



Image: Trawling for Babel fish. Concept and juxtaposition: Raeid Saqur.

Statistical + Neural machine translation

CSC401/2511 – Natural Language Computing – Spring 2026

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Lecture 6

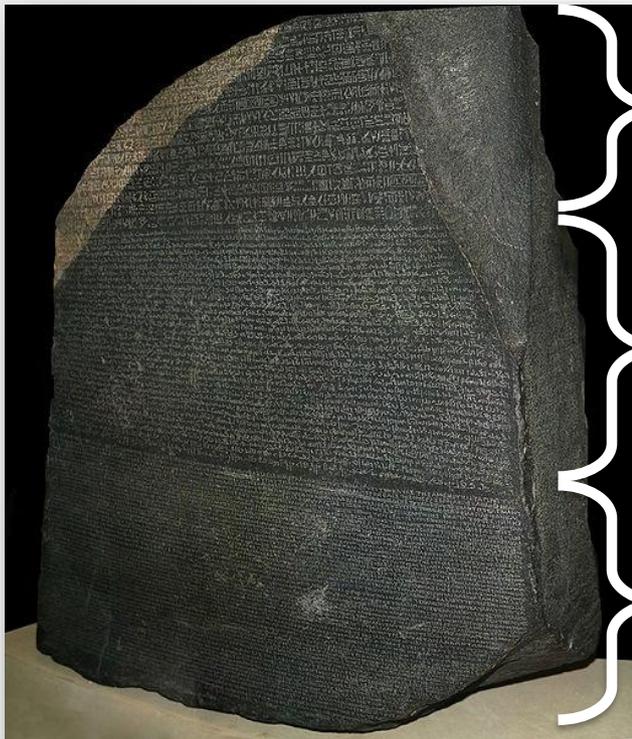
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The Rosetta Stone

- The **Rosetta Stone** dates from 196 BCE.
 - It was re-discovered by French soldiers during Napoleon's invasion of Egypt in 1799 CE.



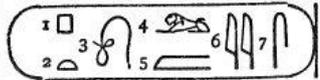
Ancient
Egyptian
hieroglyphs

Egyptian
Demotic

Ancient
Greek

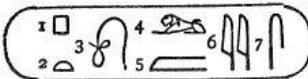
- It contains three **parallel** texts in different languages.
- Demotic had been partly deciphered.
- *For 20+ years after Rosetta's discovery, Egyptian hieroglyphics largely remained a mystery.*

Deciphering Rosetta

- During 1822–1832, **Jean-François Champollion** worked on the Rosetta stone. He noticed:
 1. The circled Egyptian symbols, e.g.  appeared in roughly the same positions as words like 'Ptolemy' in Greek.
 2. The number of Egyptian hieroglyph tokens was **much larger** than the number of Greek words → Egyptian seemed to have been partially phonographic.
 3. Cleopatra's cartouche was written 



Deciphering Rosetta

- So if  was 'Ptolemy' and  was 'Cleopatra' and the symbols corresponded to sounds – can we match up the symbols?

								
P	T	O	L	M	E	S		
								
C	L	E	O	P	A	T	R	A

- This approach demonstrated the value of working from **parallel texts** to decipher an unknown language:
 - *There are several examples of decipherment having been achieved without aligning unknown words in bitexts.*

Circa 2016

- What happened to my machine translation (SMT)?
 - ABC's speech recognizer transcribes French as though it were English in the Prime Minister's bilingual remarks:

