$\begin{aligned} \mathbf{c}(\ell(\lambda)) + \gamma \mathbf{c}(\ell_{625}) &= \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535}) \\ \longrightarrow \mathbf{c}(\ell(\lambda)) &= \alpha \mathbf{c}(\ell_{435}) + \beta \mathbf{c}(\ell_{535}) - \gamma \mathbf{c}(\ell_{625}) \end{aligned}$$

# CIE color matching

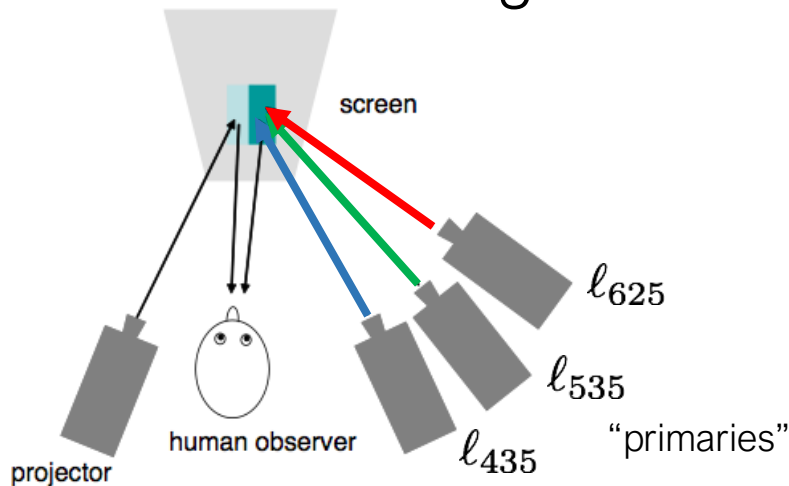
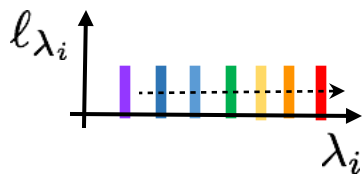
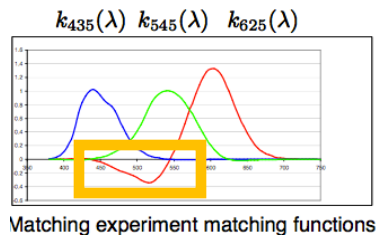


Repeat this matching experiments for pure test beams at wavelengths  $\lambda_i$  and keep track of the coefficients (negative or positive) required to reproduce each pure test beam.

$$\mathbf{c}(\lambda_i) = k_{435}(\lambda)\mathbf{c}(l_{435}) + k_{535}(\lambda)\mathbf{c}(l_{535}) + k_{625}(\lambda)\mathbf{c}(l_{625})$$

note the negative values

# CIE color matching

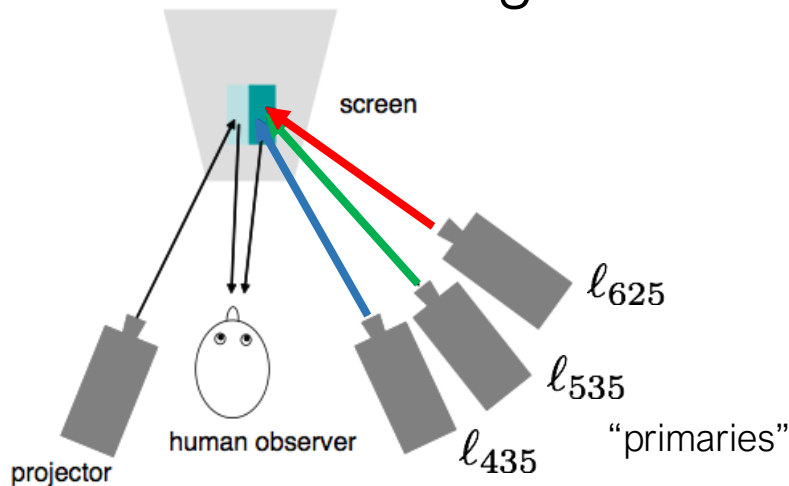
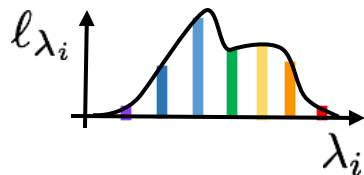
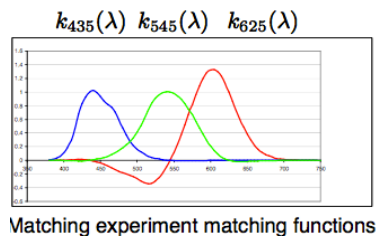


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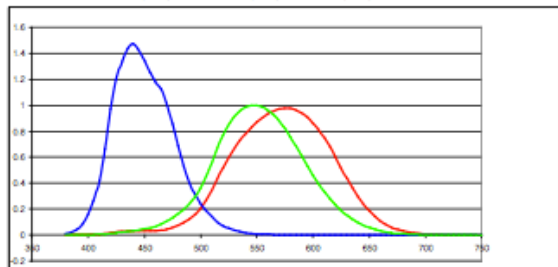
# CIE color matching



What about “mixed beams”?

# Two views of retinal color

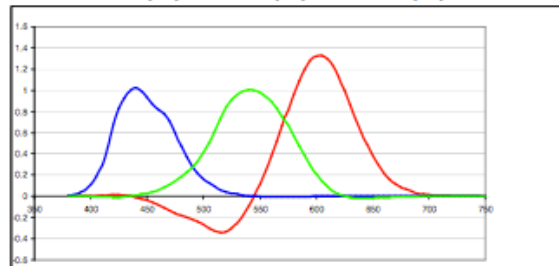
$k_s(\lambda)$   $k_m(\lambda)$   $k_l(\lambda)$



**LMS sensitivity functions**

Analytic: Retinal color is produced by analyzing spectral power distributions using the color sensitivity functions.

$k_{435}(\lambda)$   $k_{545}(\lambda)$   $k_{625}(\lambda)$

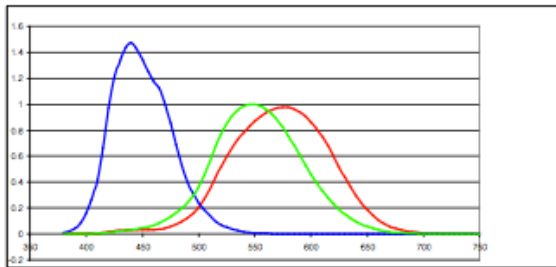


**Matching experiment matching functions**

Synthetic: Retinal color is produced by synthesizing color primaries using the color matching functions.

# Two views of retinal color

$k_s(\lambda)$   $k_m(\lambda)$   $k_l(\lambda)$

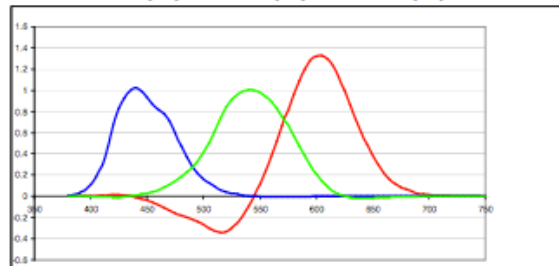


**LMS sensitivity functions**

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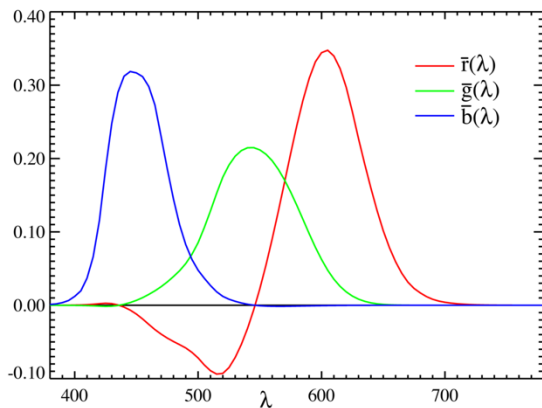
The two views are equivalent: Color matching functions are also color sensitivity functions. For each set of color sensitivity functions, there are corresponding color primaries.

$k_{435}(\lambda)$   $k_{545}(\lambda)$   $k_{625}(\lambda)$



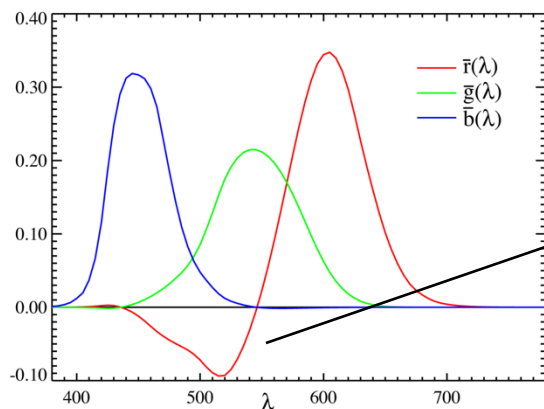
**Matching experiment matching functions**

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## CIE RGB colorspace

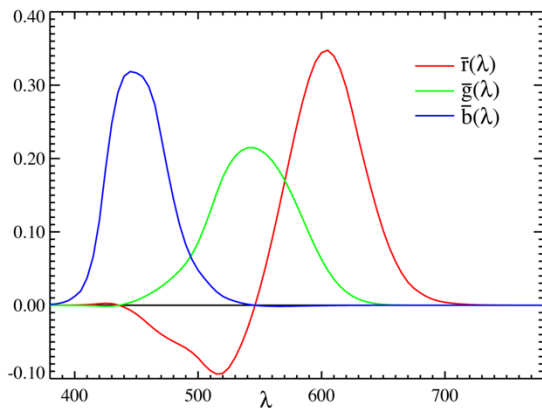
Created by the International Commission on Illumination in 1931 based on color matching experiments from 12 people!



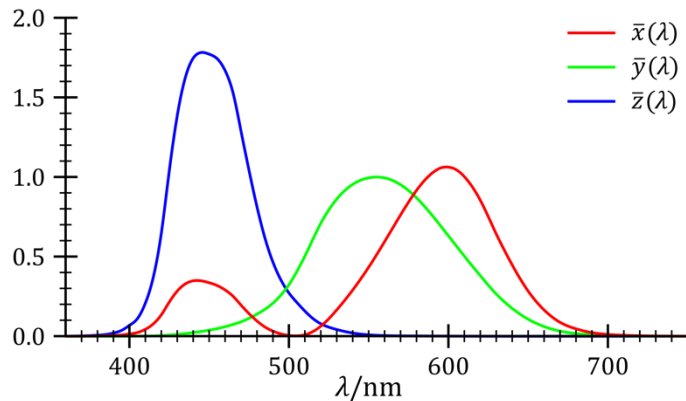
Negative values are not physical  
since we cannot subtract light

CIE RGB colorspace

Created by the International Commission on  
Illumination in 1931 based on color matching  
experiments from 12 people!



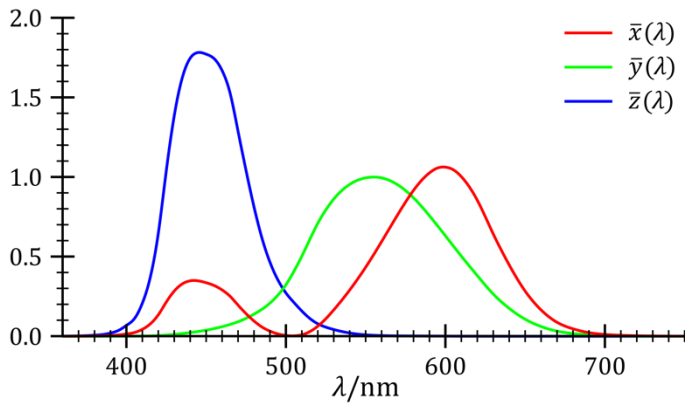
CIE RGB colorspace



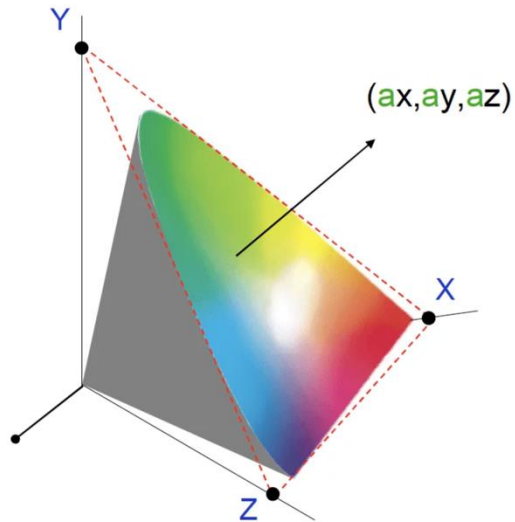
CIE XYZ colorspace

Created by the International Commission on Illumination in 1931 based on color matching experiments from 12 people!

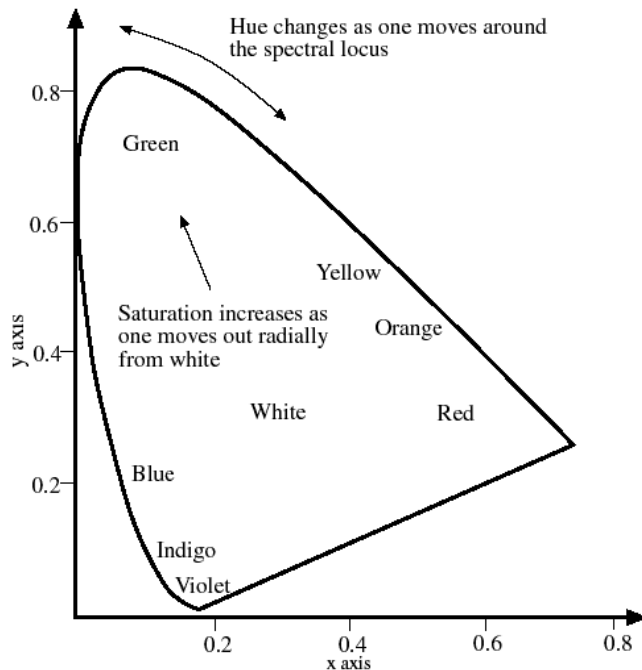
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$



CIE XYZ colorspace



# CIE xy (chromaticity)



$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$(X, Y, Z) \longleftrightarrow (\underline{x, y}, Y)$$

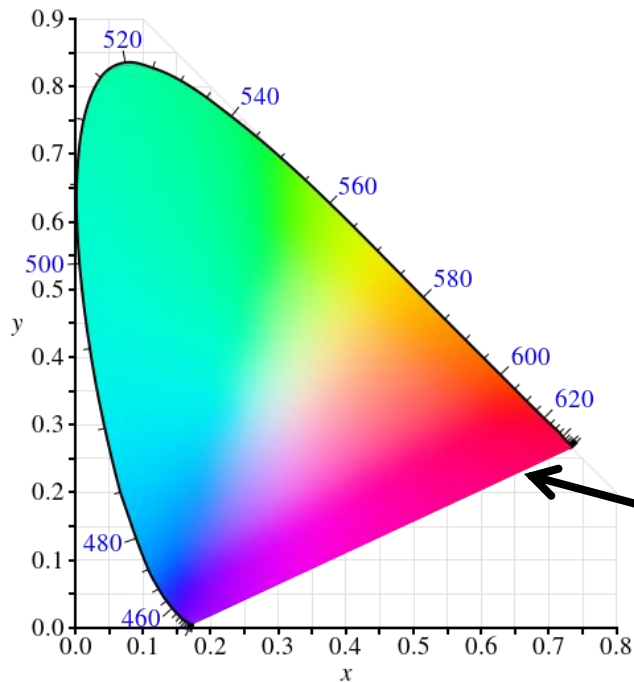
chromaticity ↑

luminance/brightness

Perspective projection of 3D retinal color space to two dimensions.



