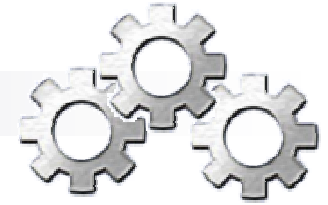


# **Deriving Intrinsic Images From Image Sequences**

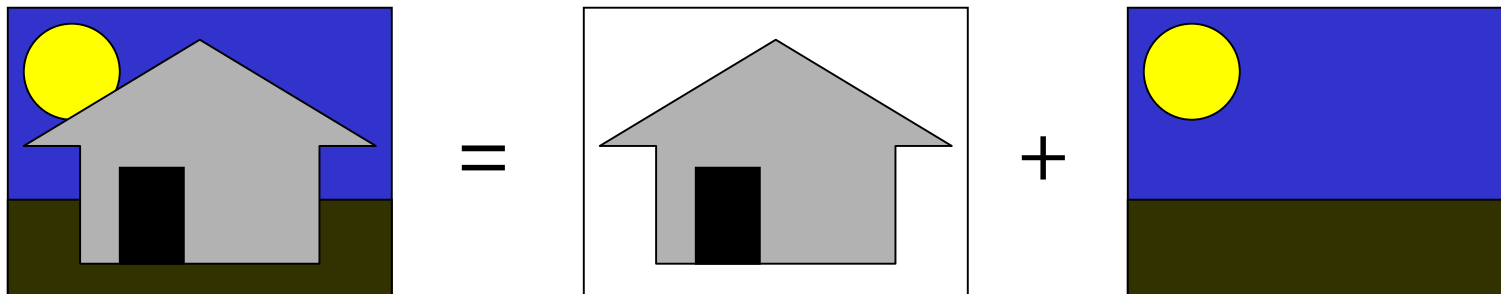
**Yair Weiss  
ICCV 2001**

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November 24, 2004**

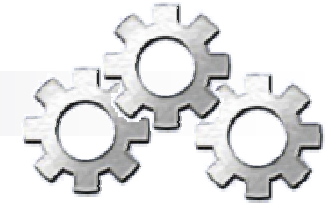


# Decomposing Images

- ⚙️ Decomposing images into layers, parts, and other types of pieces is often a useful image processing task.
- ⚙️ One of the more common decompositions is layer separation. A simple example is extracting a foreground object  $F$  from the background  $B$ .



$$I = F + B$$

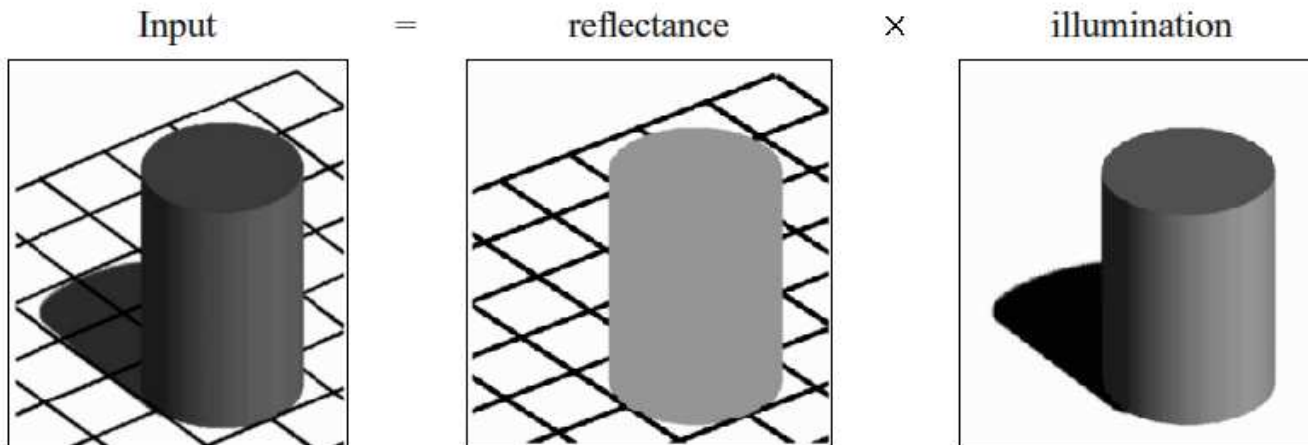


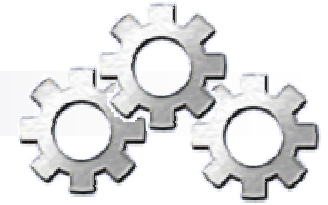
# Intrinsic Image Decomposition

- ⚙ In an intrinsic image decomposition, the goal is to decompose the input image  $I$  into a reflectance image  $R$  and an illumination image  $L$  such that:

$$I = R \times L$$

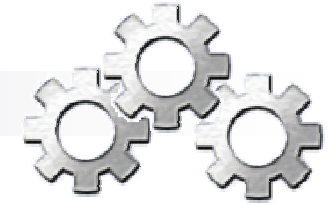
$$\log(I) = \log(R) + \log(L)$$





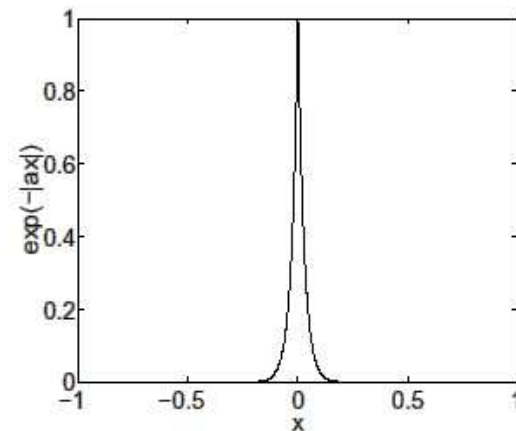
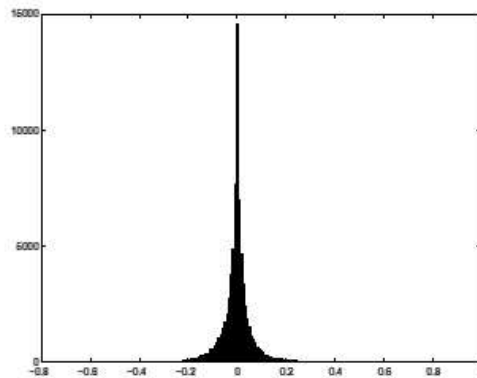
# Intrinsic Image Decomposition

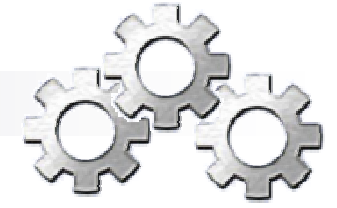
- ⚙ Why is this hard? The problem is completely ill-posed. If we set  $I=R$  and  $L=1$ , we can always obtain a perfect decomposition.
- ⚙ The part of the solution proposed in this paper is to use a set of images  $I_k$  under different illumination conditions.
- ⚙ The goal is to recover the single reflectance image  $R$  and all the illumination images  $L_k$ . This is easier, but its still ill-posed. We need some useful priors.



# Natural Image Statistics

- ⚙ The other idea in this paper is to use a prior over derivative filter outputs. Research into natural image statistics says derivative filter outputs are sparse for natural images.
- ⚙ The derivative filters used in this paper are simple horizontal and vertical derivatives:  $f_h = [-1 \ 1]$ ,  $f_v = [-1 \ 1]^T$ .





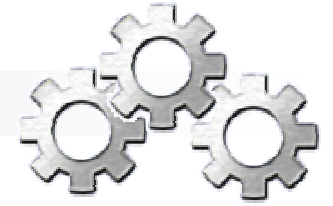
## Model

- Assume we have  $K$  images  $I_k$ . The proposed model is an IID Laplace distribution on the derivative filter outputs at each pixel  $(x, y)$  of each illumination image  $L_k$ . We can convert this into a distribution on  $R$  and  $I$ .

$$L_k^j = f^j \star L_k = f^j \star (I_k - R) = f^j \star I_k - f^j \star R = I_k^j - R^j$$

$$P(L^j) = \frac{1}{Z} \prod_{x, y, k} \exp(-\beta |L_k^j(x, y)|)$$

$$P(I^j | R^j) = \frac{1}{Z} \prod_{x, y, k} \exp(-\beta |I_k^j(x, y) - R^j(x, y)|)$$



## Solution

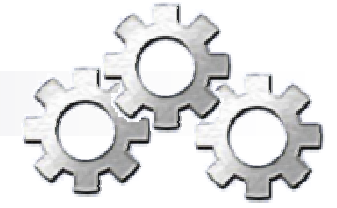
- ⚙️ **NEAT TRICK:** We can now easily get a maximum likelihood estimator for  $R^j$  since the median maximizes absolute loss:

$$\hat{R}^j(x, y) = \text{median}_k I_k^j(x, y)$$

- ⚙️ To complete the solution, we just need to invert the following over constrained system to obtain the estimated reflectance image:

$$\hat{R}^j(x, y) = f^j \star \hat{R}(x, y)$$

- ⚙️ There is a further neat trick to do this using the Fourier transform, and pseudo inverses.



**Cool, but does it work?**