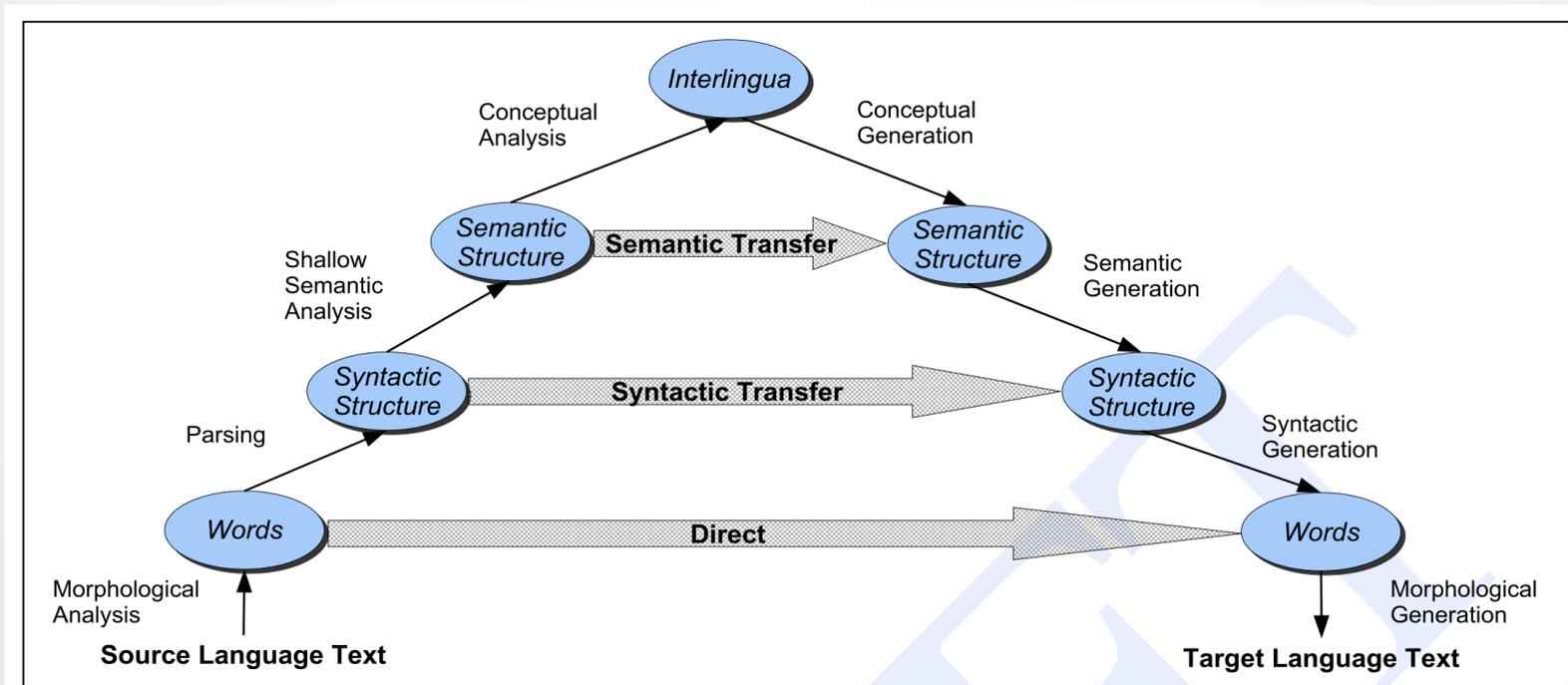


*“...Nazi innings...
...recourse to ice packs
...I'd love the log trucks”*



The Vauquois triangle (1968)

- High-level classes of methodologies:
 - “Direct” Translation
 - Syntactic Transfer
 - Semantic Transfer
 - Interlingua

