



# Problem Session 4

# Topics

- High dynamic range images
  - Debevec's Method
  - Tone mapping
- SNR Calculations
  - Burst Imaging
  - Flutter Shutter

# HDR & Tone mapping



Several 8-bit images  
acquired at different  
exposures ([0 255])

HDR algorithm



64-bit image  
That has all  
important  
information

Tone mapping



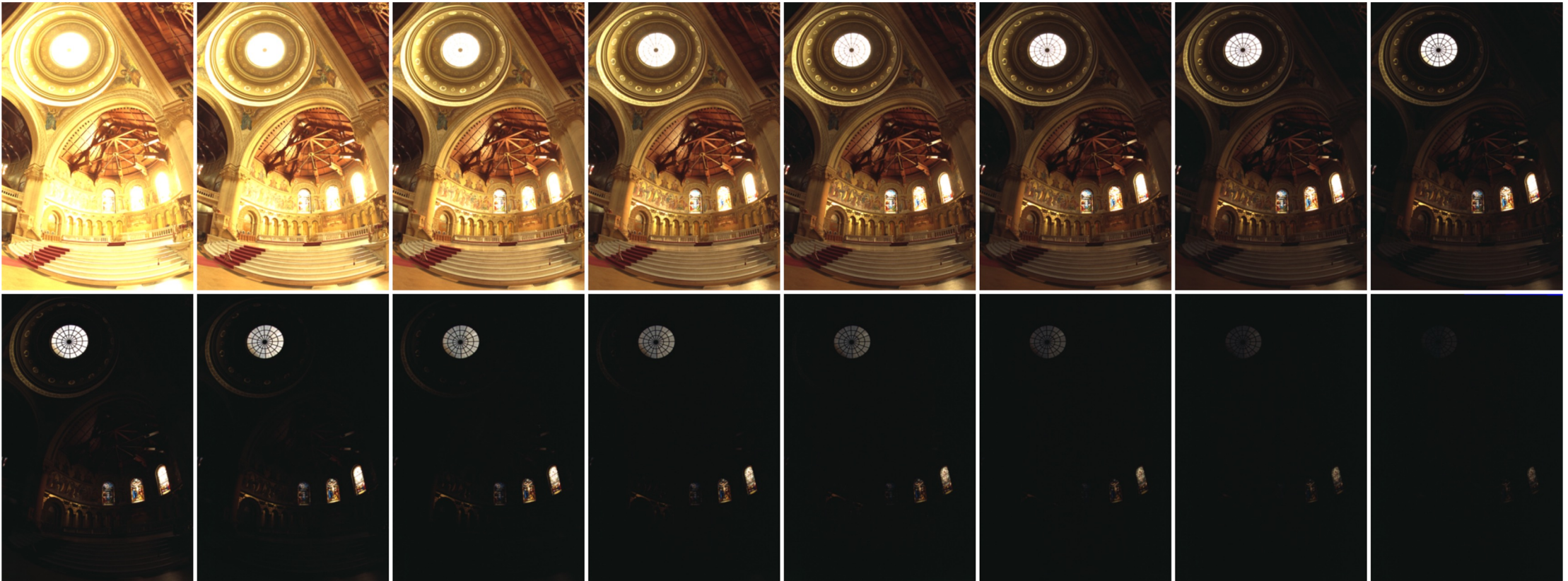
8-bit image  
That has all important  
information and can be  
viewed on a regular screen



# Task 1: High dynamic range

(Debevec's method)

```
# Number of Images
16
# Filename 1/shutter_speed f/stop gain(db) ND_filters
memorial0061.ppm 0.03125 8 0 0
memorial0062.ppm 0.0625 8 0 0
memorial0063.ppm 0.125 8 0 0
memorial0064.ppm 0.25 8 0 0
memorial0065.ppm 0.5 8 0 0
memorial0066.ppm 1 8 0 0
memorial0067.ppm 2 8 0 0
memorial0068.ppm 4 8 0 0
memorial0069.ppm 8 8 0 0
memorial0070.ppm 16 8 0 0
memorial0071.ppm 32 8 0 0
memorial0072.ppm 64 8 0 0
memorial0073.ppm 128 8 0 0
memorial0074.ppm 256 8 0 0
memorial0075.ppm 512 8 0 0
memorial0076.ppm 1024 8 0 0
```



