CSC338: Tutorial 2

1. Show that in a floating point system $F(\beta, p, L, U)$, the largest floating point number is $(1 - \beta^{-p})\beta^{U+1}$.

2. Consider, again, the IEEE SP floating point system $F(\beta = 2, p = 24, L = -126, U = 127)$. We discussed in class that 23 bits are used to store the mantissa, 8 bits for the exponent, and 1 bit for the sign. Suppose we were to use 22 bits to store the mantissa and 9 bits to store the exponent. Would our new system have more or fewer normalized floating point numbers?

3. Consider the floating point number system $F(\beta = 10, p = 4, L = -8, U = 8)$, and the following constants:

$$
\begin{aligned}
a &= 5.659 \times 10^4 \\
b &= 5.629 \times 10^4 \\
c &= 9.337 \times 10^2 \\
d &= 7.529 \times 10^{-1}
\end{aligned}
$$

   What are the values of:

   1. $a + b$
   2. $a - b$
   3. c/d
   4. $b \times d$
   5. $(a + c) - (b + d)$

   Is there a way to rearrange the last computation, to make the result more accurate?

4. You are having trouble computing $x^2 - y^2$ with enough precision in floating point arithmetic. What can you do?