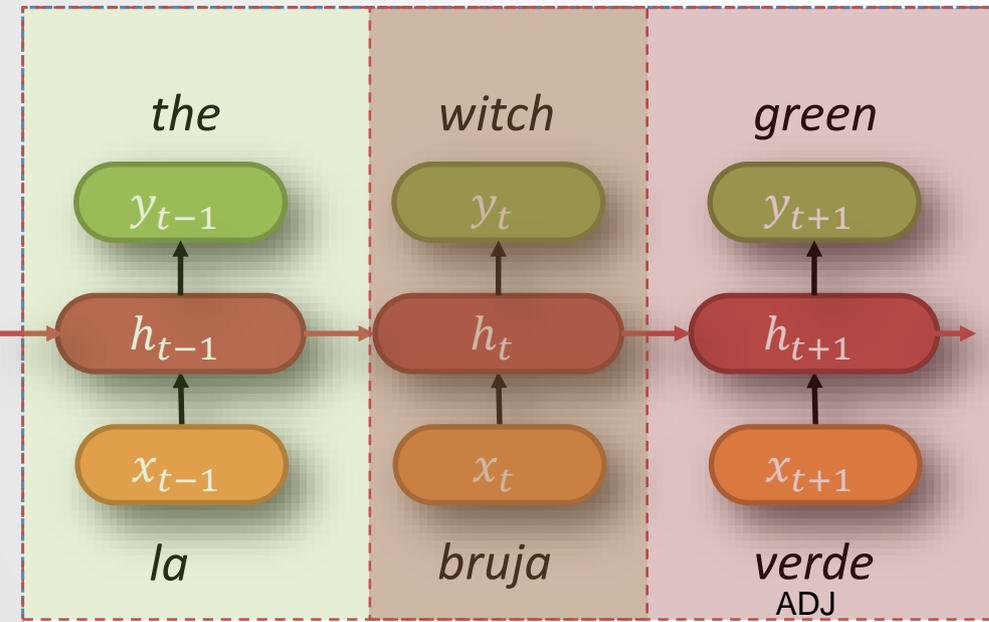


Seq2seq motivation

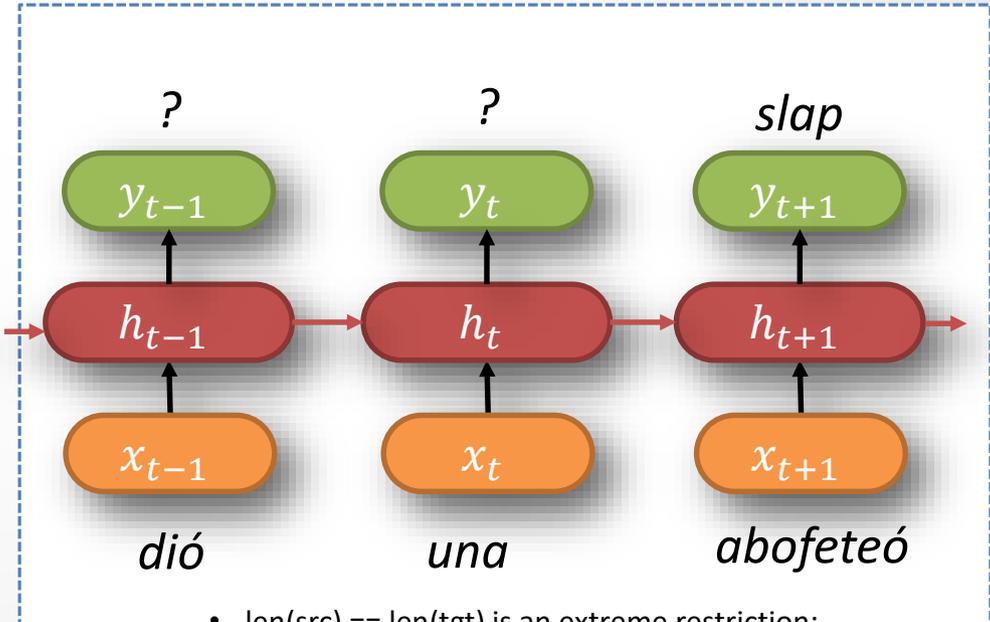
In the absence of any hierarchical structure (such as from a parser), there aren't a lot of options that are invariant to the choice of language pair.

Why not train an RNN to output a translated token from source token?

"Mary no **dió una abofeteó a la bruja verde.**" -> "Mary did not **slap the green witch.**"



Different morphology: Adj, NN order not same



- len(src) == len(tgt) is an extreme restriction:
- Mapping is not always 1:1 (e.g. many:1)

“Direct” translation

- A bilingual dictionary that aligns words across languages can be helpful, but only for certain cases.

<i>¿</i>	<i>Dónde</i>	<i>está</i>	<i>la</i>	<i>biblioteca</i>	<i>?</i>
	<i>Where</i>	<i>is</i>	<i>the</i>	<i>library</i>	<i>?</i>
	<i>Où</i>	<i>est</i>	<i>la</i>	<i>bibliothèque</i>	<i>?</i>

<i>Mi</i>	<i>nombre</i>	<i>es</i>	<i>T-bone</i>
<i>My</i>	<i>name</i>	<i>is</i>	<i>T-bone</i>
<i>Mon</i>	<i>nom</i>	<i>est</i>	<i>T-bone</i>

Difficulties in MT: ambiguity

- **Ambiguity** makes it hard to pick one translation

- Lexical: many-to-many word mappings

Paw Patte Foot Pied

- Syntactic: same token sequence, different structure

- Rick hit the Morty [with the stick]_{PP} / Rick golpeó el Morty con el palo
- Rick hit the Morty [with the stick]_{PP} / Rick golpeó el Morty que tenía el palo

