

**Lecturer** : Christina C. Christara  
**Lectures** : Tuesday 1-3pm, Room BA 1230  
**Tutorial** : Thursday 2-3pm, Room BA 2165 (tutorials will be used for lectures)  
**Office Hours** : Tuesday 3:30-4:30pm, Room BA 4226, other hours by appointment  
**Web site** : <http://www.cs.toronto.edu/~ccc/Courses/456.html>  
**Bulletin board** : <https://bb-2022-09.teach.cs.toronto.edu/c/csc456>

### Topics to be covered

- Introduction
  - Parallel architectures, communication complexity; Speedup, efficiency
  - Simple examples: inner product, matrix-vector multiplication, total exchange
  - Performance study
- Linear systems - Direct methods
  - Gauss elimination, LU factorisation, Cholesky decomposition, back substitution
  - Banded systems; Cyclic reduction; Partitioning methods
- Linear systems - Iterative methods
  - Jacobi, Gauss Seidel, SOR, SSOR and conjugate gradient methods
  - Preconditioning; Sparse linear systems; Multicolouring
  - Asynchronous iterations
- Partial Differential Equations
  - Schur complement - domain decomposition method
  - Schwarz splitting - domain decomposition method
  - Multigrid method
  - Fast Fourier Transform methods
- Interpolation
  - Deboor decomposition

### Aims of course

Introduce the basic concepts in parallel computation and state-of-the-art scientific computing.  
 Formulate parallel numerical methods.  
 Implement the above methods on specific parallel architectures.  
 Study the performance of methods and machines.  
 Offer lots of fun.

### Prerequisites

- Elementary calculus: Taylor series, Rolle's theorem, mean value theorem, graphs of functions, continuity, convergence, de l' Hospital's rule, partial derivatives, etc.
- Numerical Linear Algebra (included in CSC336): rough knowledge of direct methods for solving linear systems; some familiarity with sparse matrices; fluency in matrix and vector manipulation.
- Interpolation (included in CSC336 or CSC436): some knowledge on interpolation.
- Partial Differential Equations: minimal knowledge on PDEs.
- Theory of Computer Algorithms: some knowledge on data structures, computer algorithms and computational complexity.
- Programming: proficiency in some conventional programming language, preferably C/C++ or FORTRAN; knowledge of MATLAB is useful but not necessary.

### Tentative marks distribution

Assignment 1	Due Tuesday, October 11	20%	<ul style="list-style-type: none"> <li>• Term tests (and final exam, if any): Calculators and this course's materials are the only aids permitted.</li> <li>• The assignments include substantial computer work.</li> <li>• Assignments are expected to look like short reports, i.e., the presentation of the subject counts too.</li> </ul>
Term test	Tuesday, October 25	30%	
Assignment 2	Due Tuesday, November 15	25%	
Assignment 3	Due Thursday, December 8	25%	

The final marks distribution will be confirmed in 3 weeks.

## References

- Christina C. Christara  
CSC456-2306 Lecture Notes on the website
- James M. Ortega  
Introduction to Parallel and Vector Solution  
of Linear Systems  
Plenum Press 1988
- Yousef Saad  
Iterative Methods for Sparse Linear Systems  
PWS 1996 or SIAM 2003  
<http://www-users.cs.umn.edu/~saad/books.html>
- Ian Foster  
Designing and Building Parallel Programs  
Addison Wesley 1995 and  
<http://www.mcs.anl.gov/dbpp>
- George Em Karniadakis and Robert M. Kirby II  
Parallel Scientific Computing in C++ and MPI  
A Seamless Approach to Parallel Algorithms and  
their Implementation  
Cambridge 2003
- J. M. Bahi, S. Contassot-Vivier and R. Couturier  
Parallel Iterative Algorithms:  
from sequential to grid computing  
Chapman & Hall/CRC 2007
- William Gropp, Ewing Lusk and Anthony Skjellum  
Using MPI: portable parallel programming  
with the message-passing interface  
MIT Press 2014  
see also  
<http://wgropp.cs.illinois.edu/usingmpiweb/>
- Michael J. Quinn  
Parallel Programming in C with MPI and OpenMP  
McGraw Hill 2004
- Jianping Zhu  
Solving Partial Differential Equations  
on Parallel Computers  
World Scientific 1994
- Ananth Grama, Anshul Gupta, George Karypis  
and Vipin Kumar  
Introduction to Parallel Computing:  
Design and Analysis of Algorithms  
Addison Wesley 2003
- Jeffrey D. Ullman  
Computational Aspects of VLSI  
Computer Science Press 1984
- Dimitri P. Bertsekas and John N. Tsitsiklis  
Parallel and Distributed Computation;  
Numerical Methods  
Prentice Hall 1989  
see also  
<https://dspace.mit.edu/handle/1721.1/3719#files-area>
- William W. Hager  
Applied Numerical Linear Algebra  
Prentice Hall 1988
- Gene H. Golub and Charles Van Loan  
Matrix computations  
John Hopkins University Press 1996
- Uri Ascher and Chen Greif  
A first course in Numerical Methods  
SIAM 2011 (e-book on library)
- Samuel D. Conte and Carl de Boor  
Elementary Numerical Analysis  
SIAM 2018 (also McGraw-Hill Inc.)
- David Kincaid and Ward Cheney  
Numerical Analysis  
Brooks/Cole
- Michael Heath  
Scientific Computing: an introductory survey  
McGraw-Hill Inc.
- Richard L. Burden and J. Douglas Faires  
Numerical Analysis  
Brooks/Cole
- John C. Strikwerda  
Finite Difference schemes and  
Partial Differential Equations  
Wadsworth and Brooks/Cole 1989
- William F. Ames  
Numerical Methods for Partial Differential Equations  
Academic Press 1977 3rd edition (or 2nd edition)  
(or Thomas Nelson & Sons)
- P. M. Prenter  
Splines and Variational Methods  
John Wiley & Sons 1975
- William L. Briggs, Van Emden Henson, Steve McCormic  
A multigrid tutorial  
SIAM 2000  
Selected papers

### **Late assignment policy**

Assignments are due the day and time posted. Assignments submitted late have a reduction of marks based on the maximum total marks the assignment could get, had it been submitted on time (and not on the total marks the assignment actually got). Each day costs 10%, to a maximum of 3 days. Assignments submitted later than 3 days after the due date do not receive any marks. Weekends and holidays count as regular days for the purpose of late assignment policy.

### **Academic integrity**

Assignments, homeworks and exams must be your own individual work and using only course materials. While students at your level are well aware of what academic integrity means, please note that violating academic integrity includes more things than presenting others' work as one's own. For example, *not taking reasonable measures to protect your work from being plagiarized by others is also a violation of academic integrity*. This is becoming particularly important now that so many things are online.

You should *never post anywhere or share with anyone* assignments, exams, questions or solutions, *even after the deadline*.

### **Additional information**

Assignments will be submitted electronically; details to be given with each assessment.

Assignments will be (highly preferably) typed in latex. A template is given in the course website. Other document processors are acceptable, as long as they produce pdf output. If an assignment is *very cleanly* handwritten and scanned *on a proper scanner* as a single pdf file, and *not photographed*, then it is also acceptable. Photographed assignments will receive 0 marks.

Exams will be handwritten and in-person.

Must get at least 30% in **each** of the assessments; can't skip any

For office hours in person, please wear a mask before entering the room. Office hours are for individual students, not for groups of students.