# Task 1: High dynamic range

Linearize the images using gamma of 2.2



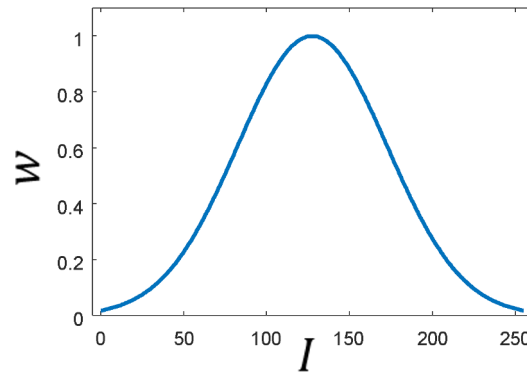
# Task 1: High dynamic range image

Computing the weights: we want to give a higher weight to pixels that are close to the center of the dynamic range at each exposure  $k$ .

$$w_{k,ij} = \exp\left(-4 \frac{(I_{k,ij} - 0.5)^2}{0.5^2}\right)$$

Center of the dynamic range  
(127.5 if pixels are [0,255])

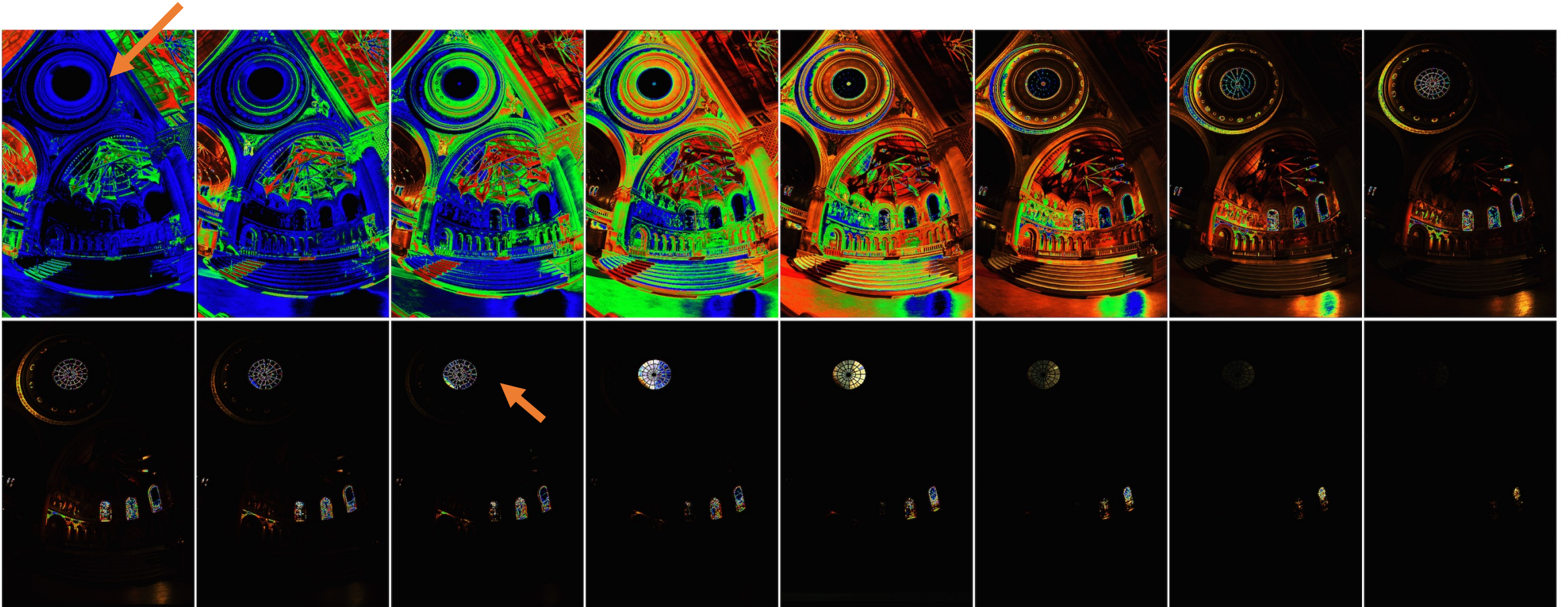
Linearized image  
( $\gamma=2.2$ )