- Semantic: same structure, different meanings

- I'll pick you up / {Je vais te chercher, Je vais te ramasser}

- Pragmatic: different contexts, different interpretations

- Poetry vs technical report

Difficulties in MT: typology

- Different **morphology** → difficult mappings, *e.g.*
 - Many (*polysynthetic*) vs one (*isolating*) roots per word
e.g., Yupik e.g., Cantonese
 - Many (*fusional*) vs few (*agglutinative*) features per morpheme
e.g., Russian e.g., Turkish
- Different **head-position effects in syntax**, *e.g.*
 - **SVO** vs. **SOV** vs. **VSO** (e.g. **English** vs. **Japanese** vs. **Arabic**)
 - **He listens to music** / **kare ha ongaku wo kiku**
Subject Verb Object Subject Object Verb
 - Satellite vs. nuclear-framed (e.g. **Spanish** vs. **English**)
 - **La botella salió flotando** / **The bottle floated out**

“Statistical Machine Translation”

- 1989-2014: SMT was a huge research field. All pre-neural.
- Best systems were extremely **complex** with many separately designed sub-components
- Lots of human effort & optimization for specific language pairs (e.g. SBMT for Arabic-English, PBMT for Chinese-English)
- Rule-based, hand-designed components never really were replaced in their entirety (e.g., headedness of NPs)

NMT – the breakout of Deep Learning in NLP

- Although there had been significant advances in neural language modelling and neural acoustic modelling beforehand, the NLP community remained resistant to embracing neural methods until a wildly successful attempt at neural MT in 2014. [1,2]
- NMT systems trained by a small group of engineers in a few months outperformed a state-of-the-art heavily engineered SMT system.
- Even now, NMT remains an important rationalizer for neural methods in NLP – it was one of the first showcase tasks for attention mechanisms.

¹ Devlin, J., Zbib, R., Huang, Z., Lamar, T., Schwartz, R., & Makhoul, J. (2014). Fast and Robust Neural Network Joint Models for Statistical Machine Translation. *Proc. ACL*, pp. 1370–1380.

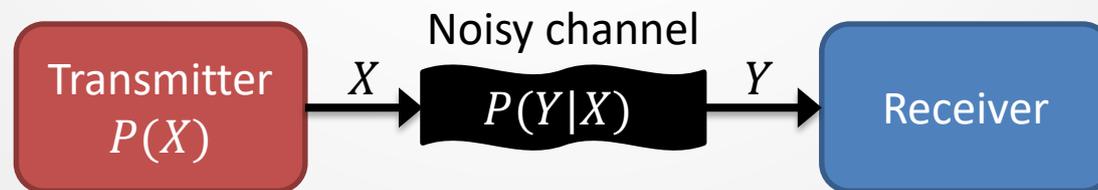
The “noisy channel” model

- Imagine that you’re given a French sentence, F , and you want to convert it to the best corresponding English sentence, E^*
 - i.e., $E^* = \operatorname{argmax}_E P(E|F)$

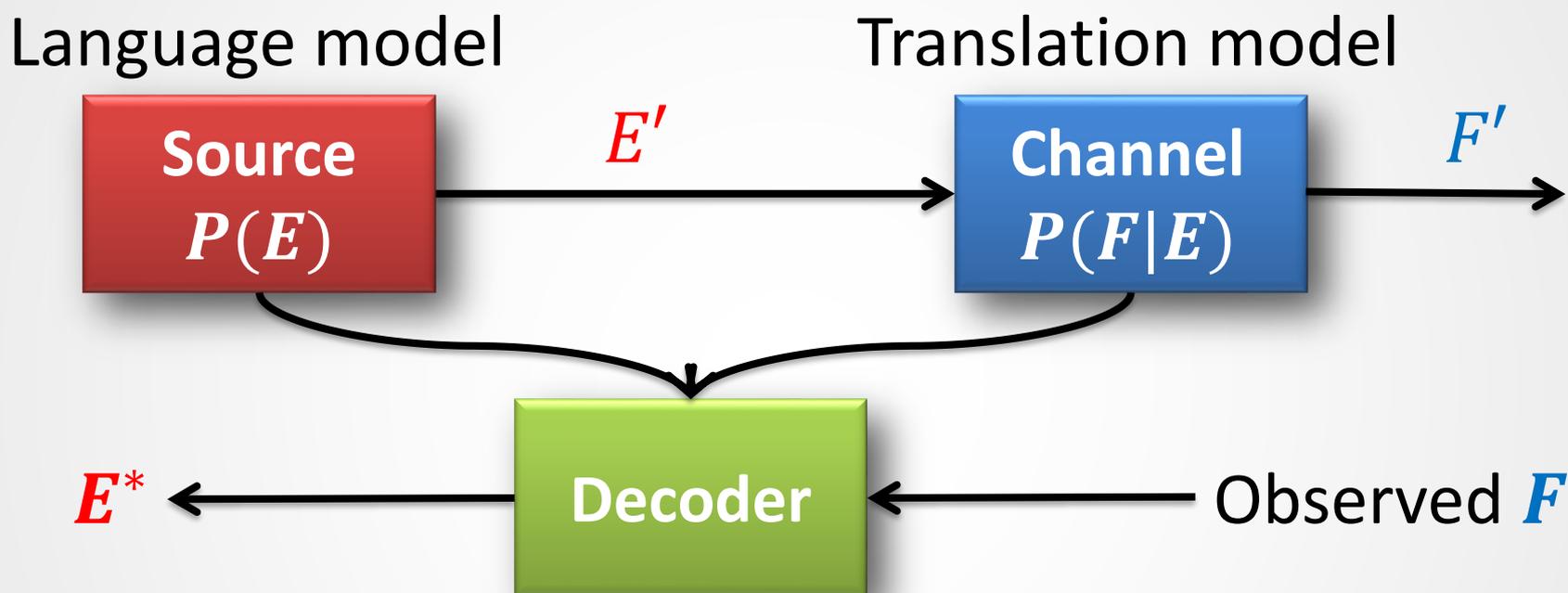
- Use Bayes’s Rule:

$$E^* = \operatorname{argmax}_E \frac{P(F|E)P(E)}{P(F)}$$

- $P(F)$ doesn’t change argmax



The “noisy channel” model



$$E^* = \operatorname{argmax}_E P(F|E)P(E)$$

How SMT uses the noisy channel

- How does SMT work?

$$E^* = \underset{E}{\operatorname{argmax}} \underbrace{P(F|E)}_{\text{Translation model}} \underbrace{P(E)}_{\text{Language model}}$$

- $P(E)$ is a **language model** (e.g., N -gram) and encodes knowledge of word order.
- $P(F|E)$ is a **word- (or phrase-)level translation model** that encodes only knowledge on an *unordered* basis.
- **Combining** these models can give us **fluency** and **consistency**, respectively.

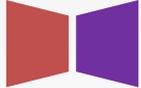
What about NMT?

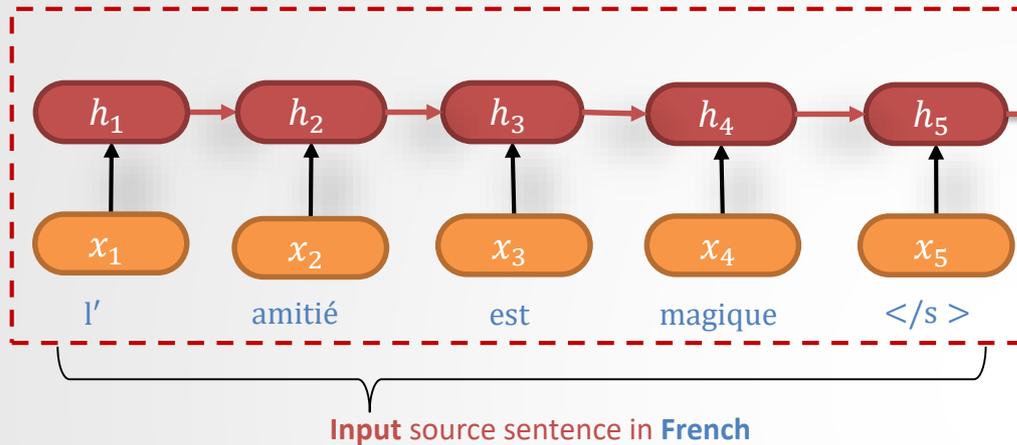
- Machine translation with neural networks
- *Usually* drops noisy channel: $E^* = \operatorname{argmax}_E P(E|F)$
 - Some NMT researchers (e.g. “Simple and effective noisy channel modeling for neural machine translation,” 2019. Yee *et al.*) use an objective inspired by the noisy channel
- No (explicit) alignments – often not even sentence-aligned
- Outperforms SMT by a large margin on poorly resourced language pairs.