# CIE xy (chromaticity)



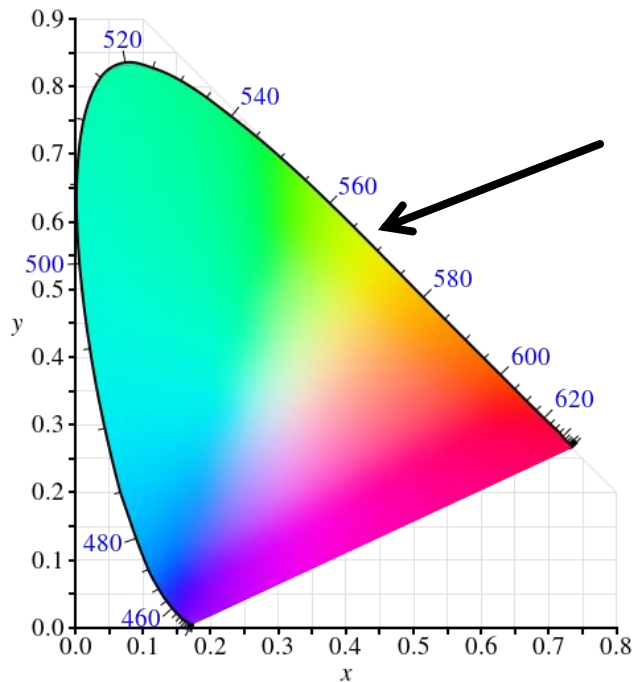
$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$(X, Y, Z) \longleftrightarrow (x, y, Y)$$

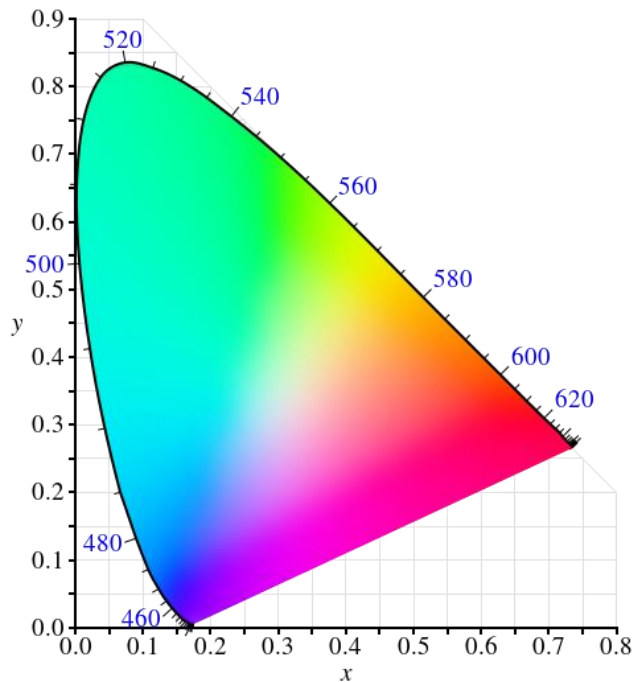
Note: These colors can be extremely misleading depending on the file origin and the display you are using

# CIE xy (chromaticity)



What does the boundary of the chromaticity diagram correspond to?

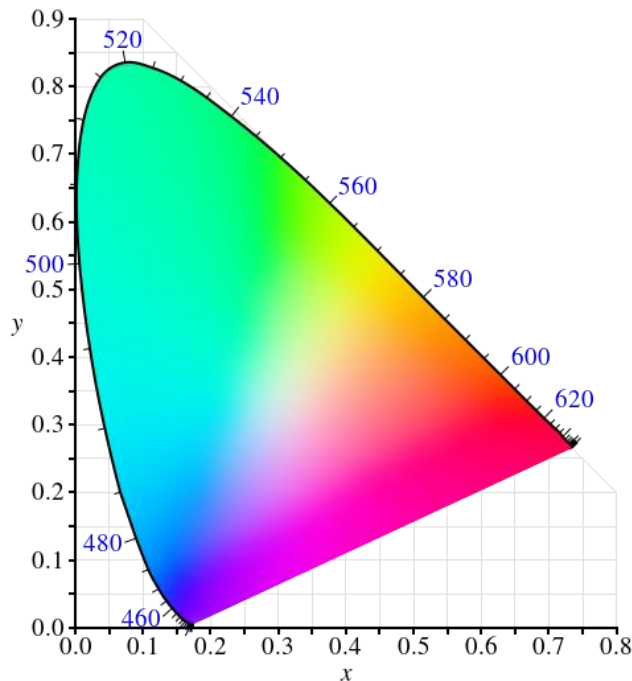
# Color gamuts



We can compare color spaces by looking at what parts of the chromaticity space they can reproduce with their primaries.

But why would a color space not be able to reproduce all of the chromaticity space?

# Color gamuts

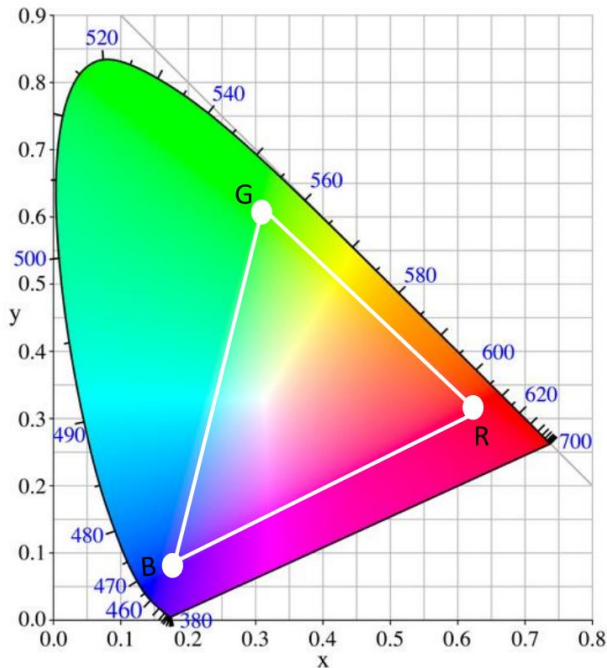


We can compare color spaces by looking at what parts of the chromaticity space they can reproduce with their primaries.

But why would a color space not be able to reproduce all of the chromaticity space?

- Many colors require negative weights to be reproduced, which are not realizable.

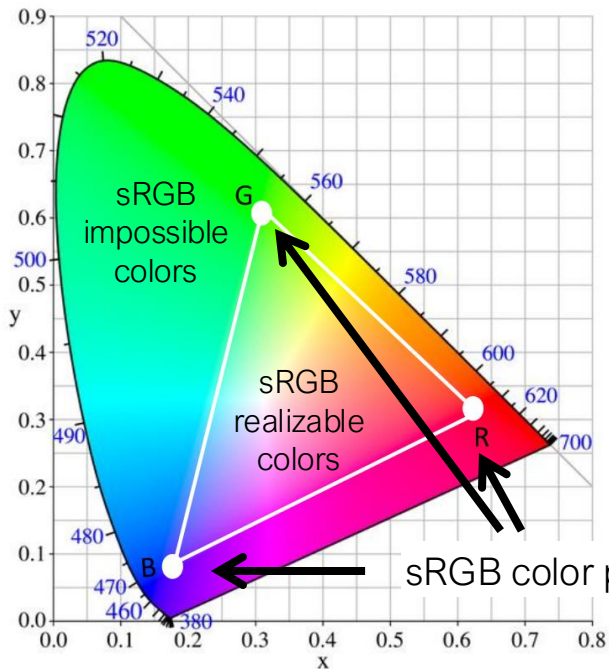
# Color gamuts



sRGB color gamut:

- What are the three triangle corners?
- What is the interior of the triangle?
- What is the exterior of the triangle?

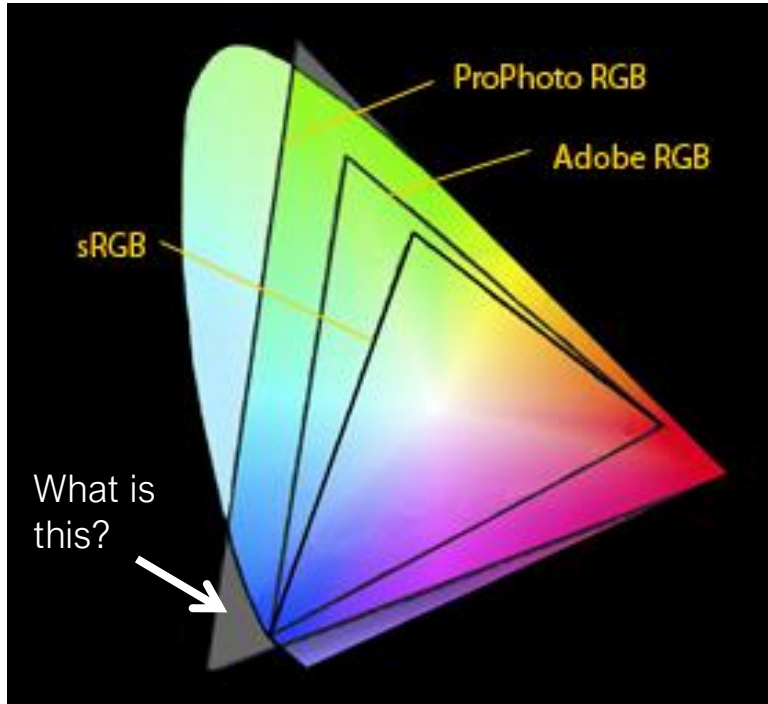
# Color gamuts



sRGB color gamut

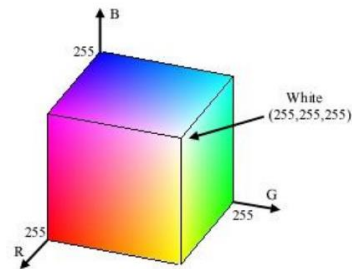
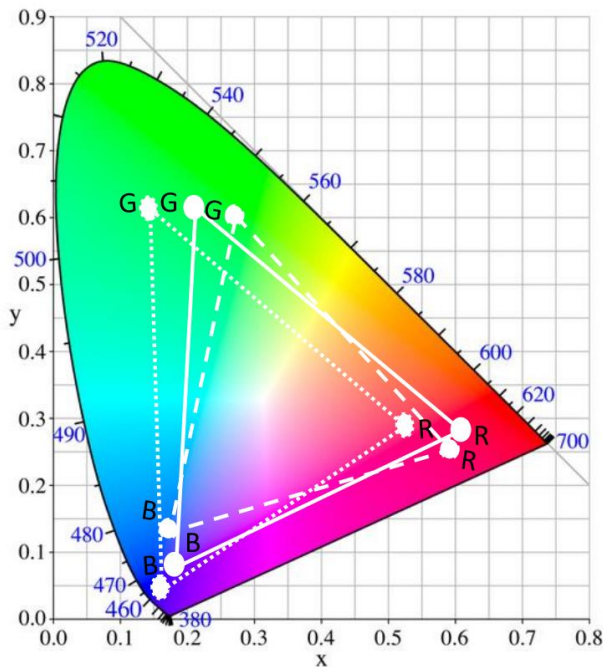
sRGB color primaries

# Color gamuts



Gamuts of various common industrial RGB spaces

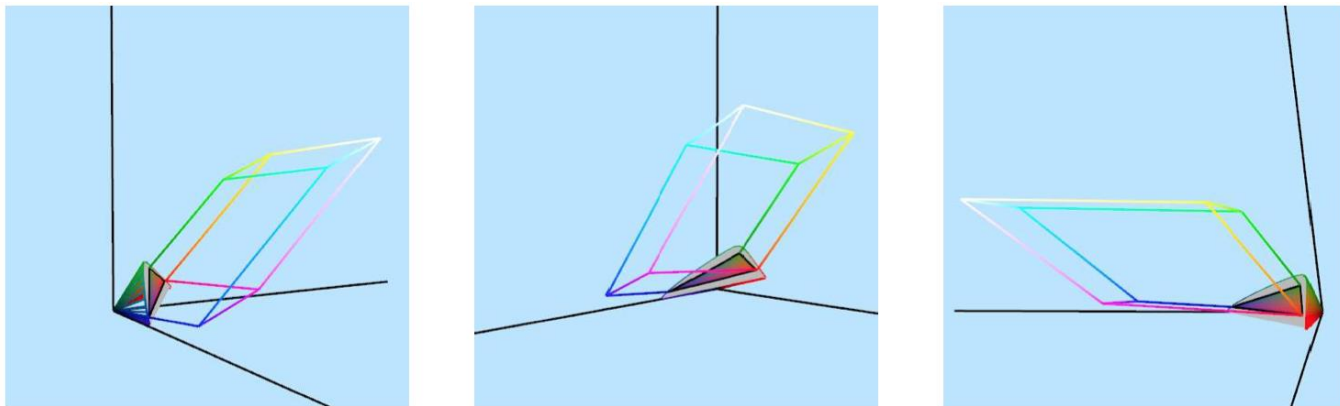
# The problem with RGBs visualized in chromaticity space



RGB values have no meaning if the primaries between devices are not the same!



