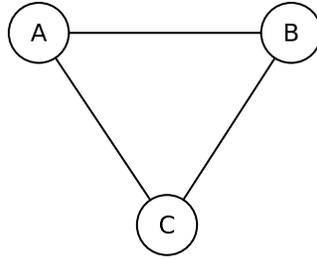


# CSC303: Practice Questions 3

Here we go again!

*Question 1:* Prove that no solution to the following bargaining network is stable



*Question 2:* The bargaining networks we have seen assign \$1 to each edge. Under this constraint we've seen that a solution  $(M, v)$  is stable iff  $\forall (A, B) \in E \setminus M : v(A) + v(B) \geq 1$ , where  $G = (V, E)$  is the underlying network.

If we allow for edges to have different weights (e.g.,  $A$  and  $B$  can split \$1.5, and  $B$  and  $C$  can split \$0.75, and so on), then does our previous theorem still capture stable solutions (i.e., solutions in which no two nodes out of the matching can make a strictly better deal among themselves)?

Justify your answer.

*Question 3:* Consider the following matching problem

$m_1 \succ_{w_1} m_2 \succ_{w_1} m_3$

$m_2 \succ_{w_2} m_1 \succ_{w_2} m_3$

$m_1 \succ_{w_3} m_2 \succ_{w_3} m_3$

$w_2 \succ_{m_1} w_1 \succ_{m_1} w_3$

$w_1 \succ_{m_2} w_2 \succ_{m_2} w_3$

$w_1 \succ_{m_3} w_2 \succ_{m_3} w_3$

- (a) Run MPDA and FPDA on the given preferences
- (b) Which solution is female-pessimal, and which is male-pessimal?

*Question 4:* If we add a new line in a subway system, then can Braess' paradox emerge? Ignore the time it requires to load/unload travelers. Is it important whether we're considering the travel time of people or subway cars? Is it important whether we consider subway cars to have finite or infinite capacity?