Solving the alignment problem

- Recall that source and target words (or, sentences) are not always one-to-one
- SMT solution is to marginalize explicit alignments
 - $E^* = \operatorname{argmax}_E \sum_A P(F, A|E)P(E)$
- NMT uses “sequence-to-sequence (seq2seq)” encoder/decoder architectures
 - An **encoder** produces a representation of F
 - A **decoder** interprets that representation and generates an output sequence E

NMT: the seq2seq model

Encoder  Decoder

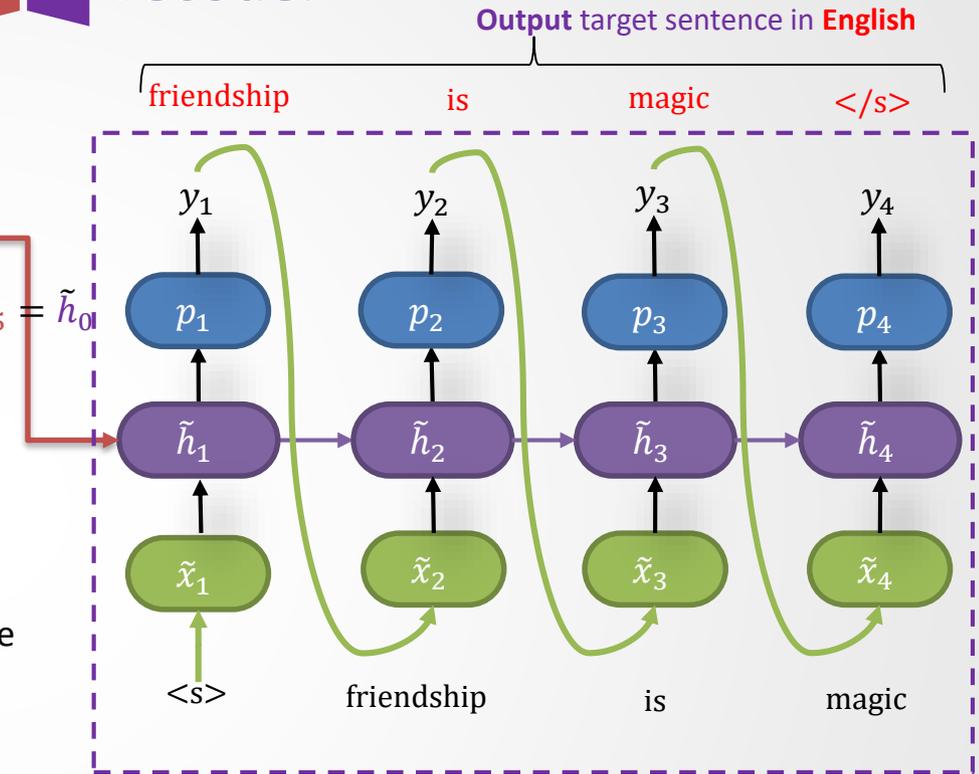


Input source sentence in French

Encoder (RNN) produces an encoding of the source (French) sentence

- The *seq2seq* model is an example of conditioned language model (LM)
- Many variants exist. The classical (vanilla) seq2seq model outlined here
- NMT directly calculates $y^* = \operatorname{argmax}_y P(y|x)$
- I.e. with our formulation:

$$E^* = \operatorname{argmax}_E P(E|F)$$



Decoder (RNN) generates target sentence (in English), conditioned on the encoding

Decoder is predicting the next word of the target sentence y

Prediction is **conditioned** on the source sentence x

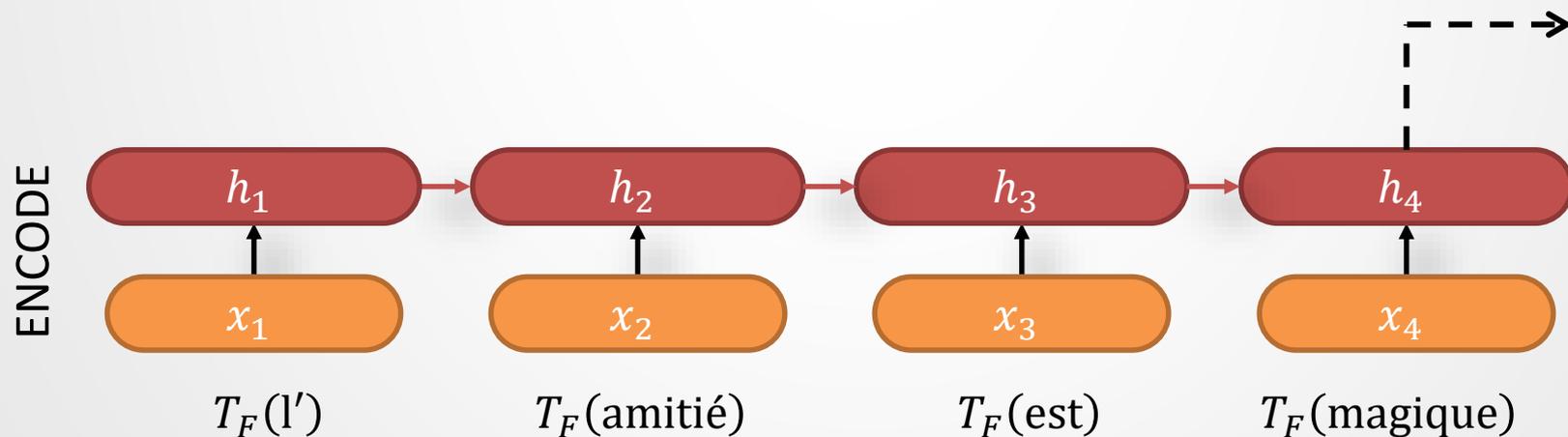
$$P(y|x) = P(y_1|x)P(y_2|y_1, x) \dots P(y_T|y_1, \dots, y_{(T-1)}, x)$$