Compute this per color channel

# Task 1: High dynamic range

Weights using Debevec's method (all 3 color channels)



# Task 1: High dynamic range image

Find a good estimation,  $\hat{X}$ , for the “true image”,  $X$ , using an optimization problem:

Perceptually similar

Minimize the difference, in log scale, between your result,  $\hat{X}$ , at different exposures  $t_k$  and the acquired images at different exposures ( $I_{lin_k}$ ). Multiplied by weight to indicate what's more important.

$$\underset{\hat{X}}{\text{minimize } O} = \sum_k w_k \left( \log(I_{lin_k}) - \log(t_k \hat{X}) \right)^2$$

Calculating the derivative of  $O$ , we get:

$$\hat{X} = \exp \left( \frac{\sum_k w_k (\log(I_{lin_k}) - \log(t_k))}{\sum_k w_k} \right)$$

scale



# Task 1: High dynamic range - Tonemapping

- After exp, scaling, cropping, try your own scaling+gamma correction
- Choose scale and gamma yourself, report chosen parameters and resulting image
  - Don't scale+shift to fill the range [0, 1], scale only

$$I_{HDR} = (s \times I_{HDR_{linear}})^{\gamma}$$

- Also try Drago's tonemapping from opencv

```
# Normalize
hdr = np.exp(hdr / scale)
hdr *= 0.8371896/np.mean(hdr) # th

# convert to 32 bit floating point
hdr = np.float32(hdr)

# crop boundary - image data here a
hdr = hdr[29:720, 19:480, :]
```

# Task 1: High dynamic range

Adjusting  $\gamma$  and  $s$



$s = 0.1$

$s = 1.0$

$$\gamma = \frac{1}{5}$$

$$\gamma = \frac{1}{3}$$

$$\gamma = \frac{1}{2.2}$$

$$\gamma = 1/4$$

# Task 1: High dynamic range

Generate a tonemapped image using  
`cv2.createTonemapDrago`



# Task 2/3: Denoising and SNR

- Read noise
  - Noise from heat in pixel hardware when image is captured
  - Signal-independent
  - Typically modelled as a **Gaussian distribution**
- Shot noise
  - Noise from statistics of light-pixel interactions
  - Signal-dependent
  - Typically modelled as a **Poisson distribution**

## Task 2: Burst SNR calculations

$$SNR = \frac{\mu}{\sigma} = \frac{\text{mean number of photons}}{\text{standard deviation of noise}}$$

- Adding  $k$  signals of strength  $\mu \Rightarrow$  mean becomes  $k\mu$
- Scaling Gaussian/Poisson variable by  $k \Rightarrow$  variance becomes  $k^2\sigma^2$
- Adding independent Gaussian distributions  
$$G(\mu_1, \sigma_1^2) + G(\mu_2, \sigma_2^2) \sim G(\mu_1 + \mu_2, \underbrace{\sigma_1^2 + \sigma_2^2}_{\text{Variance} = (\text{standard deviation})^2})$$
- Adding independent Poisson distributions  
$$Pois(\lambda_1) + Pois(\lambda_2) \sim Pois(\underbrace{\lambda_1 + \lambda_2}_{\text{Both mean and variance}})$$
- Both signal and noise increase with the number of photons.
  - However, signal increases faster than noise!

# Task 3: Flutter Shutter

You're asked to compare the SNR of two imaging setups:

- Consumer camera in everyday use
- sCMOS in microscopy

At different acquisition modes:

- Flutter shutter
- Burst

Calculate the SNR and discuss your results.

