

Hill Climbing

Algorithm 1 Hill Climbing

```
1: current  $\leftarrow$  a random state
2: while true do
3:   next  $\leftarrow$  get-best-neighbour(current)
4:   if cost(current)  $\leq$  cost(next) then
5:     break
6:   end if
7:   current  $\leftarrow$  next
8: end while
9: return current
```

lowest cost

local optimum

move to neighbour

Hill Climbing with Sideway Moves

Allow ≤ 100 consecutive sideway moves.

Algorithm 2 Hill Climbing with Sideway Moves

```
1: current ← a random state  
2: while true do  
3:   next ← get-best-neighbour(current)  
4:   if cost(current) < cost(next) then  
5:     strict local minimum  
6:     stop / break  
7:   end if  
8:   if cost(current) == cost(next) then  
9:     if not over sideway limit  
10:      then move to neighbour and increment sideway count.  
11:     otherwise break.  
11:   end if  
12:   move to neighbour.  
13:   reset sideway count.  
14: end while  
15: return current
```

Hill Climbing with Tabu List

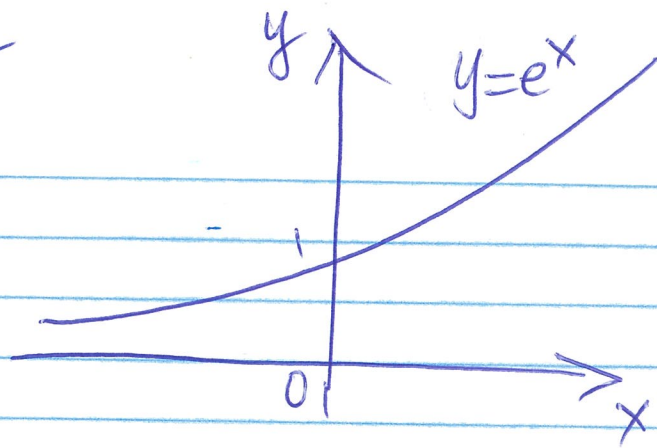
Do not go back ≤ 100 recently visited nodes.

▶ How do you keep track of the most recent nodes visited?
queue.

▶ How would you update the list? (only useful on a plateau)
If best neighbour in queue,
consider next best neighbour.
else
if queue size below limit,
add to queue.
else
add to queue, ~~##~~ remove the oldest.

Simulated Annealing

$$e^{\frac{\Delta E}{T}}$$



$\Delta E = -10$ Change $T = 100$ to $T = 10$.

$$e^{\frac{-10}{100}} = e^{-0.1} \approx 0.9$$

$$e^{\frac{-10}{10}} = e^{-1} \approx 0.36$$

$$\Delta E < 0. \quad T > 0. \quad \frac{\Delta E}{T} < 0.$$

$$T \downarrow \quad \left| \frac{\Delta E}{T} \right| \uparrow \quad \frac{\Delta E}{T} \downarrow \quad e^{\frac{\Delta E}{T}} \downarrow$$

$T = 10.$ $\Delta E = -10$ to $\Delta E = -100.$

$$e^{\frac{-10}{10}} = e^{-1} = 0.36$$

$$e^{\frac{-100}{10}} = 0.000045$$

$$\Delta E \downarrow \quad |\Delta E| \uparrow \quad \left| \frac{\Delta E}{T} \right| \uparrow \quad \frac{\Delta E}{T} \downarrow \quad e^{\frac{\Delta E}{T}} \downarrow$$

Genetic Algorithm 8-Queens.

24748552	32752411	24415124	32543213
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fitness 24	23	20	11
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prob 31%	29%	26%	14%
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parents 24748552	parents 32752411	parents 24748552	parents 24415124
32752411	24415124	32543213	32752411

child. 24748411	child. 32415124	child. 24743213	child. 24752411
↓	↓	↓	↓
24748415	32415124	54743213	247112411

- Keep track of multiple states.
- cost function: - fitness
- neighbour relation:
 - choose parents proportional to fitness
 - cross over
 - mutate

Early in the process

population is diverse, child can be very diff from parents
large steps in the space

Later on

individuals are similar, small steps.