Notation

Term	Meaning
$F_{1:S}$	Source sequence (translating from)
$E_{1:T}$	Target sequence (translating to)
$x_{1:S}$	Input to encoder RNN (i.e. source embeddings $x_s = T_F(F_s)$)
$h_{1:S}^{(\ell,n)}$	Encoder hidden states (w/ optional layer index ℓ or head n)
$\tilde{x}_{1:T}$	Input to decoder RNN
$\tilde{h}_{1:T}^{(\ell,n)}$	Decoder hidden states (w/ optional layer index ℓ or head n)
$p_{1:T}$	Decoder output token distribution parameterization $p_t = f(\tilde{h}_t)$
$y_{1:T}$	Sampled output token from decoder $y_t \sim P(y_t p_t)$
$c_{1:T}$	Attention context $c_t = \text{Attend}(\tilde{h}_t, h_{1:S}) = \sum_s \alpha_{t,s} h_s$
$e_{1:T,1:S}$	Score function output $e_{t,s} = \text{score}(\tilde{h}_t, h_s)$
$\alpha_{1:T,1:S}$	Attention weights $\alpha_{t,s} = \exp e_{t,s} / \sum_{s'} \exp e_{t,s'}$
$\tilde{z}_{1:T}^{(\ell)}$	Transformer decoder intermediate hidden states (after self-attention)

Encoder

- Encoder given source text $x = (x_1, x_2, \dots)$
 - $x_s = T_F(F_s)$ a source word embedding
- Outputs last hidden state of RNN
- Note $h_s = f(F_{1:s})$ conditions on entire source



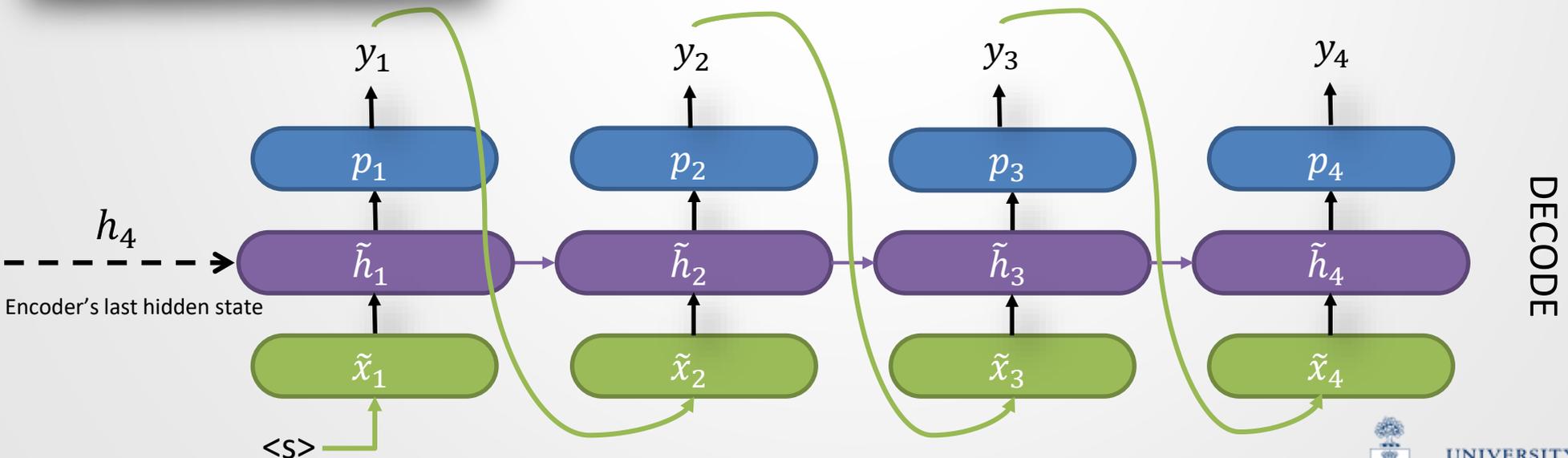
Source sentence (French): *L' amitié est magique*