# Chromaticity diagrams can be misleading



Different gamuts may compare very differently when seen in full 3D retinal color space.

# Some take-home messages about color spaces

Analytic: Retinal color is three numbers formed by taking the dot product of a power spectral distribution with three color matching/sensitivity functions.

Synthetic: Retinal color is three numbers formed by assigning weights to three color primaries to match the perception of a power spectral distribution.

# Some take-home messages about color spaces

Fundamental problem: Analysis spectrum (camera, eyes) cannot be the same as synthesis one (display) - impossible to encode all possible colors without something becoming negative

- CIE XYZ only needs positive coordinates, but need primaries with negative light.
- sRGB must use physical (non-negative) primaries, but needs negative coordinates for some colors.

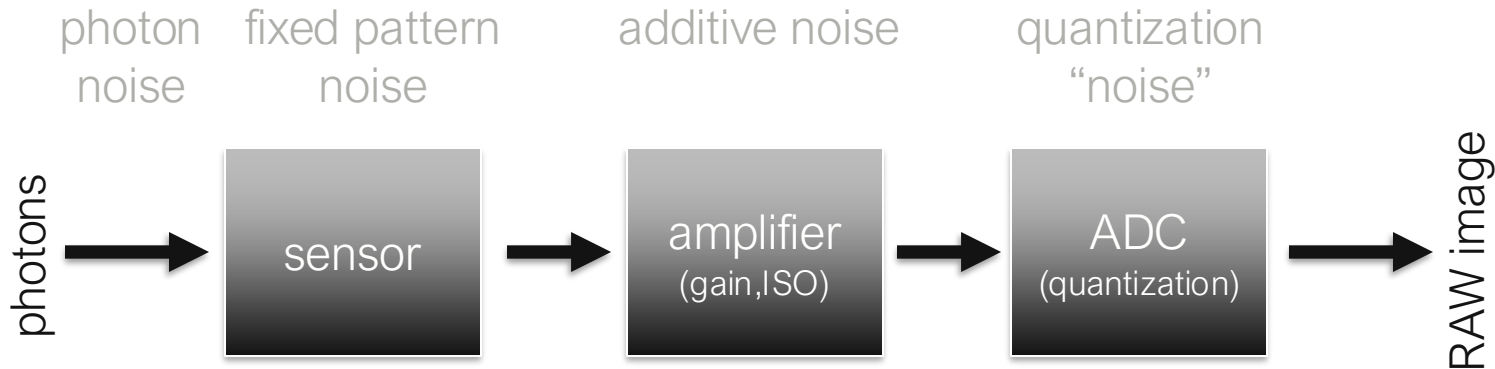
# Some take-home messages about color spaces

Problem with current practice: Many different RGB color spaces used by different devices, without clarity of what exactly space a set of RGB color values are in.

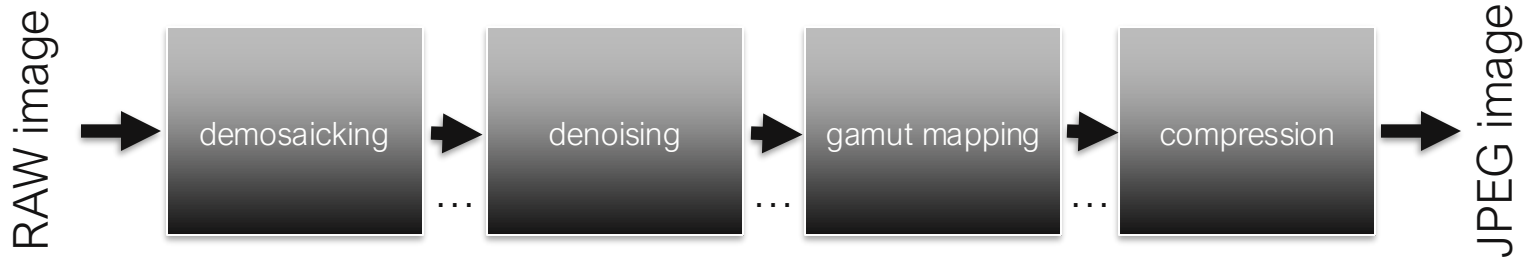
- Huge problem for color reproduction from one device to another.
- there are standards (like sRGB), but consumer displays are not calibrated—so you cannot really conclude that images are color accurate

camera processing pipeline

# Review: Photons to RAW Image



# Image Processing Pipeline



also:

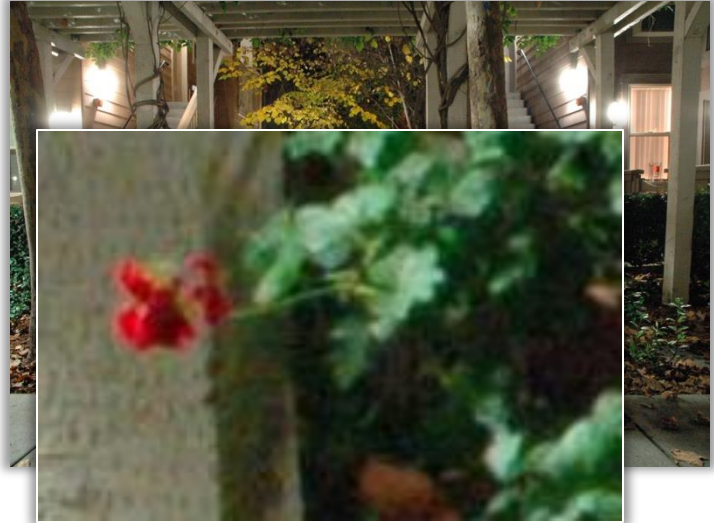
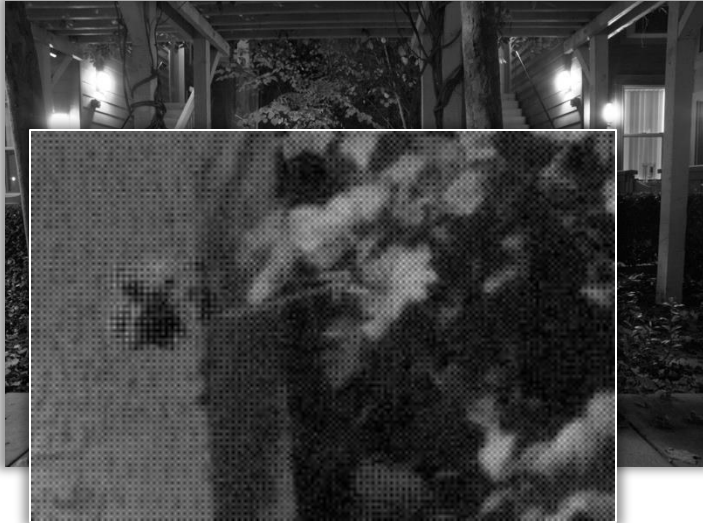
- dead pixel removal
- dark frame subtraction (fixed pattern / thermal noise removal)
- lens blur / vignetting / distortion correction
- sharpening / edge enhancement

# Image Processing Pipeline

RAW image  
(dcraw -D)



JPEG image





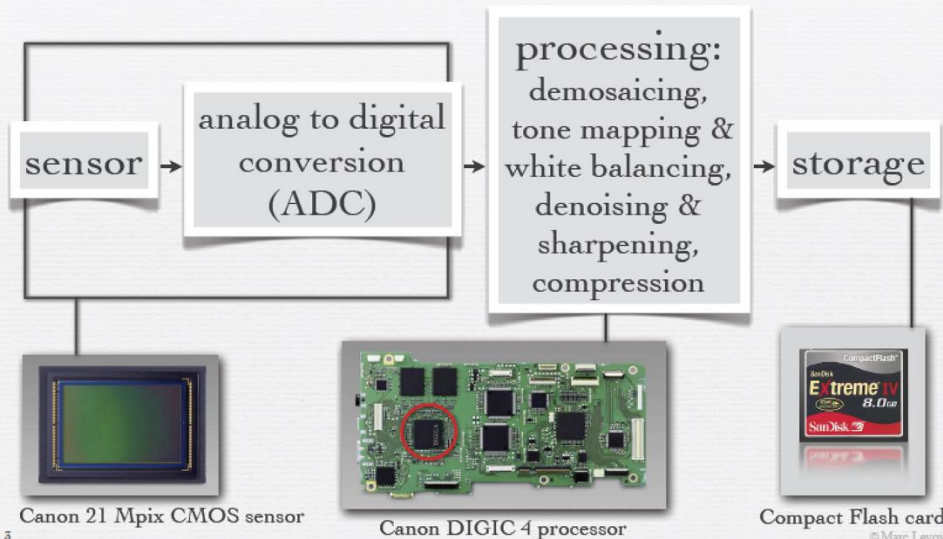
# Image Processing Pipeline

- demosaicking
- denoising
- digital autoexposure
- white balancing
- linear 10/12 bit to 8 bit gamma
- compression



# Image Processing Pipeline

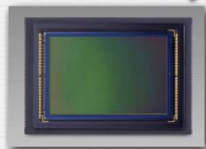
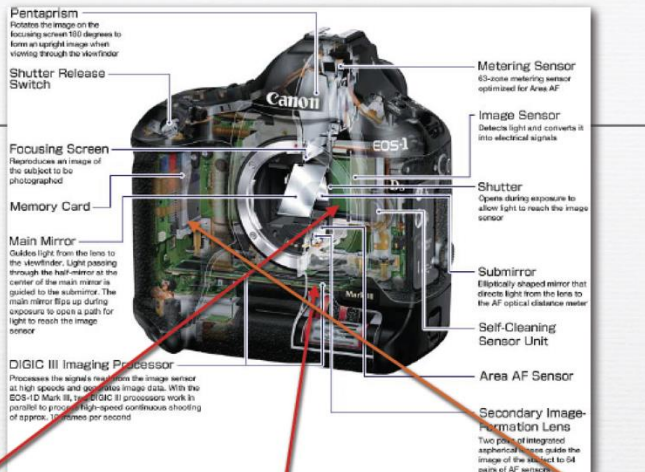
## Example pipeline



# Image Processing Pipeline

## Example

(parts are from a Canon 5DII, but cutaway view is of 1DIII)



Canon 21 Mpix CMOS sensor



Canon DIGIC 4 processor



Compact Flash card

© Marc Levy

filename - night nikon.JPG

Make - NIKON CORPORATION

Model - NIKON D70S

Orientation - Top left

XResolution - 300

YResolution - 300

ResolutionUnit - Inch

Software - Ver.1.00

DateTime - 2005:09:01 12:16:43

YCbCrPositioning - Co-Sited

ExifOffset - 216

ExposureTime - 10 seconds

FNumber - 13.00

ExposureProgram - Manual control

ExifVersion - 0221

DateTimeOriginal - 2005:09:01 12:16:43

DateTimeDigitized - 2005:09:01 12:16:43

ComponentsConfiguration - YCbCr

CompressedBitsPerPixel - 1 (bits/pixel)

ExposureBiasValue - 0.50

MaxApertureValue - F 3.48

MeteringMode - Center weighted average

LightSource - Auto

Flash - Not fired

FocalLength - 18.00 mm

UserComment - (c) Gordon Wetzstein

SubsecTime - 00

SubsecTimeOriginal - 00

SubsecTimeDigitized - 00

FlashPixVersion - 0100

ColorSpace - sRGB

ExifImageWidth - 3008

ExifImageHeight - 2000

InteroperabilityOffset - 29230

SensingMethod - One-chip color area sensor

FileSource - Other

SceneType - Other

CustomRendered - Custom process

ExposureMode - Manual

White Balance - Auto

DigitalZoomRatio - 1 x

FocalLengthIn35mmFilm - 27 mm

SceneCaptureType - Portrait

GainControl - Low gain up

Contrast - Normal

Saturation - Normal

Sharpness - Soft

SubjectDistanceRange - Unknown

Maker Note (Vendor): -

Data version - 0210 (808595760)

ISO Setting - 1600

Image Quality - BASIC

White Balance - AUTO

Image Sharpening - MED.L

Focus Mode - MANUAL

Flash Setting - NORMAL

Flash Mode -

White Balance Adjustment - 0

Exposure Adjustment - 1.7

Thumbnail IFD offset - 1430

Flash Compensation - 67072

ISO 2 - 1600

Tone Compensation - AUTO

Lens type - AF-D G

Lens - 618

Flash Used - Not fired

AF Focus Position - Center

Bracketing - 131072

Color Mode - MODE1a

Light Type - NORMAL

Hue Adjustment - 0

Noise Reduction - FPNR

Total pictures - 22346

Optimization - PORTRAIT

Thumbnail: -

Compression - 6 (JPG)

XResolution - 300

YResolution - 300

ResolutionUnit - Inch

JpegIFOffset - 29368

JpegIFByteCount - 8393

YCbCrPositioning - Co-Sited



# Exif Meta Data

Filename - night nikon.JPG

Make - NIKON CORPORATION

Model - NIKON D70S

Orientation - Top left

XResolution - 300

YResolution - 300

ResolutionUnit - Inch

Software - Ver.1.00

DateTime - 2005:09:01 12:16:43

YCbCrPositioning - Co-Sited

ExifOffset - 216

ExposureTime - 10 seconds

FNumber - 13.00

ExposureProgram - Manual control

ExifVersion - 0221

DateTimeOriginal - 2005:09:01 12:16:43

DateTimeDigitized - 2005:09:01 12:16:43

ComponentsConfiguration - YCbCr

CompressedBitsPerPixel - 1 (bits/pixel)

ExposureBiasValue - 0.50

MaxApertureValue - F 3.48

MeteringMode - Center weighted average

LightSource - Auto

Flash - Not fired

FocalLength - 18.00 mm

UserComment - (c) Gordon Wetzstein

SubsecTime - 00

SubsecTimeOriginal - 00

SubsecTimeDigitized - 00

FlashPixVersion - 0100

ColorSpace - sRGB

Maker Note (Vendor): -

Data version - 0210 (808595760)

ISO Setting - 1600

Image Quality - BASIC

White Balance - AUTO

Image Sharpening - MED.L

Focus Mode - MANUAL

Flash Setting - NORMAL

Flash Mode -

White Balance Adjustment - 0

Exposure Adjustment - 1.7

Thumbnail IFD offset - 1430

Flash Compensation - 67072

ISO 2 - 1600

Tone Compensation - AUTO

Lens type - AF-D G

Lens - 618

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Bracketing - 131072

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Total pictures - 22346

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Compression - 6 (JPG)

