

62 Simplify (no proof)

(a)  $null, nil$

(b)  $null; nil$

(c)  $*nil$

(d)  $[null]$

(e)  $[*null]$

After trying the question, scroll down to the solution.

(a)  $null, nil$   
§  $nil$   
according to the identity law  $null, A = A$

(b)  $null; nil$   
§  $null$   
according to the identity law  $S; nil = S$

(c)  $*nil$   
§  $nil$   
Informally,  $*nil = nil, nil; nil, nil; nil; nil, \dots = nil, nil, nil, \dots = nil$   
Formally, the proof requires induction.

(d)  $[null]$   
§  $null$   
according to the distribution of list formation over bunch union

(e)  $[*null]$   
§  $[nil]$   
Informally,  
 $*null = nil, null, null; null, null; null; null, \dots = nil, null, null, null, \dots = nil$   
So  $[*null] = [nil]$ . Formally, the proof requires induction.