Interpreting Regression Coefficients



Auguste Rodin, The Thinker (1903)

SML201: Introduction to Data Science, Spring 2019

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Linear Regression

##				
##	Call:			
##	<pre>lm(formula = lifeExp</pre>	~ log(gdpPercap)	+ continent, dat	a = gap.1982)
##				
##	Coefficients:			
##	(Intercept)	log(gdpPercap)	continentAmerica	S
##	12.264	5.342	7.29	9
##	continentAsia	continentEurope	continentOceani	a
##	6.473	9.563	9.53	4

- An increase of 1 in log(gdpPercap) is associated with an increase of 5.3 years in predicted life expectancy
 - An increase of 1 in log(gdpPercap) is an increase by a factor of 2.7 in gdpPercap
- All other things (i.e., gdpPercapita) being equal, we'll predict a country in Europe will have life expectancy that's (9.6-7.3 = 2.3) years higher than a country in the Americas
 - i.e., we'll predict LE that's 2.3 higher for a country that has the same gdpPercapita, but is in Europe and not in the Americas

Association vs. Causation

• Does this mean that increases in GDP per capita cause increases in life expectancy?

Association vs. Causation

- Does this mean that increases in GDP per capita *cause* increases in life expectancy? Not necessarily.
 - Reverse causation: increased life expectancy causes increase in GDP per capita
 - Common cause: no natural/human-cause disaster cause both increased LE and increased GDP per capita, and are not distributed equally across continents
 - The causation goes both ways
 - It's a coincidence

Log-Odds





You pay \$2 if Biden doesn't win, and get \$13 if he does

$$\frac{p}{1-p} = \frac{2}{13}$$

$$13p = 2(1-p)$$

$$(2+13)p = 2$$

$$p = \frac{2}{2+13}$$

Probability of Biden win assuming the odds are "fair" (i.e., player and house don't stand to win on average because the odds represent the probabilities)

Out of 15 times, Biden would lose thirteen times and win twice

Logistic Regression

```
##
## Call: glm(formula = Survived ~ Sex + Age, family = binomial, data = titanic)
##
## Coefficients:
## (Intercept) Sexmale Age
## 1.11388 -2.50000 -0.00206
##
## Degrees of Freedom: 886 Total (i.e. Null); 884 Residual
## Null Deviance: 1183
## Residual Deviance: 916 AIC: 922
```

- An increase of 1 year in Age is associated with a decrease of 0.002 in the logodds of survival, all other things (i.e, sex) being the same
 - Corresponds to different things in terms of the change in probability
- All other things (i.e., age) being equal, men will have predicted log-odds of survival that are 2.5 lower
 - I.e., all other things being equal, the odds of survival for a woman are exp(2.5)=12 times higher
 - Note: not the same as the probability