# Sports Field Localization 

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## Motivation

Sports Field Localization: Have to figure out where the field and players are in 3d space in order to make measurements and generate statistics.

http://stats.nba.com/

## Motivation

## STEPHEN CURRY



## How is this done in practice?

- There are various tracking and analytics companies
- Their solutions for field localization is based mostly on hardware

http://www.stats.com/sportvu/sportvu-basketball-media/


## How is this done in practice?

Real-Time Objects Tracking and Motion Capture in Sports Events<br>US 20080192116 A1

## ABSTRACT

Non-intrusive peripheral systems and methods to track, identify various acting entities and capture the full motion of these entities in a sports event. The entities preferably include players belonging to teams. The motion capture of more than one player is implemented in real-time with image processing methods. Captured player body organ or joints location data can be used to generate a three-dimensional display of the real sporting event using computer games graphics.

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External Links: USPTO, USPTO Assignment, Espacenet

## IMAGES (16)


http://www.google.com/patents/US20080192116

## How is this done in practice?



FIG. 7a
http://www.google.com/patents/US20080192116

## How is this done in practice?


http://www.google.com/patents/US20080192116

## How is this done in practice?

- There are various tracking and analytics companies
- Their solutions for field localization is based mostly on hardware

http://pixellot.tv/


## How is this done in practice?

- There are various tracking and analytics companies
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http://www.catapultsports.com/


## Drawbacks

- Very expensive: e.g. Sportvue costs $>\$ 100000$ per season for a team
- Only rich teams can afford them
- Have to maintain all the hardware
- Still not bulletproof. Require workers to fix mistakes


## Simpler Solution?

Can we get rid of all these cameras/gps systems and just figure out where the players are by looking at a broadcast image of the field?


## Simpler Solution? YES!

Goal: Given a single broadcast image of a sport game, such as soccer, can we localize it?


- $H$ is a $3 \times 3$ invertible matrix with 8 d.f. Called a projective transformation/homography


## Homography Matrix

The matrix $H$ captures all the following transformations:

| Group | Matrix | Distortion | Invariant properties |
| :---: | :---: | :---: | :---: |
| Projective 8 dof | $\left[\begin{array}{lll}h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33}\end{array}\right]$ | $\square$ | Concurrency, collinearity, order of contact: intersection ( 1 pt contact); tangency ( 2 pt contact); inflections <br> ( 3 pt contact with line); tangent discontinuities and cusps. cross ratio (ratio of ratio of lengths). |
| Affine <br> 6 dof | $\left[\begin{array}{ccc}a_{11} & a_{12} & t_{x} \\ a_{21} & a_{22} & t_{y} \\ 0 & 0 & 1\end{array}\right]$ |  | Parallelism, ratio of areas, ratio of lengths on collinear or parallel lines (e.g. midpoints), linear combinations of vectors (e.g. centroids). The line at infinity, $l_{\infty}$. |
| Similarity <br> 4 dof | $\left[\begin{array}{ccc}s r_{11} & s r_{12} & t_{x} \\ s r_{21} & s r_{22} & t_{y} \\ 0 & 0 & 1\end{array}\right]$ | $\square$ $\square$ | Ratio of lengths, angle. The circular points, I, J (see section 2.7.3). |
| Euclidean 3 dof | $\left[\begin{array}{ccc}r_{11} & r_{12} & t_{x} \\ r_{21} & r_{22} & t_{y} \\ 0 & 0 & 1\end{array}\right]$ |  | Length, area |

Multiple View Geometry by Hartley and Zisserman

## How to find $H$ ?

- Require 4 point correspondences

- Difficulty arises in finding the 4 corresponding points


## Related Work: Academia

- Hess et al., Improved Video Registration using Non-Distinctive Local Image Features, 2007
- Gupta et al. Using Line and Ellipse Features for Rectification of Broadcast Hockey Video, 2011


Key-frame 1


Key-frame 3


Key-frame 5

Gupta et al. 2011

## Related Work: Academia

- Based on Keyframes and old school computer vision transforms (eg. SIFT)


Key-frame 1


Key-frame 3


Key-frame 5

Gupta et al. 2011

- Limitation: Depends on fixed features and also requires manual annotation of keyframes for each game and


## Can we do better?

- Can we automatically localize the field from a broadcast image?

- Lets come up with a learning approach
- Based on joint work with Sanja Fidler and Raquel Urtasun submitted to CVPR


## In case of Soccer

- Large dimensions and exposed to the elements
- Different grass textures and patterns



## This Work

- Introduce a parametrization of the field
- Incorporate prior knowledge about the soccer field as potentials in an CRF
- Find the mapping $H$ implicitly by doing inference in the CRF
- Single Camera, No key-frame, Fast Inference


## Methodology

- Let $x \in \mathcal{X}$ be random variable corresponding to a broadcast image of a soccer field.
- A soccer field is restricted by two long sides referred to as touchlines and two shorter sides referred to as goallines

- We aim to infer the position of the touchlines and the goallines in the image $x$. (Not all visible at the same time)


## Methodology



## Methodology: Parametrization

- It's very important how we parametrize this problem
- What are we trying to find?
- Vanishing Points: Where parallel lines meet in the image
- Manhattan World Assumption: Existence of three dominant orthogonal vanishing points in human-made scenes.
- In a soccer field we usually have clues for the two orthogonal vanishing point


## Methodology: Parametrization



## Methodology: Parametrization

- Create a grid by emanating rays from the vanishing points



## Methodology: Parametrization



## Methodology: Parametrization



## Methodology: Parametrization

- We parametrize the soccer field by four rays
$y=\left(y_{1}, y_{2}, y_{3}, y_{4}\right)$ on the grid
- State space: $\mathcal{Y}=\prod_{i=1}^{4}\left\{\left[y_{i, \min }^{\text {init }}, y_{i, \max }^{\text {init }}\right]\right\} \subset \mathbb{N}^{4}$