XResolution - 300

YResolution - 300

ResolutionUnit - Inch

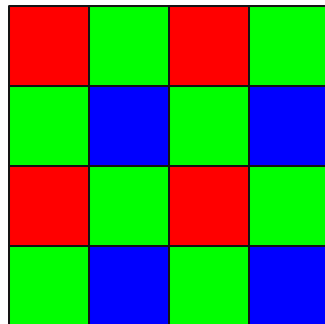
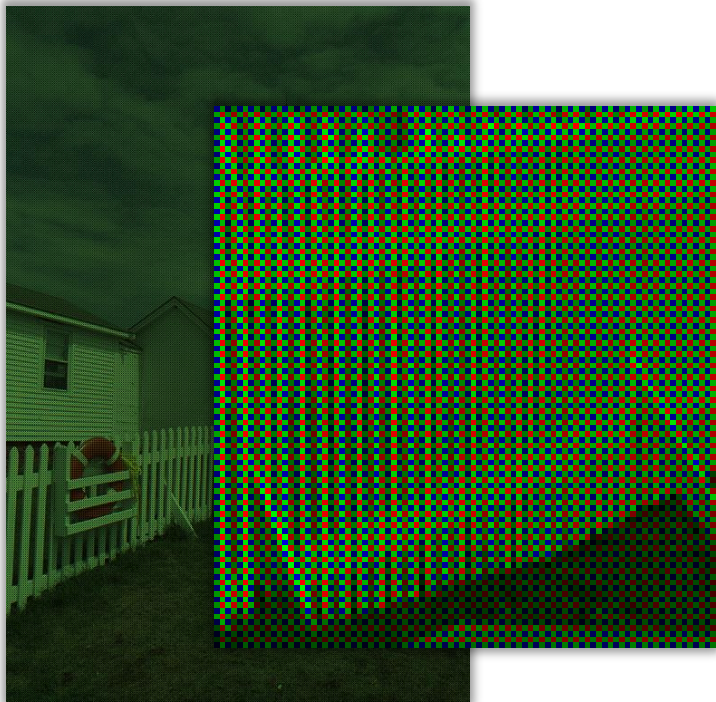
JpegIFOffset - 29368

JpegIFByteCount - 8393

YCbCrPositioning - Co-Sited

# Demosaicking (CFA Interpolation)

RAW

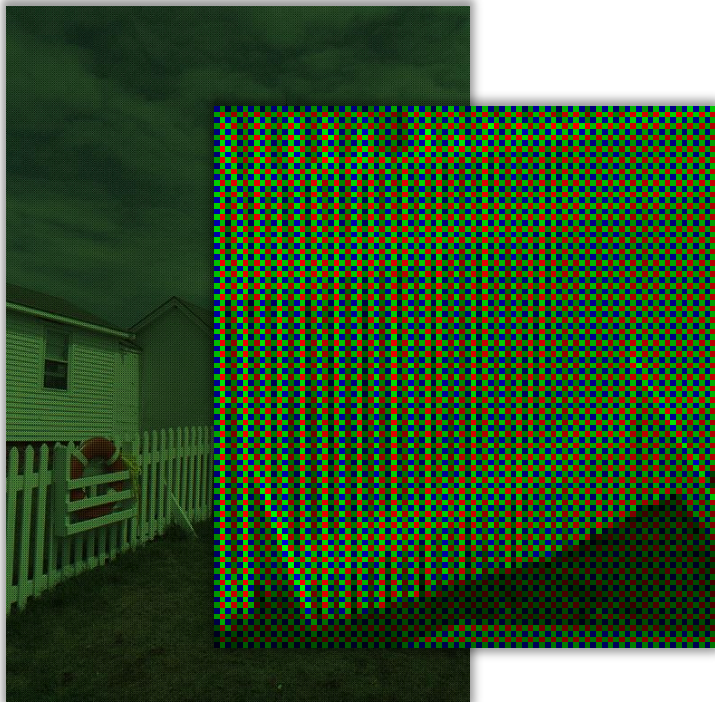


Bayer CFA

# Demosaicking (CFA Interpolation)

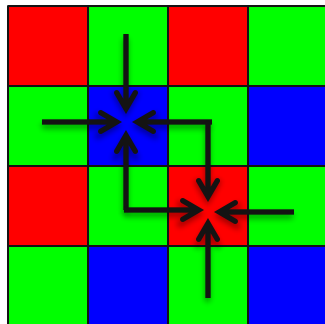
RAW

linear interpolation green channel



$$\hat{g}_{lin}(x, y) = \frac{1}{4} \hat{a}_{(m,n)} g(x + m, y + n)$$

$$(m, n) = \{(0, -1), (0, 1), (-1, 0), (1, 0)\}$$



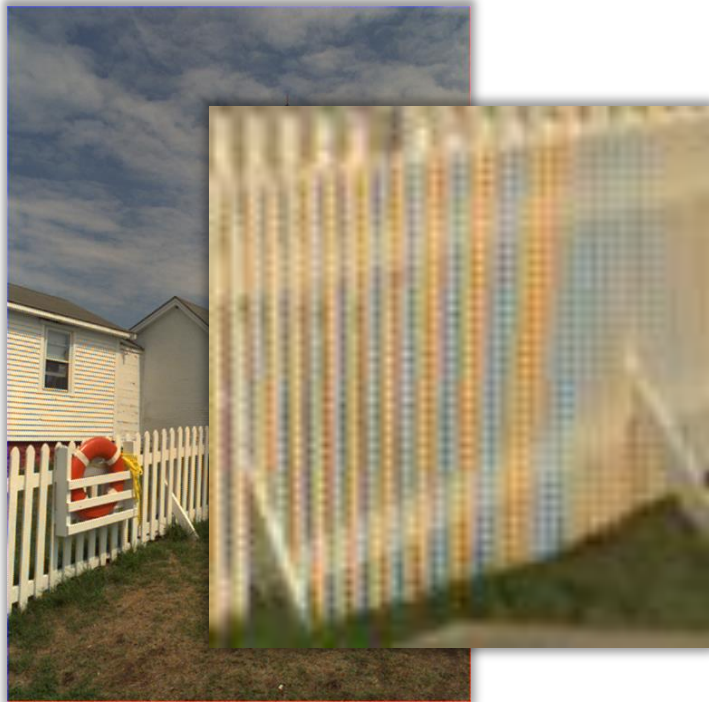
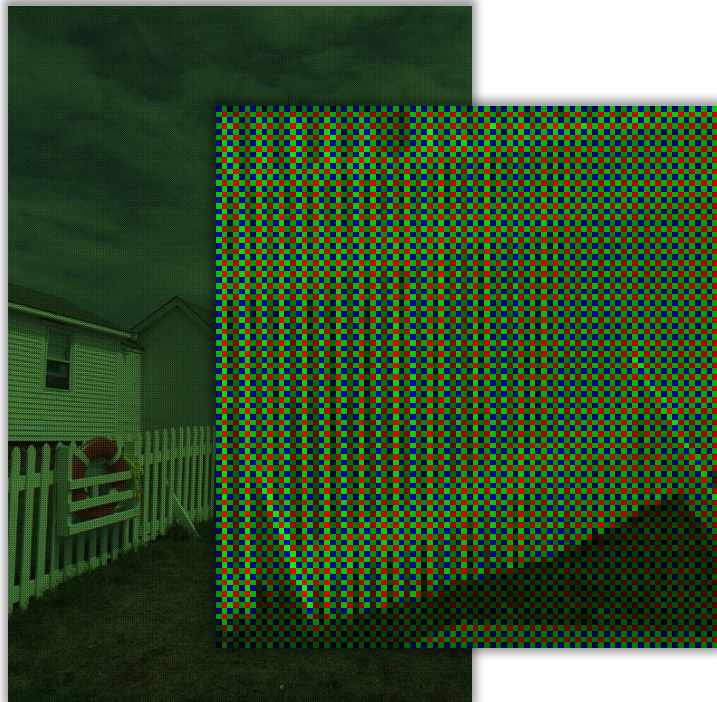
Bayer CFA



# Demosaicking (CFA Interpolation)

RAW

linear interpolation



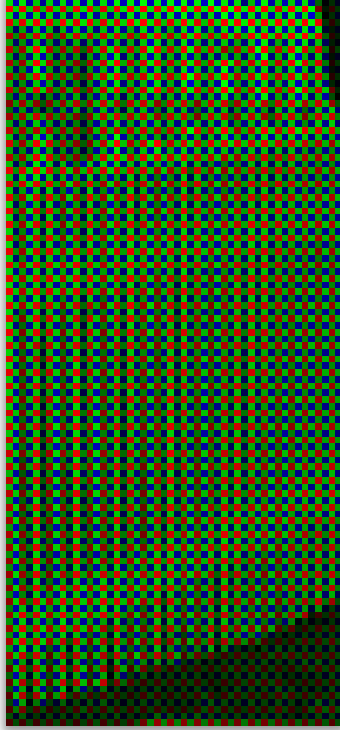
# Demosaicking (CFA Interpolation)

image from Kodac dataset

original



RAW



demosaicked



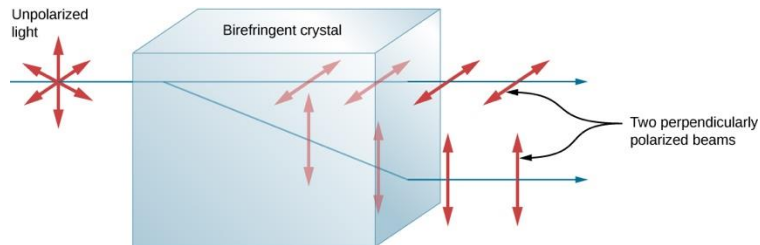


# Quick aside: optical low-pass filter

- Sensors often have a separate glass sheet in front of them acting as an optical low-pass filter (OLPF, also known as optical anti-aliasing filter).
- The OLPF is typically implemented as two birefringent layers, combined with the infrared filter.
- The two layers split 1 ray into 4 rays, implementing a 4-tap discrete convolution filter kernel.



birefringence in a calcite crystal



birefringence ray diagram

# Quick aside: optical low-pass filter

- Sensors often have a separate glass sheet in front of them acting as an optical low-pass filter (OLPF, also known as optical anti-aliasing filter).
- The OLPF is typically implemented as two birefringent layers, combined with the infrared filter.
- The two layers split 1 ray into 4 rays, implementing a 4-tap discrete convolution filter kernel.



- However, the OLPF means you also lose resolution.
- Photographers often hack their cameras to remove the OLPF, to avoid the loss of resolution (“hot rodding”).
- Camera manufacturers offer camera versions with and without an OLPF.

# Quick aside: optical low-pass filter

Example where OLPF is needed



without OLPF



with OLPF

# Quick aside: optical low-pass filter

Example where OLPF is unnecessary



without OLPF



with OLPF

# Quick aside: optical low-pass filter

Identical camera model with and without an OLPF (no need for customization).



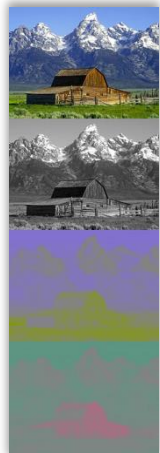
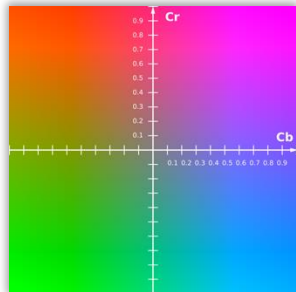
Nikon D800



Nikon D800E

# Demosaicing – Low-pass Chroma

- sampling problem (despite optical AA filter): (too) high-frequency red/blue information
- simple solution: low-pass filter chrominance – humans are most sensitive to “sharpness” in luminance:
  1. apply naïve interpolation
  2. convert to  $Y'CbCr$  (related to  $YUV$ )
  3. median filter chroma channels:  $Cb$  &  $Cr$
  4. convert back to  $RGB$

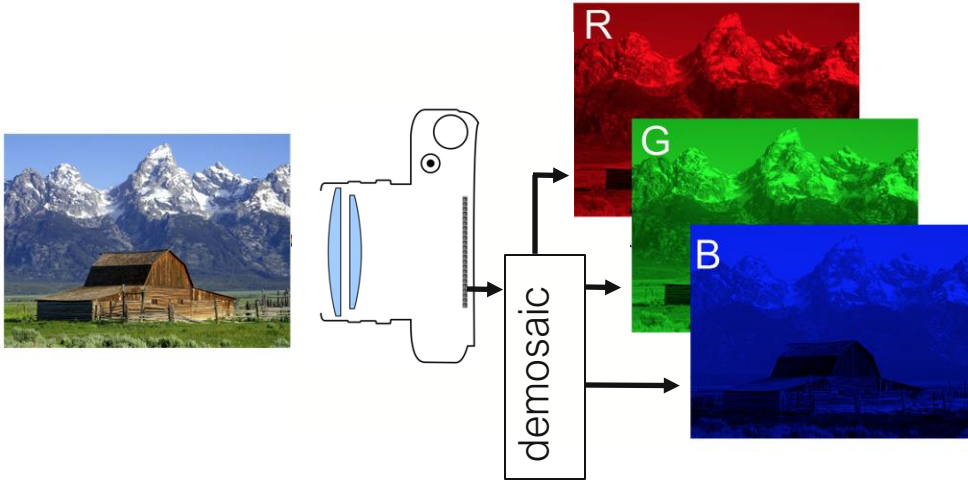


$Y'$

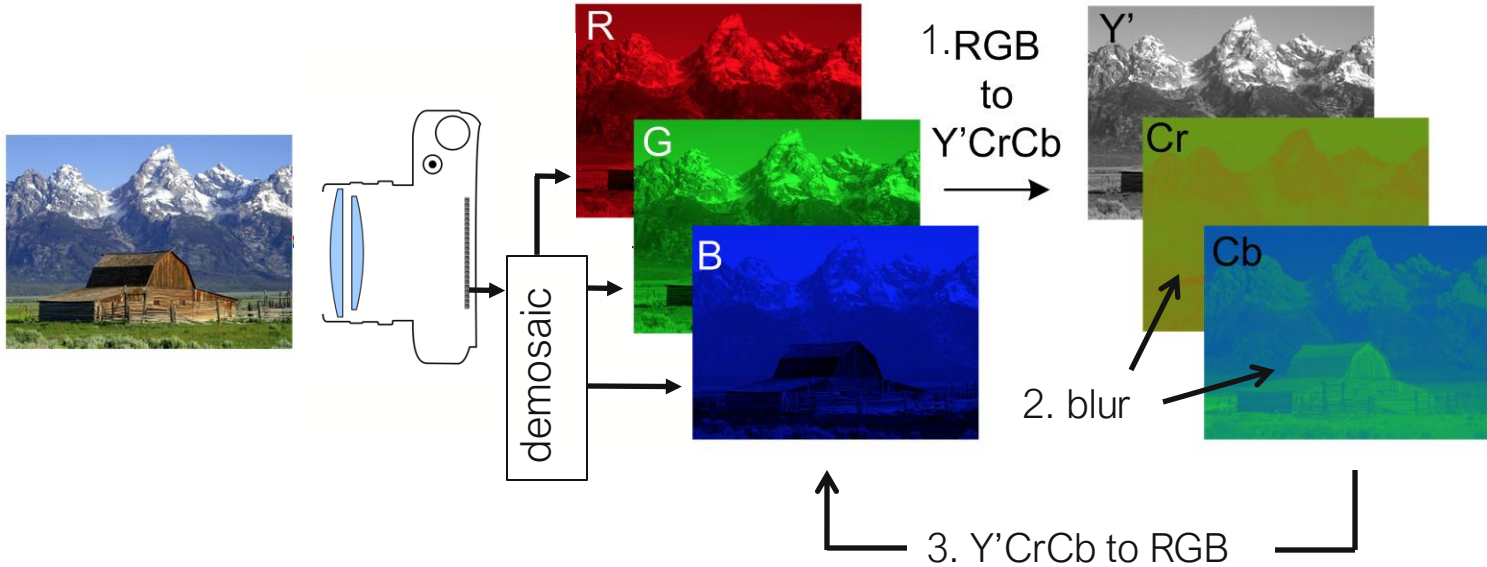
$Cb$

$Cr$

# Demosaicing – Low-pass Chroma



# Demosaicing – Low-pass Chroma





# Demosaicing – Low-pass Chroma

RGB to Y'CrCb:

$$\begin{bmatrix} Y' \\ Cb \\ Cr \end{bmatrix} = \underbrace{\begin{bmatrix} 65.48 & 128.55 & 24.87 \\ -37.80 & -74.20 & 112.00 \\ 112.00 & -93.79 & -18.21 \end{bmatrix}}_M \begin{bmatrix} R \\ G \\ B \end{bmatrix} \cdot \frac{257}{65535} + \begin{bmatrix} 16 \\ 128 \\ 128 \end{bmatrix}$$

Y'CrCb to RGB:

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = M^{-1} \left( \begin{bmatrix} Y' \\ Cb \\ Cr \end{bmatrix} - \begin{bmatrix} 16 \\ 128 \\ 128 \end{bmatrix} \right) \cdot \frac{65535}{257}$$

Matlab functions: *rgb2ycbcr()* and *ycbcr2rgb()*

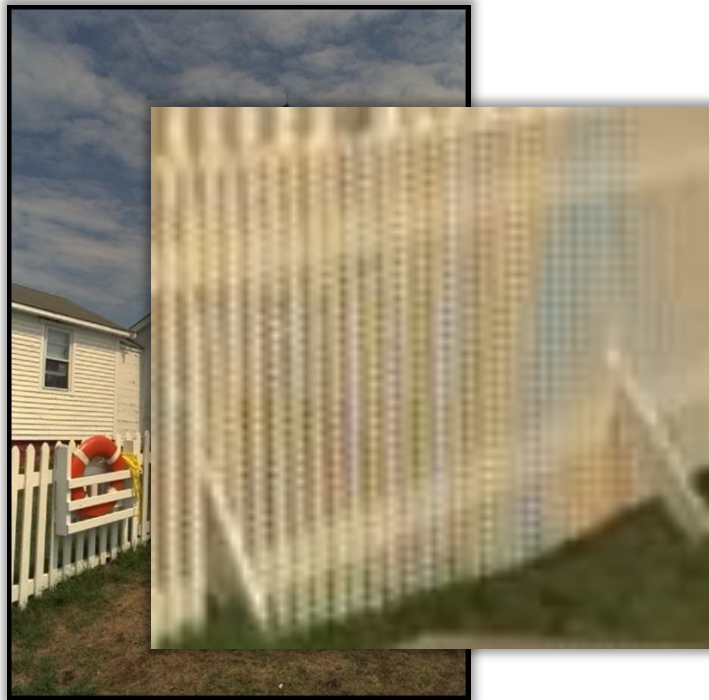
Pixel values for above equations between 0 and 255!

# Demosaicing – Low-pass Chroma

linear interpolation



chrominance filtered



# Demosaicing – Edge-Directed Interpolation

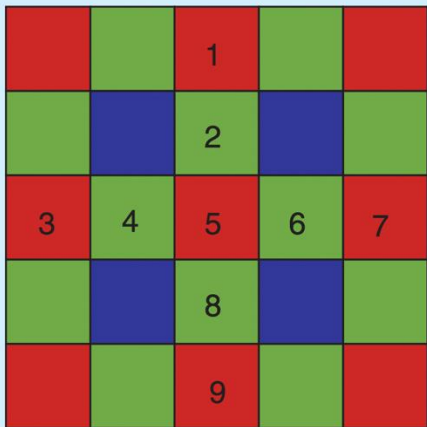
- intuitive approach: consider 3x3 neighborhood
- example: recover missing green pixel

	1	
2	3	4
	5	

1. Calculate horizontal gradient  $\Delta H = |G2 - G4|$
2. Calculate vertical gradient  $\Delta V = |G1 - G5|$
3. If  $\Delta H > \Delta V$ ,  
$$G3 = (G1 + G5)/2$$
Else if  $\Delta H < \Delta V$ ,  
$$G3 = (G2 + G4)/2$$
Else  
$$G3 = (G1 + G5 + G2 + G4)/4$$

# Demosaicing – Edge-Directed Interpolation

- better: consider 5x5 neighborhood
- example: recover missing green pixel on red pixel



1. Calculate horizontal gradient  $\Delta H = |(R3 + R7)/2 - R5|$
2. Calculate vertical gradient  $\Delta V = |(R1 + R9)/2 - R5|$
3. If  $\Delta H > \Delta V$ ,  
 $G5 = (G2 + G8)/2$   
Else if  $\Delta H < \Delta V$ ,  
 $G5 = (G4 + G6)/2$   
Else  
 $G5 = (G2 + G8 + G4 + G6)/4$

# Demosaicing – Edge-Directed Interpolation

- insights so far:
  - larger pixel neighborhood may be better, but also more costly
  - using gradient information (edges) may be advantageous, even if that info comes from other color channels!
  - nonlinear method is okay, but not great – linear would be best!
- Malvar et al. 2004 – what's the best linear filter for 5x5 neighborhood?
- this is implemented in Matlab function *demosaic()* and part of HW2

# Demosaicing- Malvar et al. 2004

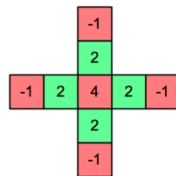
- interpolate G at R pixels:  $\hat{g}(x, y) = \hat{g}_{lin}(x, y) + aD_R(x, y)$

red gradient: 
$$D_R(x, y) = r(x, y) - \frac{1}{4} \sum_{(m, n)} r(x + m, y + n)$$
$$(m, n) = \{(0, -2), (0, 2), (-2, 0), (2, 0)\}$$

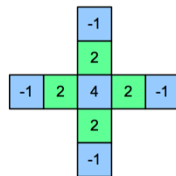
- interpolate R at G pixels:  $\hat{r}(x, y) = \hat{r}_{lin}(x, y) + bD_G(x, y)$
- interpolate R at B pixels:  $\hat{r}(x, y) = \hat{r}_{lin}(x, y) + gD_B(x, y)$
- gain parameters optimized from Kodak dataset:  $a = 1/2, b = 5/8, g = 3/4$

# Demosaicing - Malvar et al. 2004

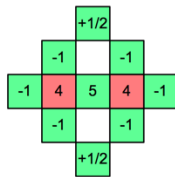
- write out math to get linear filters:
- use normalized filters in practice, i.e. scale numbers by sum of filter



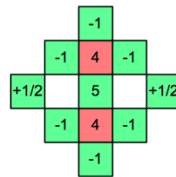
G at R locations



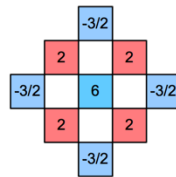
G at B locations



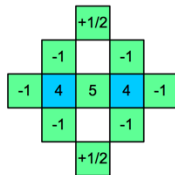
R at green in  
B row, B column



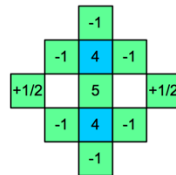
R at green in  
B row, R column



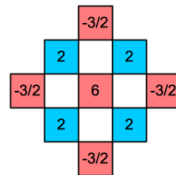
R at blue in  
B row, B column



B at green in  
B row, R column



B at green in  
R row, B column



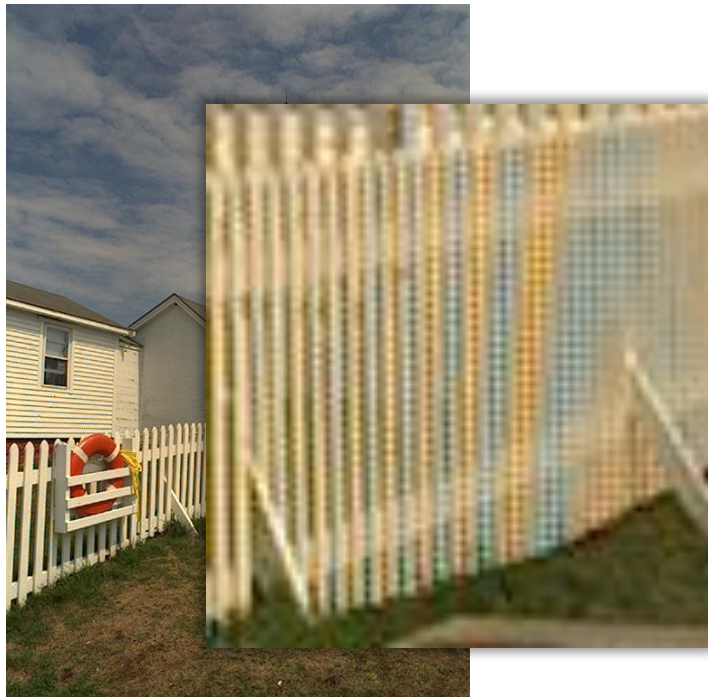
B at red in  
R row, R column

# Demosaicing - Malvar et al. 2004

linear interpolation



Malvar et al.





# Deblurring / Deconvolution

common sources:

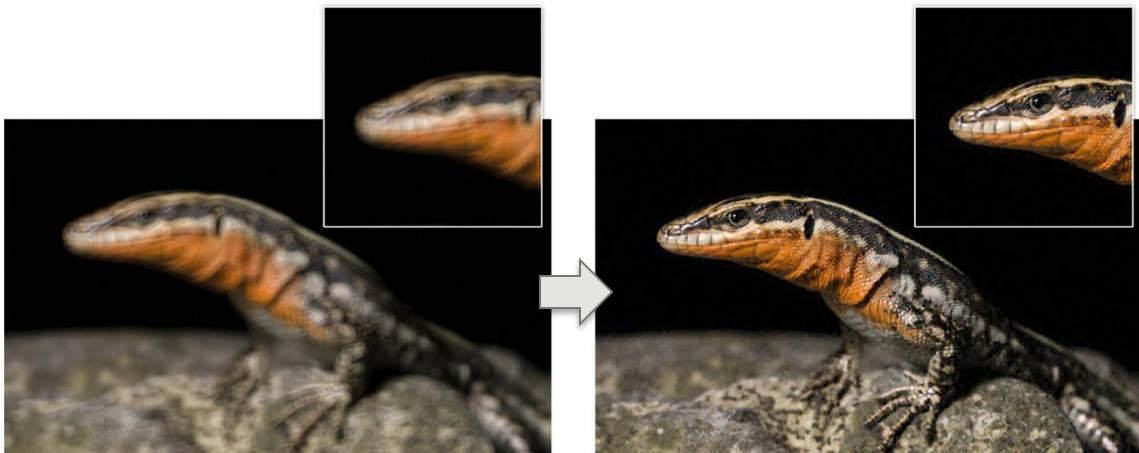
out-of-focus blur

geometric distortion

spherical aberration

chromatic aberration

coma



Blurred input image

Deblurred / deconvolved image

# Denoising



noisy image

(Gaussian iid noise,  $\sigma=0.2$ )

- problem: have noisy image, want to remove noise but retain high-frequency detail

# Denoising – Most General Approach

$$i_{denoised}(x) = \frac{1}{\sum_{\text{all pixels } x'} w(x, x')} \sum_{\text{all pixels } x'} i_{noisy}(x') \times w(x, x')$$



- many (not all) denoising techniques work like this
- idea: average a number of similar pixels to reduce noise
- question/difference in approach: how similar are two noisy pixels?

