

CSC338: Tutorial 2

1. Show that in a floating point number system $F(\beta, p, L, U)$, the largest floating point number is $(1 - \beta^p)\beta^{U+1}$.
2. Consider, again, the IEEE SP floating point system $F(\beta = 2, p = 24, L = -126, U = 127)$. We discussed in class that 23 bits are used to store the mantissa, 8 bits for the exponent, and 1 bit for the sign. Suppose we were to use 22 bits to store the mantissa and 9 bits to store the exponent. Would our new system have more or fewer normalized floating point numbers?
3. Consider the floating point number system $F(\beta = 10, p = 4, L = -8, U = 8)$, and the following constants:

$$a = 5.659 \times 10^4$$

$$b = 5.629 \times 10^4$$

$$c = 9.337 \times 10^2$$

$$d = 7.529 \times 10^{-1}$$

What are the values of:

1. $a + b$
2. $a - b$
3. c/d
4. $b \times d$
5. $(a + c) - (b + d)$

Is there a way to rearrange the last computation, to make the result more accurate?

4. You are having trouble computing $x^2 - y^2$ with enough precision in floating point arithmetic. What can you do?