# Task 3: SNR calculations

## **Consumer camera in everyday conditions:**

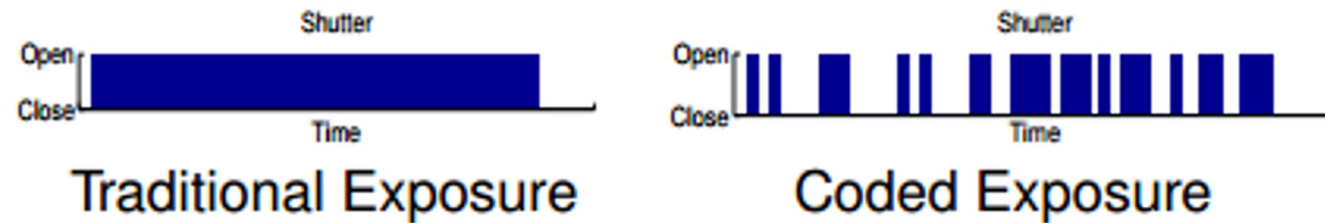
- Lots of photons (low shot noise)
- Room temperature (high read noise)

## **sCMOS microscope sensor in controlled conditions:**

- Few photons (high shot noise)
- Cooled sensor (low read noise)

# Task 3: SNR calculations

**Flutter shutter:** temporally modulated aperture pattern. Used, for example, for better motion deblurring (see “*Coded Exposure Photography: Motion Deblurring using Fluttered Shutter*”, Raskar et al.). The result is a single image.



**Burst:** acquires multiple short-exposure images. (for this problem, assume no delay between exposures)

**Tradeoff:** Number of exposures vs. number of photons



# Task 3: SNR calculations

For each of the four cases, calculate:

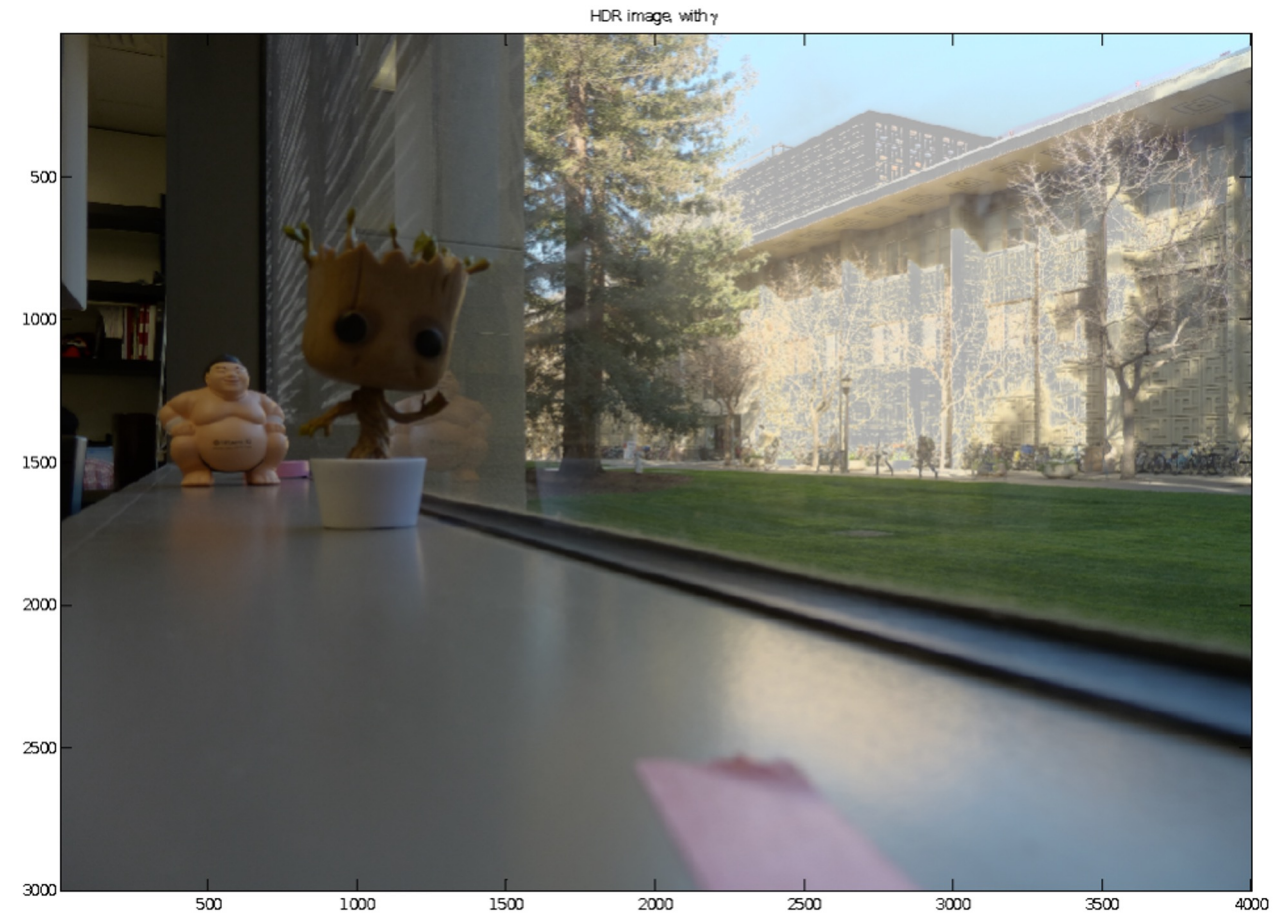
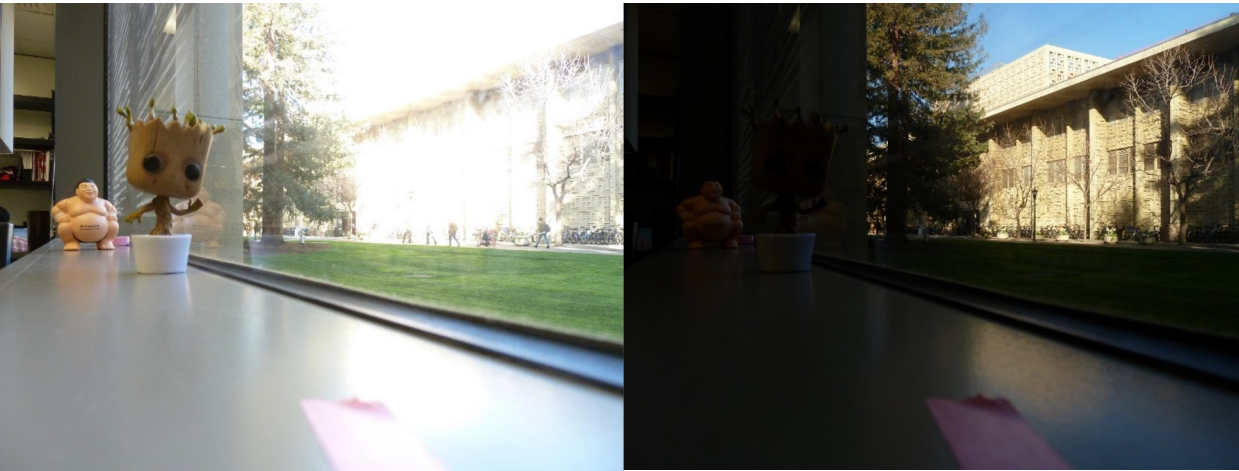
- The average number of photons (the signal)
- The standard deviation of the noise
- and divide them

Don't forget to describe your results and conclusions.

Intuitively, what general behavior do you expect?

# Bonus: your own HDR image

Around ~10 images with different exposures



# Have a nice weekend!

And good luck with the homework!



Stanford Memorial Church (HDR) <https://www.flickr.com/photos/scottloftesness/4334766965>