# Denoising – Most General Approach

$$i_{denoised}(x) = \frac{1}{\sum_{\text{all pixels } x'} w(x, x')} \sum_{\text{all pixels } x'} i_{noisy}(x') \times w(x, x')$$

1. Local, linear smoothing
2. Local, nonlinear filtering
3. Anisotropic diffusion
4. Non-local methods

# Denoising – 1. Local, Linear Smoothing

$$i_{denoised}(x) = \frac{1}{\sum_{\text{all pixels } x'} w(x, x')} \sum_{\text{all pixels } x'} i_{noisy}(x') \times w(x, x')$$

$$w(x, x') = \exp\left(-\frac{\|x' - x\|^2}{2\sigma^2}\right)$$

- naïve approach: average in local neighborhood, e.g. using a Gaussian low-pass filter

## Denoising – 2. Local, Nonlinear Filtering

$$i_{denoised}(x) = \textit{median}\left(W\left(i_{noisy}, x\right)\right)$$



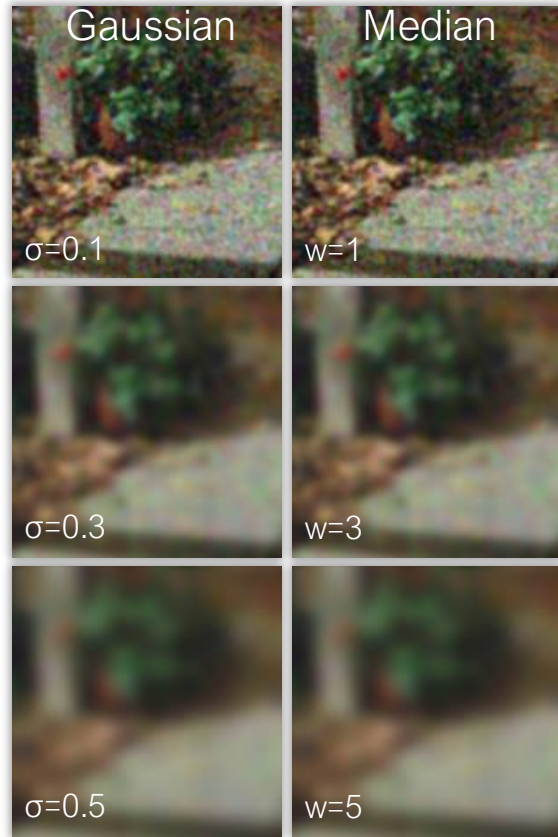
small window of image  $i_{noisy}$  centered at  $x$

- almost as naïve: use median filter in local neighborhood

# Denoising



noisy image (Gaussian,  $\sigma=0.2$ )



# Denoising – 3. Bilateral Filtering



original



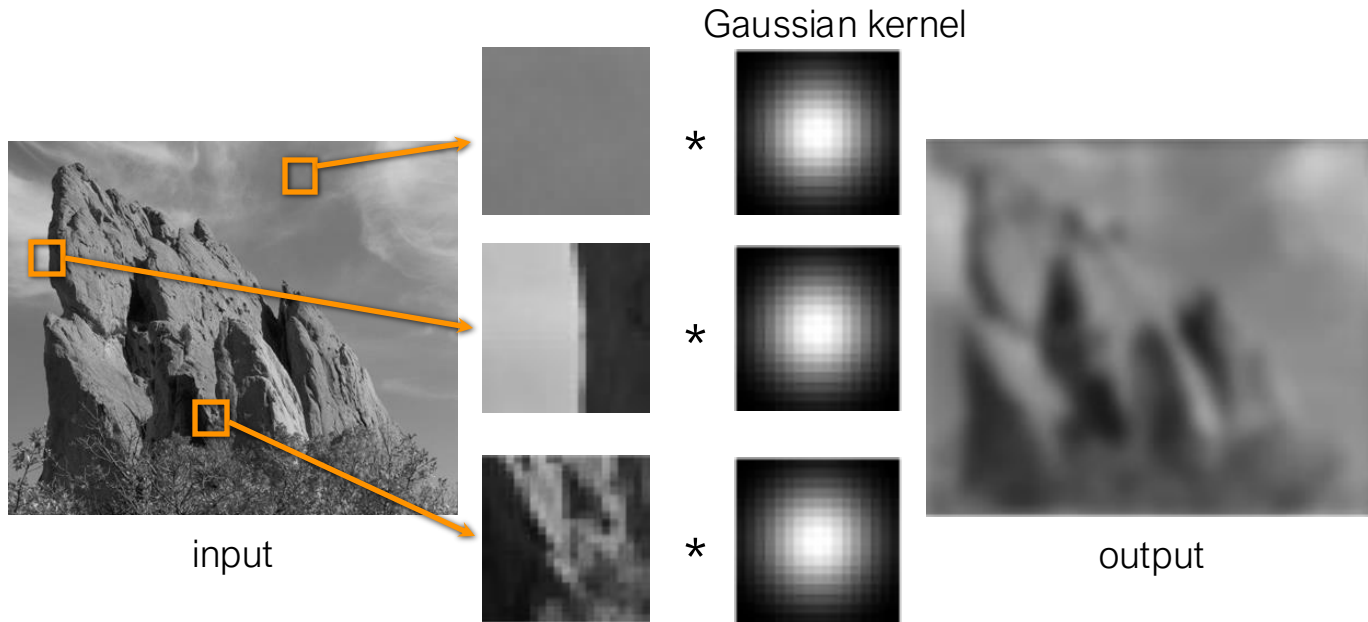
Gaussian filtering



bilateral filtering

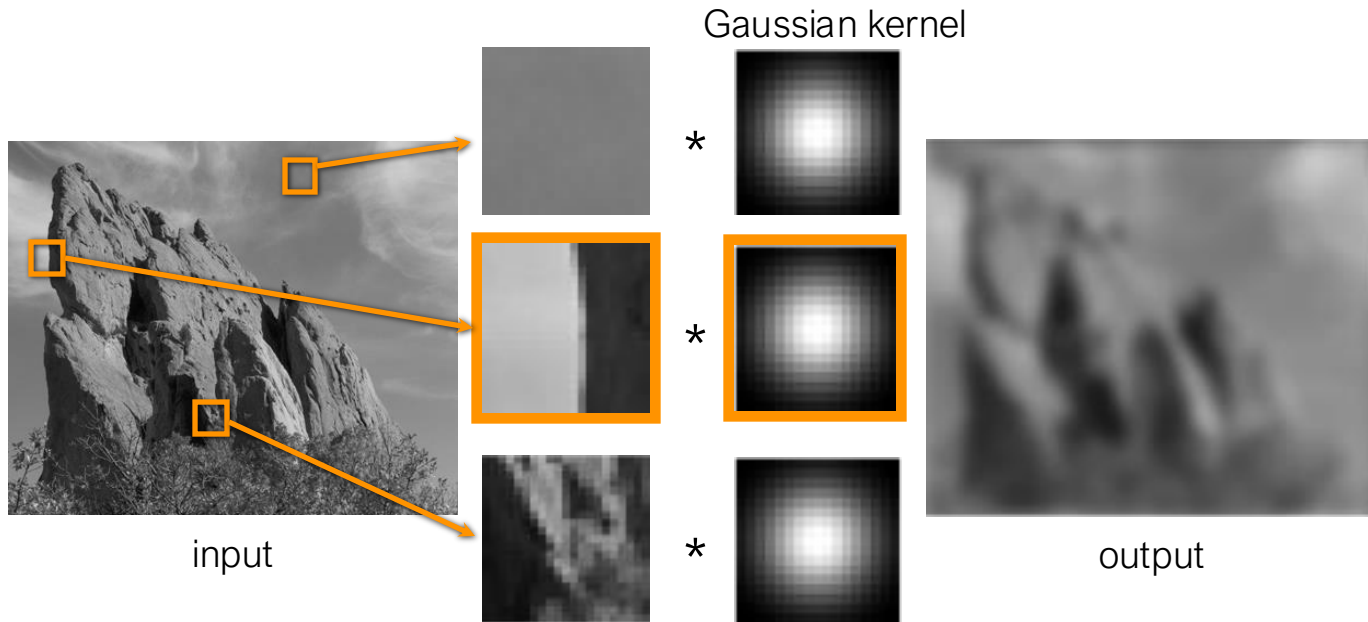


# Denoising – 3. Bilateral Filtering

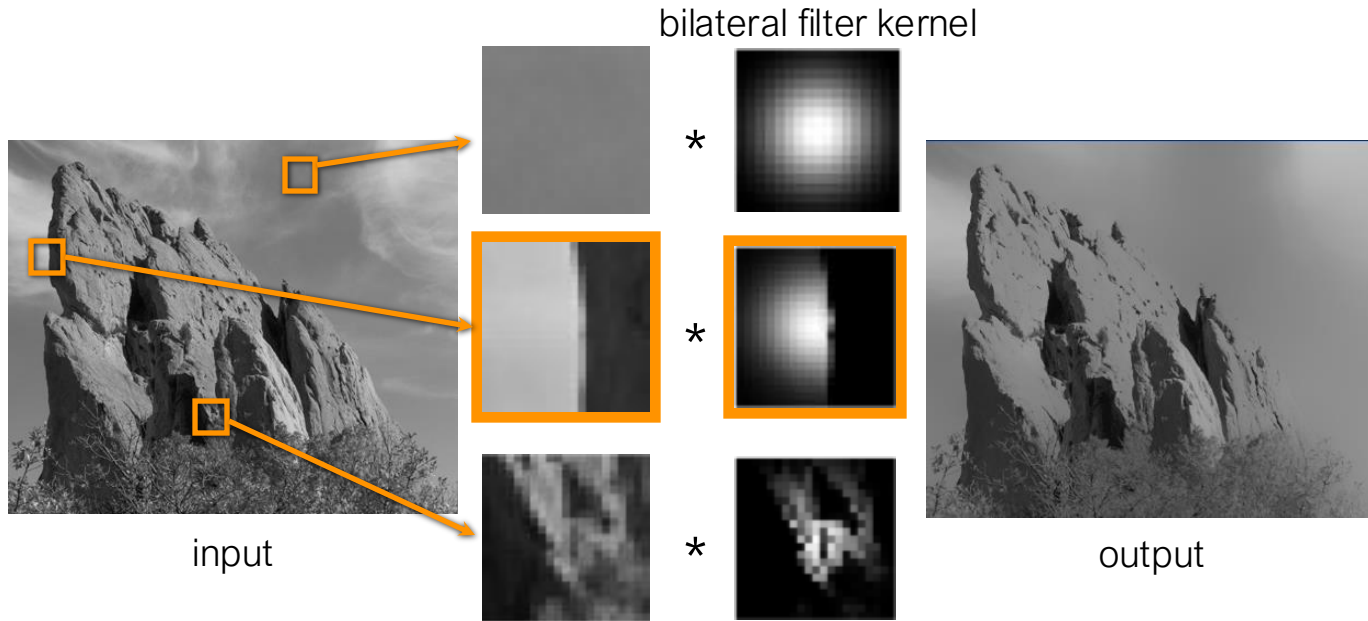


Why is the output so blurry?

# Denoising – 3. Bilateral Filtering



# Denoising – 3. Bilateral Filtering



Do not blur if there is an edge! How does it do that?

# Denoising – 3. Bilateral Filtering

$$i_{denoised}(x) = \frac{1}{\sum_{\text{all pixels } x'} w(x, x')} \sum_{\text{all pixels } x'} i_{noisy}(x') \times w(x, x')$$

spatial distance                      distance of intensities

$$w(x, x') = \exp\left(-\frac{\|x' - x\|^2}{2\sigma^2}\right) \cdot \exp\left(-\frac{\|i_{noisy}(x') - i_{noisy}(x)\|^2}{2\sigma_i^2}\right)$$

- more clever: average in local neighborhood, but only average similar intensities!

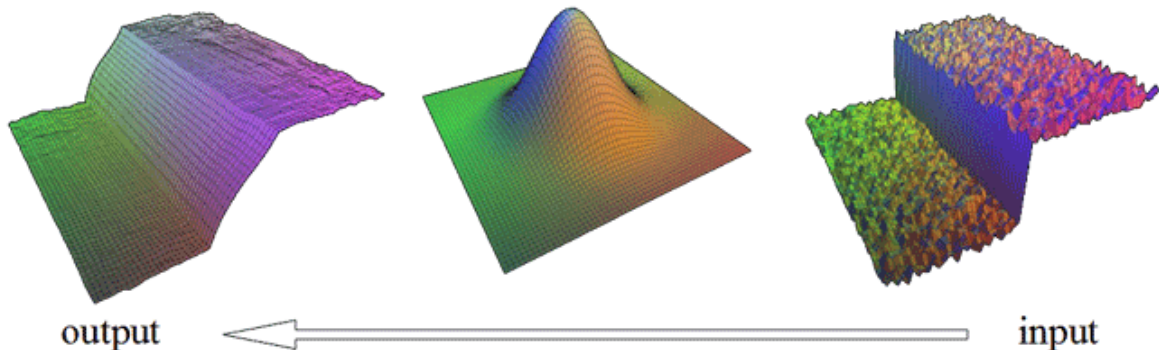
# Denoising – Gaussian Filter

$J$ : filtered output (is blurred)

$f$ : Gaussian convolution kernel

$I$ : step function & noise

$$J(x) = \sum_{\xi} f(x, \xi) I(\xi)$$



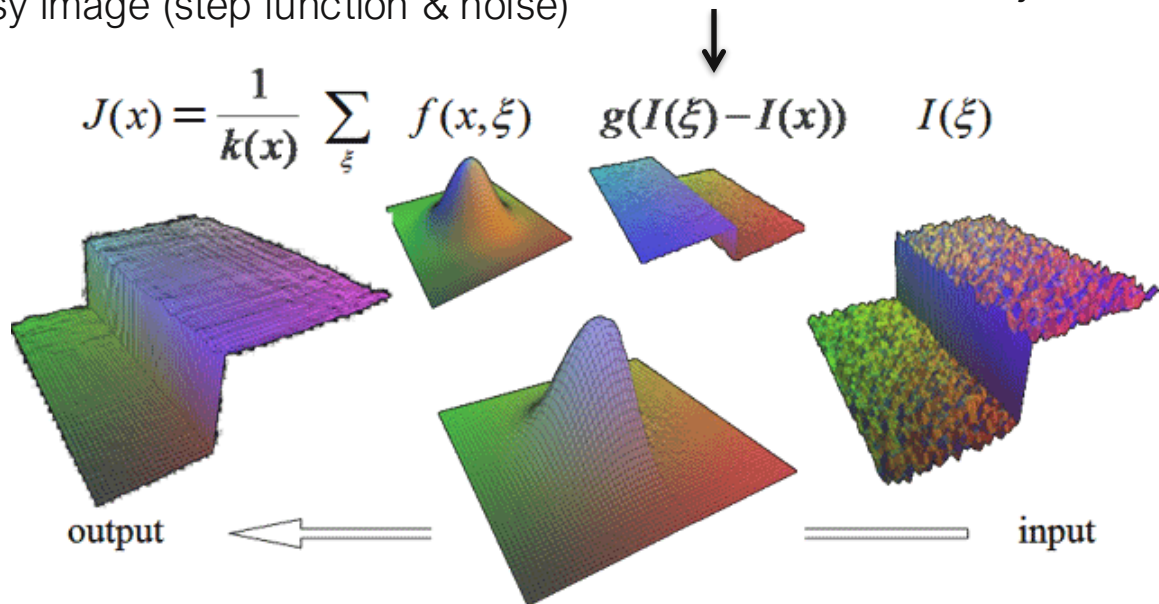
# Denoising – Bilateral Filter

J: filtered output (is not blurred)

f: Gaussian convolution kernel

I: noisy image (step function & noise)

difference in intensity as scale!