Target sentence (English): *Friendship is magic* [Ground truth output]

Decoder

- **Sample** a target sentence word by word $y_t \sim P(y_t|p_t)$
- Set input to be embedding of **previously generated word** $\tilde{x}_t = T_E(y_{t-1})$
- $p_t = f(\tilde{h}_t) = f(g(\tilde{x}_t, \tilde{h}_{t-1}))$ is **deterministic**
- Base case: $\tilde{x}_1 = T_E(\langle s \rangle)$, $\tilde{h}_0 = h_S$
- $P(y_{1:T}|F_{1:S}) = \prod_t P(y_t|y_{<t}, F_{1:S}) \rightarrow$ **auto-regressive**

N.B.: Implicit $y_0 = \langle s \rangle, P(y_0) = 1$

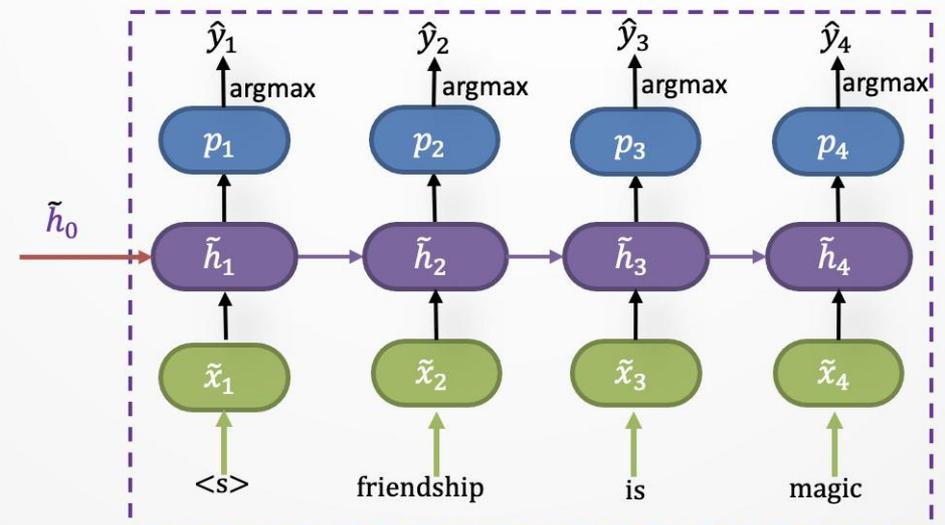


NMT: Training a MT system

- Train towards maximum likelihood estimate (MLE) against **one** translation E
- Auto-regression simplifies independence

$$\begin{aligned} \text{MLE: } \theta^* &= \operatorname{argmin}_{\theta} \mathcal{L}(\theta | E, F) & \mathcal{L}(\theta | E, F) &= -\log P_{\theta}(y = E | F) \\ & & &= -\sum_t \log P_{\theta}(y_t = E_t | E_{<t}, F_{1:s}) \end{aligned}$$

$$\mathcal{L} = -\log P(\text{friendship} | \dots) - \log P(\text{is} | \dots) - \log P(\text{magic} | \dots) - \log P(\langle /s \rangle | \dots)$$



Attention advantages

- Improves NMT **performance** significantly (reply to RNN)
- Appears to solve the **bottleneck** problem
 - Allows the decoder to look at the source sentence directly, circumventing the bottleneck
- Helps with the long-horizon (**vanishing gradient**) problem – by providing shortcut to distant states
- Makes the model (somewhat) **interpretable**
 - We can examine the attention distribution to see what the decoder was focusing on
- We get soft **alignment** for free
 - Compare w/ the ‘*word alignment*’ matrix from SMT
 - This was also often soft
 - Comes from only sentence-aligned input
 - There had already been a number of unsupervised alignment methods proposed for SMT

