UNIVERSITY OF TORONTO
Faculty of Arts and Science

Midterm CSC324H1

Duration: 50 minutes Instructor(s): David Liu. **No Aids Allowed**

Name:

Student Number:

Please read the following guidelines carefully.

- Please print your name and student number on the front of the exam.
- This examination has **4** questions. There are a total of **8 pages, DOUBLE-SIDED**.
- The last page is an aid sheet that may be detached.
- You may always write helper functions unless asked not to.
- Documentation is *not* required unless asked for.
- Answer questions clearly and completely. Provide justification unless explicitly asked not to.

Take a deep breath.

This is your chance to show us

How much you've learned.

We **WANT** to give you the credit

That you've earned.

A number does not define you.

Question	Grade	Out of
Q1		8
Q2		8
Q3		4
Q4		6
Total		26

1. **[8 marks] Short answer.**

   (a) **[4 marks]** You are given the following Racket definitions.

```
(define (f x)
  (lambda (y) (* x y)))

(define g (f 10))
```

   For each of the following Racket code snippets, state what value would be output, or briefly describe what error would be raised, when the snippet is evaluated.

   (i) `g`

   (ii) `(g 3)`

   (iii) `((g 3))`

   (iv)
```
(let ([x 100])
  (g 3))
```

(b) **[2 marks]** Consider the following Racket function.

```
(define (count-evens numbers)
  (if (null? numbers)
      0
      (if (even? (first numbers))
          (+ 1 (count-evens (rest numbers)))
          (count-evens (rest numbers)))))
```

Is this function *tail-recursive*? Explain your answer.

(c) **[2 marks]** Consider the following Haskell function.

```
f 0 x = x
f 1 x = 0
f n x = f (n - 2) (x + 4)
```

When we evaluate `f 10000000 0` in the interpreter (`ghci`), a very large amount of memory is used. Explain.

2. **[8 marks] Functional programming.** Consider the following description of a function `sequence`.

```
#|
(sequence functions input)
    Given a list of unary functions [f1, f2, f3, ... f-k] and input x,
    returns the value of (f-k (f-{k-1} ... (f2 (f1 x)) ... )).
    Returns `input` itself if the list of functions is empty.
|#
; Example:
(sequence (list (lambda (x) (+ x 1)) (lambda (x) (* x 3)) (lambda (x) (- 100 x)))
          4)
; Equals 85: (- 100 (* (+ 4 1) 3))
```

(a) **[4 marks]** Implement `sequence` in Racket **or** Haskell using explicit recursion. (Don't do both; only the first implementation will be graded.) Do not define any helper functions, and do not use any *list* functions that aren't found on the aid sheet.

(b) **[4 marks]** Implement `sequence` in Racket **or** Haskell without explicit recursion, and instead using one or more higher-order list functions (e.g., `map`, `filter`, `foldl`).

3. **[4 marks] Short answer (macros).** Consider the following Racket macro.

```
(define-syntax my-mac
  (syntax-rules ()
    [(my-mac <a> (<b> ...))

     (define (<a> f)
       (cond
         [(f <b>) <b>] ...
         [else (error "None")]))]))
```

(a) **[2 marks]** In the space below, give an example use of `my-mac` so that below it, the expression `(my-f even?)` evaluates to `4`.

```
; YOUR MACRO EXPRESSION GOES HERE.




(my-f even?)   ; After evaluating your macro expression, this line should evaluate to 4.
```

(b) **[2 marks]** We have seen in the course that macros can be used to avoid the eager evaluation semantics of function calls. Write a Racket code snippet that illustrates *short-circuiting behaviour* of `my-mac`. Also, *briefly explain* why your code illustrates that behaviour.

4. **[6 marks] Class macro.** The macro `my-class-constraints` behaves similarly to `my-class` (on the aid sheet), except it supports runtime checks on values passed to the constructor, raising an error if a check is violated.

```
(my-class-constraints Point
  ; A point has two attributes, x and y, that must both be integers.
  ; Note that `integer?` is a built-in predicate.
  ((x integer?)
   (y integer?))

  ; The syntax for methods is the same as on the aid sheet.
  ...
  )

> (define p1 (Point 2 3))        ; p1 behaves exactly the same as in the original macro.
> (define p2 (Point "hello" 3))  ; Calling `Point` here raises an error.
Error: Contract violation in constructor
```

(a) **[2 marks]** Give an example use of `my-class-constraints` to create a class `Person` that has *no methods* and *two attributes*, `name` and `age`. This class enforces the following constraints when its constructor is called:

- A person's name is a string (use `string?`).
- A person's age is a non-negative integer.

(b) **[2 marks]** Complete the macro *pattern* for `my-class-constraints`. Your pattern should match zero or more attributes; *every* attribute must be paired with an expression representing a predicate.

```
(define-syntax my-class-constraints
    (syntax-rules (method)
      [(my-class-constraints <Class>
         ; (non-function) attributes
         ; YOUR CHANGES GO HERE!









         ; methods -- Don't change this part.
         (method (<name> <params> ...) <body>) ...)
```

(c) **[2 marks]** Write the macro *template* (i.e., what the macro expands into) to implement the required behaviour for `my-class-constraints`.

Important: in the `my-class` macro found on the aid sheet, refer to the entire `(let ([class__dict__ ...]) ...)` nested under `(define (<Class> <attr> ...)` expression as `LET-EXPR`. You may *not* modify anything in `LET-EXPR` in your new template; instead, write "`LET-EXPR`" in your new template to refer to this part (so that you don't need to rewrite the entire thing).

```
; Write your template here.
; Your solution should be quite short. Write "LET-EXPR" to re-use most of the
; original macro template.
; HINT: `and` and `or` take an arbitrary number of arguments.
```

Use this page for rough work. If you want work on this page to be marked, please indicate this clearly *at the location of the original question.*