# Denoising – Bilateral Filter



original image



bilateral filter = “edge-aware smoothing”

# Denoising – Bilateral Filter



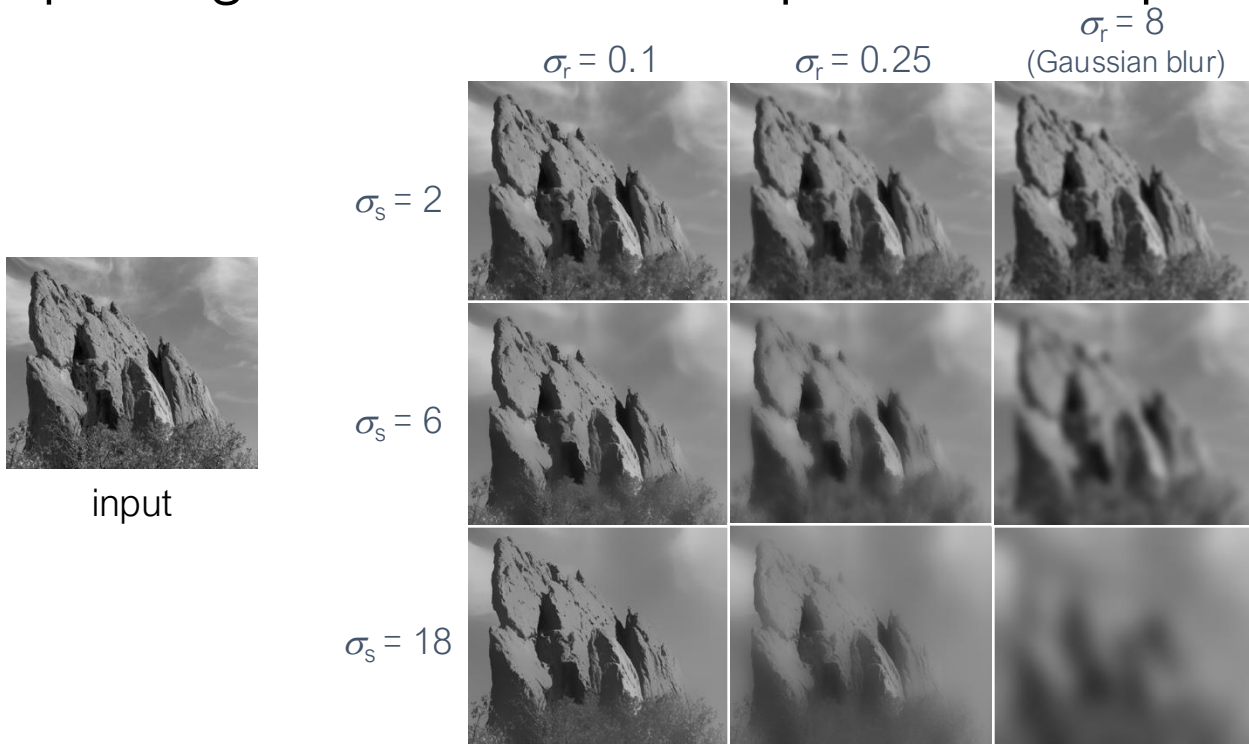
noisy image



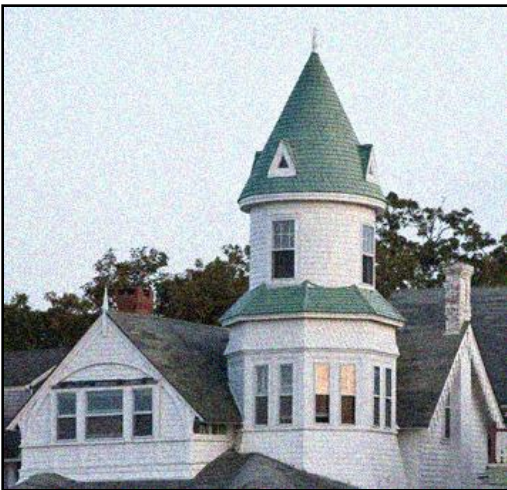
bilateral filter = “edge-aware smoothing”



# Exploring the bilateral filter parameter space



# Denoising



noisy input



bilateral filtering



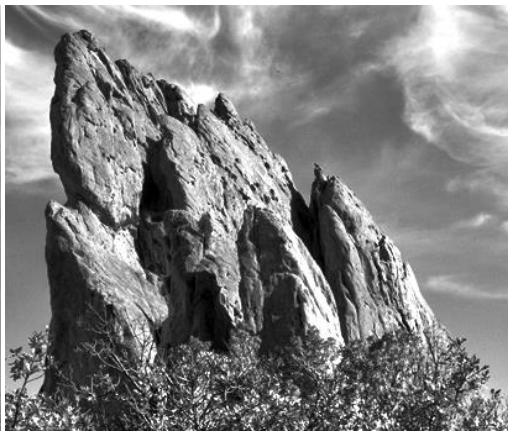
median filtering

# Contrast enhancement

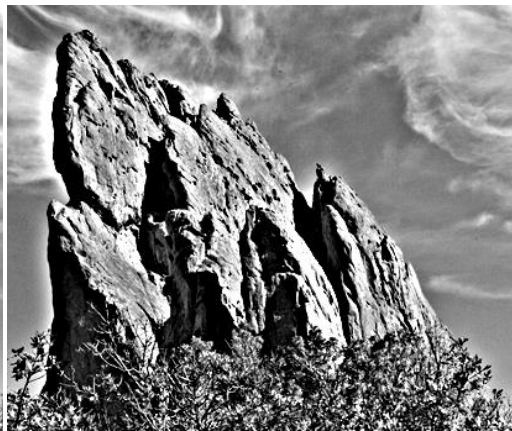
How would you use Gaussian or bilateral filtering for sharpening?



input



sharpening based on  
bilateral filtering



sharpening based on  
Gaussian filtering

# Photo retouching



# Photo retouching



original



digital pore removal (aka bilateral filtering)



# Before



# After



# Close-up comparison



original



digital pore removal (aka bilateral filtering)



# Cartoonization



input



cartoon rendition

# Cartoonization



How would you create this effect?

# Cartoonization



edges from bilaterally filtered image



+

bilaterally filtered image



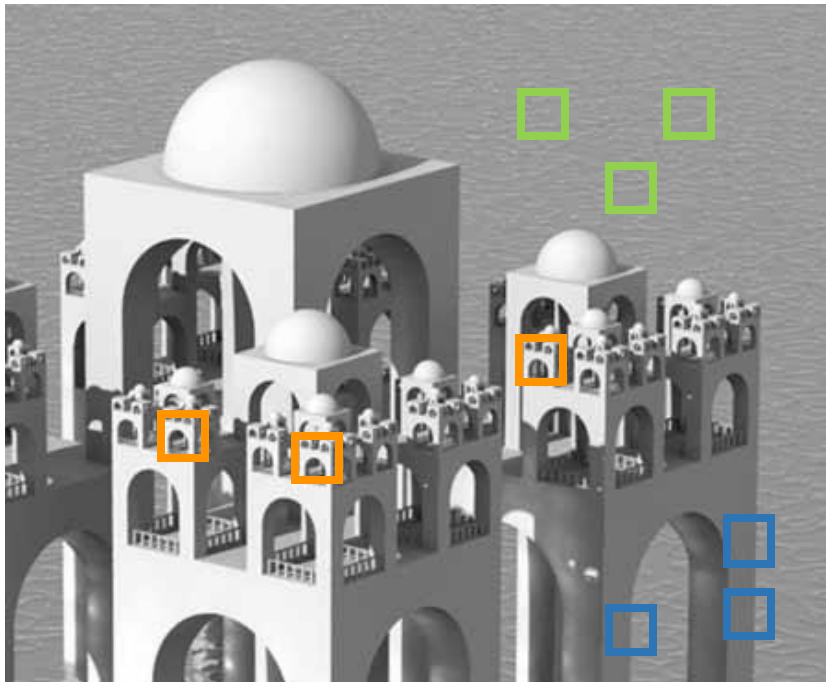
=

cartoon rendition



Note: image cartoonization and abstraction are very active research areas.

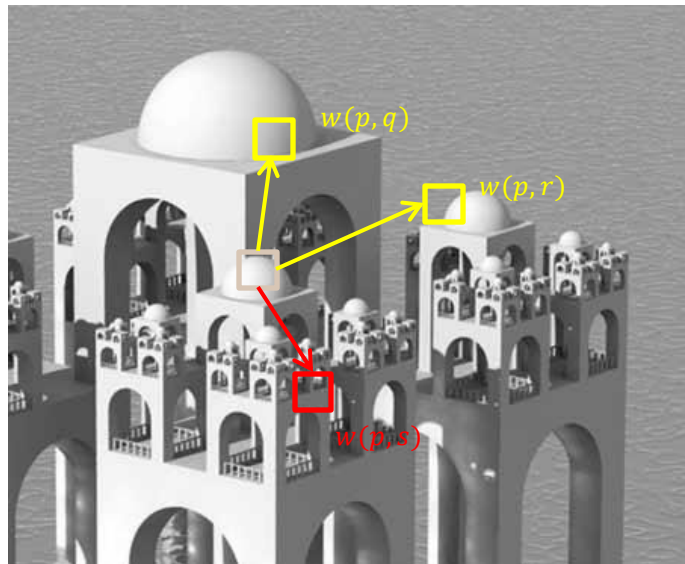
# Denoising – 4. Non-local Means



# Denoising – 4. Non-local Means

- define distance between global image patches
- average distant pixels with similar neighborhood!

$$i_{denoised}(x) = \frac{1}{N} \sum_{\text{all pixels } x' \in \mathcal{I}} i_{noisy}(x') \times w(x, x')$$



## Denoising – 4. Non-local Means

$$i_{denoised}(x) = \frac{1}{\sum_{\text{all pixels } x'} w(x, x')} \sum_{\text{all pixels } x'} i_{noisy}(x') \times w(x, x')$$

$$w(x, x') = \exp \left( - \frac{\|W(i_{noisy}, x') - W(i_{noisy}, x)\|^2}{2S^2} \right)$$

- very powerful approach: exploit self-similarity in image; average pixels with a similar neighborhood, but don't need to be close → non-local

# Denoising – 4. Non-local Means

noisy

Gaussian filtering

anisotropic filtering



TV

bilateral filtering

NL-means

# Everything put together

## Gaussian filtering

Smooths everything nearby (even edges)  
Only depends on spatial distance

## Bilateral filtering

Smooths 'close' pixels in space and intensity  
Depends on spatial and intensity distance

## Non-local means

Smooths similar patches no matter how far away  
Only depends on intensity distance



# Denoising – Other Non-local Method BM3D

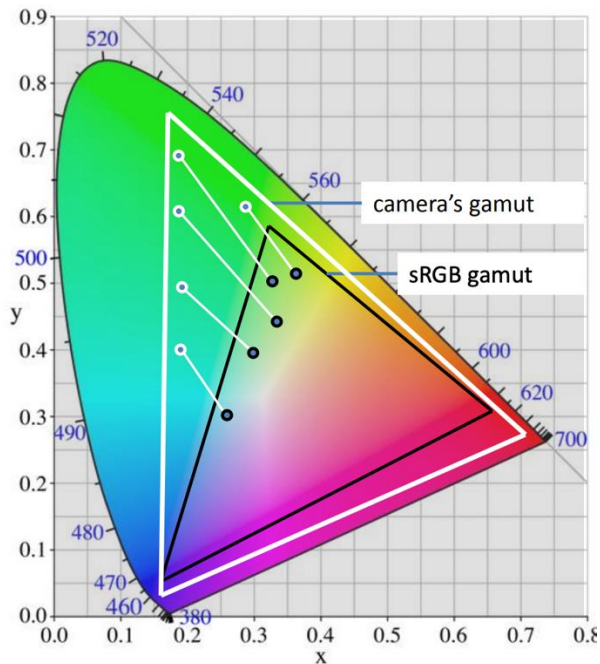
- find similar image patches and group them in 3D blocks
- apply collaborative filter on all of them:
  - DCT-transform each 3D block
  - threshold transform coefficients
  - inverse transform 3D block



# Denoising

- many methods for denoising (check Buades 2005):
  - filtering wavelet or other coefficients
  - total variation denoising
  - patch-based or convolutional sparse coding ...
- state of the art: non-local methods, in particular BM3D

# Gamut Mapping



Need to map from camera gamut to standard gamut (sRGB).

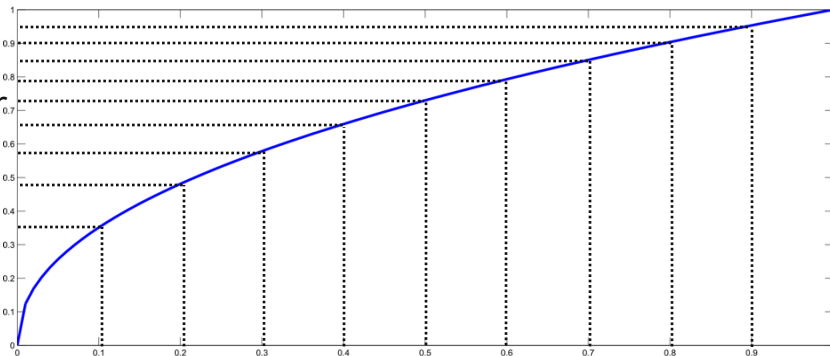
Different ways of projecting the colors lead to different camera modes (e.g., vivid, portrait, landscape, etc.).

Internally, we transform from camera XYZ  $\rightarrow$  CIE XYZ and eventually sRGB

# Gamma Correction

- from linear 10/12 bit to 8 bit (save space)
- perceptual linearity for optimal encoding with specific bit depth
- sensitivity to luminance is roughly  $\gamma=2.2$

perceptually linear  
spacing! →

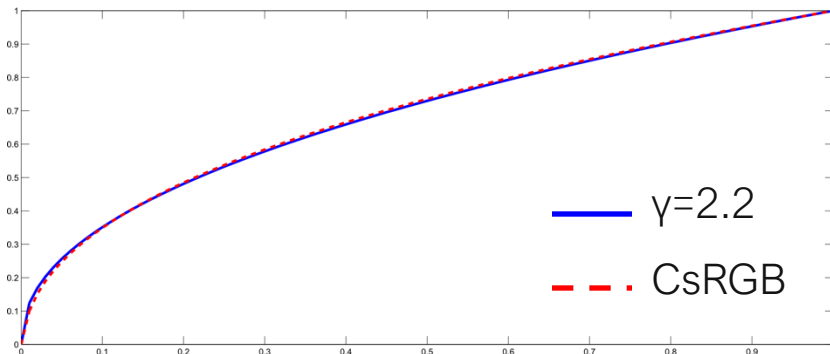


# Gamma Correction in sRGB

- standard 8 bit color space of most images, e.g. jpeg
- roughly equivalent to  $\gamma=2.2$

$$C_{sRGB} = \begin{cases} 12.92 C_{linear} & C_{linear} \leq 0.0031308 \\ (1 + a) C_{linear}^{1/2.4} - a & C_{linear} > 0.0031308 \end{cases}$$

linear  
 $a = 0.055$   
gamma



# Compression – JPEG (joint photographic experts group)



jpeg – ps quality 0

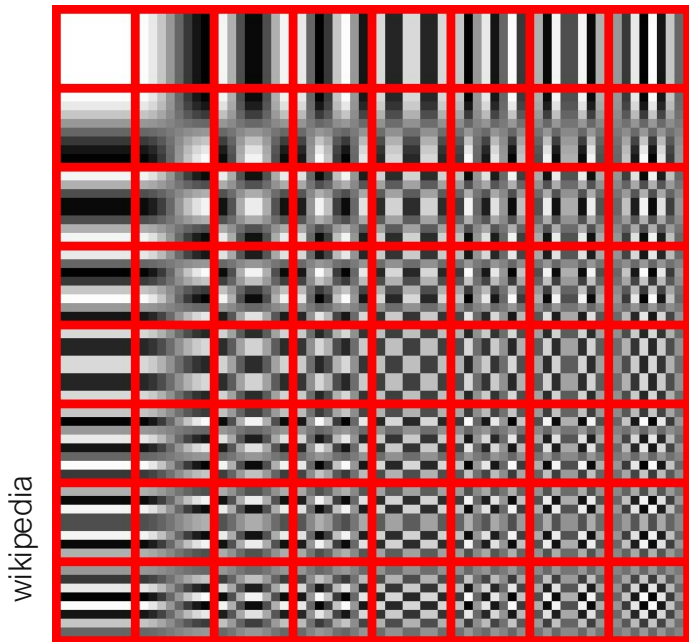
jpeg – ps quality 2

original

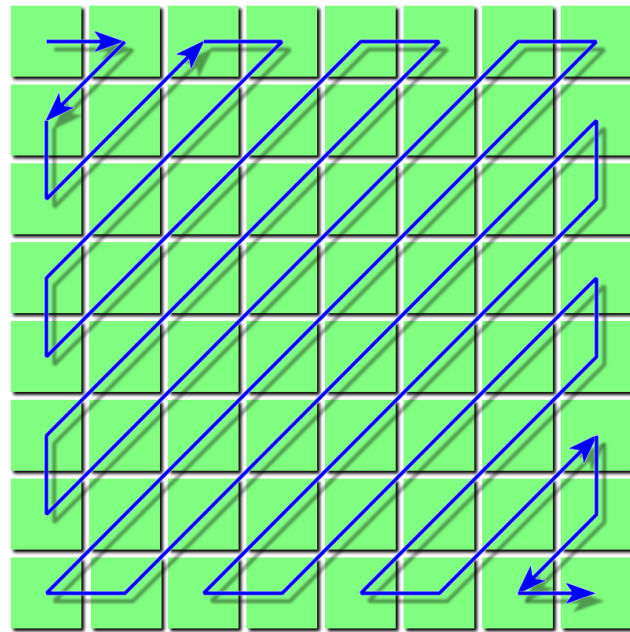
# Compression – JPEG (joint photographic expert group)

1. transform to YCbCr
2. downsample chroma components Cb & Cr
  - 4:4:4 – no downsampling
  - 4:2:2 – reduction by factor 2 horizontally
  - 4:2:0 – reduction by factor 2 both horizontally and vertically
3. split into blocks of 8x8 pixels
4. discrete cosine transform (DCT) of each block & component
5. quantize coefficients
6. entropy coding (run length encoding – lossless compression)

# Compression – JPEG (joint photographic expert group)



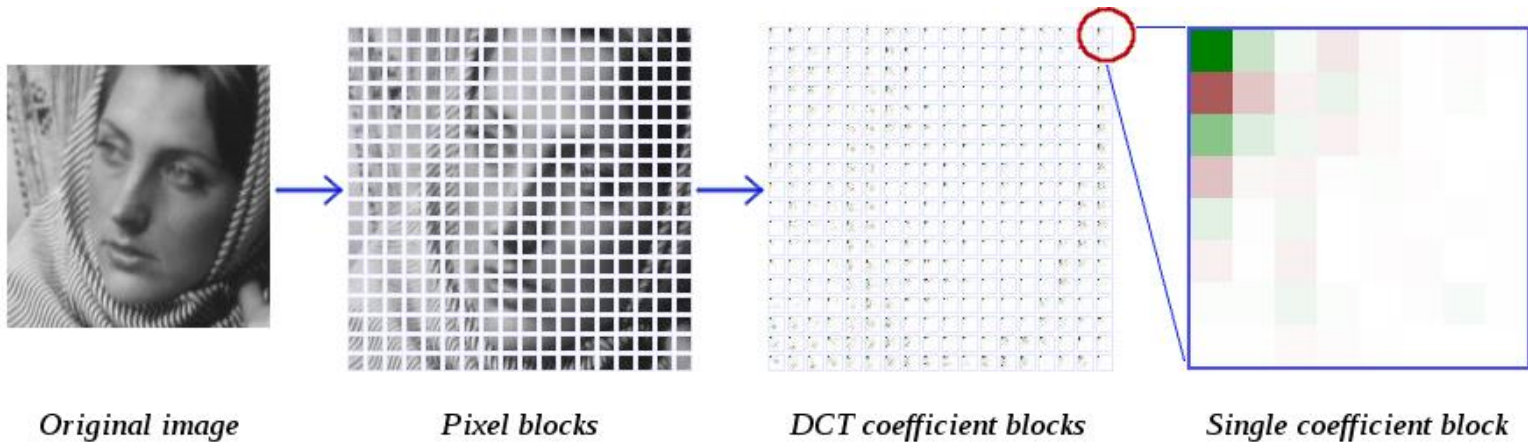
DCT basis functions



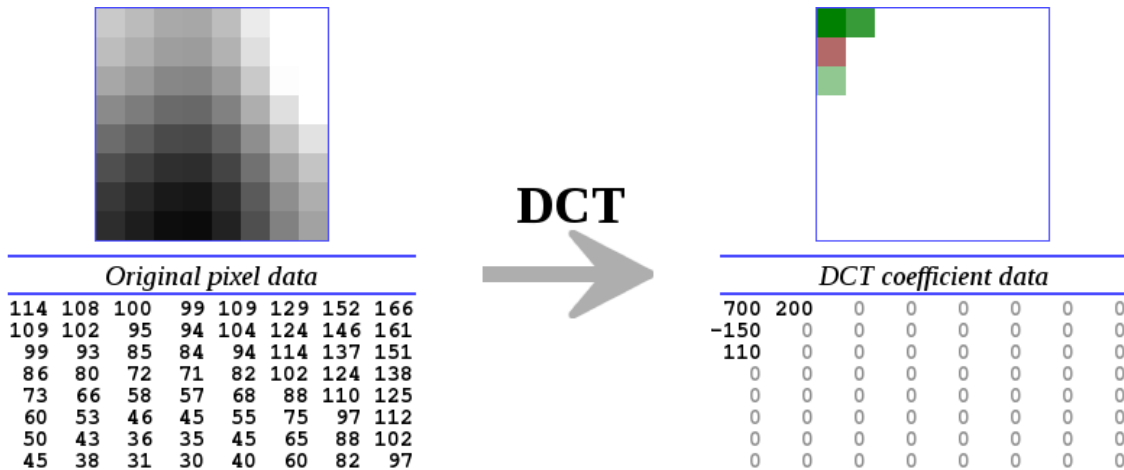
RLE of “same frequency” coefficients



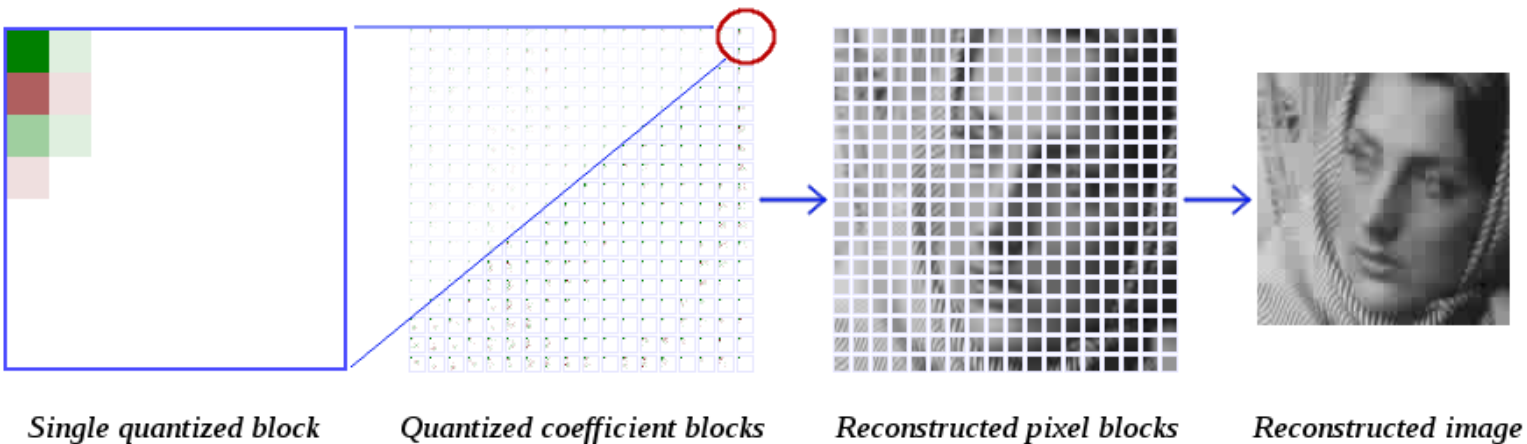
# Compression – JPEG (joint photographic expert group)



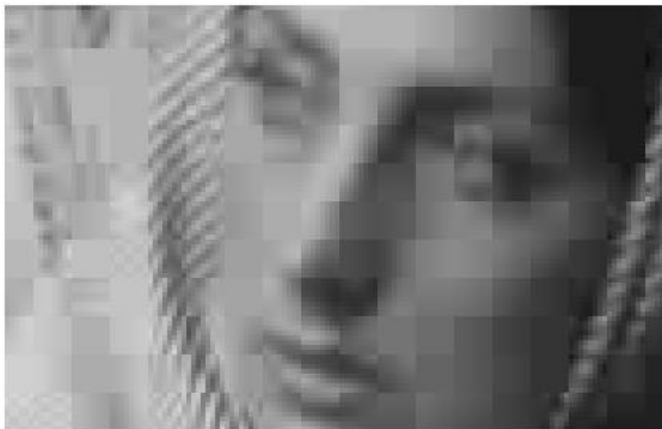
# Compression – JPEG (joint photographic expert group)



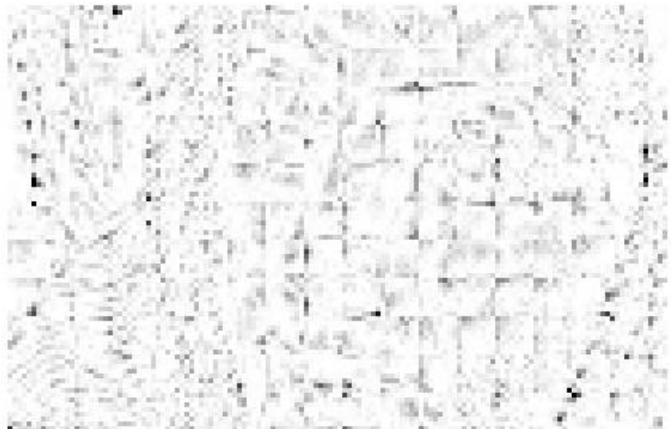
# Compression – JPEG (joint photographic expert group)



# Compression – JPEG (joint photographic expert group)



*Closeup of reconstructed image*



*Normalized error distribution within each block*

# Compression – JPEG (joint photographic experts group)



jpeg – ps quality 0



jpeg – ps quality 2



original

# Image Processing Pipeline



RAW image



demosaicking



...

denoising



...

gamut mapping



...

compression



JPEG image

# Homework 2

- calculate and plot depth of field of different cameras
- implement a simple image processing pipeline in Python and explore demosaicking, denoising, etc.

# Next: Math Review

- sampling
- filtering
- deconvolution
- sparse image priors
- ...



# References and Further Reading

## Denoising

- S. Paris, P. Kornprobst, J. Tumblin, F. Durand “A Gentle Introduction to Bilateral Filtering and its Applications”, SIGGRAPH 2007 course notes
- Buades, Morel, “A non-local algorithm for image denoising”, CVPR 2005
- Dabov, Foi, Katkovnik, Egiazarian, “Image denoising by sparse 3D transform-domain collaborative filtering”, IEEE Trans. Im. Proc. 2007

## Demosaicking

- Malvar, He, Cutler, “High-quality Linear Interpolation for Demosaicking of Bayer-patterned Color Images”, Proc. ICASSP 2004
- Gunturk, Glotzbach, Alltunbasak, Schafer, “Demosaicking: Color Filter Array Interpolation”, IEEE Signal Processing Magazine 2005

## Plenoptic function

- E. Adelson, J. Bergen “The Plenoptic Function and Elements of Early Vision”, Computational Models of Visual Processing, 1991
- G. Wetzstein, I. Ihrke, W. Heidrich “On Plenoptic Multiplexing and Reconstruction”, Int. Journal on Computer Vision, 2013

## Other, potentially interesting work

- F. Heide, S. Diamond, M. Niessner, J. Ragan-Kelly, W. Heidrich, G. Wetzstein, “ProxImaL: Efficient Image Optimization using Proximal Algorithms”, ACM SIGGRAPH 2016
- Kodac dataset (especially good and standard for demosaicking): <http://r0k.us/graphics/kodak/>