## Methodology: Parametrization


$v p_{V}$


## Inference Task

Given an image $x$ of the field, obtain the best prediction of the touchlines and the goallines by solving the following inference task:

$$
\hat{y}=\arg \max _{y \in \mathcal{Y}} w^{\top} \phi(x, y)
$$

- $\phi(x, y)$ : feature vector
- $w$ : weights to be learned from training data
- Note: $|\mathcal{Y}| \propto\left(\# \text { rays from } v p_{H}\right)^{2}\left(\# \text { rays from } v p_{V}\right)^{2}$

We find an exact solution by using branch and bound for inference. More on that later

## Model: Features

A soccer field is made up of grass and there are white marking corresponding to lines and circles with fixed dimensions


We incorporate these as features.

## Model: Features

- We need good features in the presence of noise
- Different weather and lighting conditions and shadows
- Methods based on heuristics are very fragile


## Model: Features - Semantic Segmentaition

Train a semantic segmentation network to classify image pixels to either belonging to:

1. Vertical Lines
2. Horizontal Lines
3. Middle Circle
4. Side Circles
5. Grass
6. Outside

## Model: Features - Some Examples



## Model: Features - Some Examples



## Model: Features - Some Examples



## Model: Features - Grass



## Model: Features - Lines

7 vertical line segments corresponding to $v p_{V}$ and 10 horizontal line segments corresponding to $v p_{H}$


## Model: Features - Lines

- Given $y$, need to construct a potential function that is large when the projection of each line segment in the image $x$ is close to its ground truth.
- But given $y$, where does each line segment fall in the image $x$ ?
- Use Cross Ratios: Given 4 points $A, B, C, D$ on a line, their cross ratio is given by:

$$
C R(A, B, C, D)=\frac{|A-C| \cdot|B-D|}{|B-C| \cdot|A-D|}
$$



- Cross ratios invariant under any projective transformation.


## Model: Features - Lines

- Use cross ratios to find the position of each line on the grid



## Model: Features - Lines

- For example for line $\ell_{3}$ :



## Model: Features - Circles

A cemicircle on each side of the field $C_{2}, C_{3}$ and a circle in the middle:


## Model: Features - Circles

Transformed to ellipses $C_{k}^{\prime}$ in $x$


## Model: Features - Circles

- Similar to line potentials, want potential functions that count the fraction of supporting pixels in the image $x$ for each circular shape $C_{i}$ given a hypothesis field $y$
- Unlike lines, the ellipses don't fall on the grid.
- Ellipse detection: slow and unreliable


## Model: Features - Circles

- For each circle there are unique inscribing and circumscribing rectangles aligned with the vanishing points.
- Similar to lines, we can find the quadrilaterals associated with these rectangles on the grid $\mathcal{Y}$.



## Model: Features - Efficient Computation

- We have positive features.
- Can use 3d accumulators to compute the potentials efficiently.


Schwing et al. 2012

## Branch and Bound Inference

- Inference task

$$
\hat{y}=\arg \max _{y \in \mathcal{Y}} w^{T} \phi(x, y)
$$

- Aim to do it efficiently and exactly
- Exactness comes from using branch and bound
- Efficiency comes from using integral images and tight upper bounds in branch and bound


## Branch and Bound Inference - 3 Ingredients

Suppose $Y \subset \mathcal{Y}=\prod_{i=1}^{4}\left\{\left[y_{i, \text { min }}^{\text {init }}, y_{i, \text { max }}^{\text {init }}\right]\right\}$ is a subset of parametrized fields. Branch and bound needs

- A branching mechanism that divides the set $Y$ into two disjoint subsets $Y_{1}$ and $Y_{2}$ of parametrized fields.
- A set function $\bar{f}$ such that $\bar{f}(Y) \geq \max _{y \in Y} w^{t} \phi(x, y)$.
- A priority queue $P Q$ which orders sets of parametrized fields $Y$ according to $\bar{f}$.


## Branch and Bound Inference - Optimality

In order to guarantee the optimality of the converged solution:

1. $\bar{f}(Y) \geq \max _{y \in Y} w^{t} \phi(x, y)$ for any arbitrary $Y \in \mathcal{Y}$
2. $\bar{f}(Y)=w^{t} \phi(x, y)$ when $Y=\{y\}$

Algorithm 1 branch and bound (BB) inference
put pair $(\bar{f}(\mathcal{Y}), \mathcal{Y})$ into queue and set $\hat{\mathcal{Y}}=\mathcal{Y}$
repeat
split $\hat{\mathcal{Y}}=\hat{\mathcal{Y}}_{1} \times \hat{\mathcal{Y}}_{2}$ with $\hat{\mathcal{Y}}_{1} \cap \hat{\mathcal{Y}}_{2}=\emptyset$
put pair $\left(\bar{f}\left(\hat{\mathcal{Y}}_{1}\right), \hat{\mathcal{Y}}_{1}\right)$ into queue
put pair $\left(\bar{f}\left(\hat{\mathcal{Y}}_{2}\right), \hat{\mathcal{Y}}_{2}\right)$ into queue
retrieve $\hat{\mathcal{Y}}$ having highest score
until $|\hat{\mathcal{Y}}|=1$

## Branch and Bound Inference - Branching

- How to branch a set $Y=\prod_{i=1}^{4}\left\{\left[y_{i, \min }, y_{i, \max }\right]\right\} \subset \mathcal{Y}$ into two disjoint sets $Y_{1}$ and $Y_{2}$



## Branch and Bound Inference - Branching



## Branch and Bound Inference - Branching



## Branch and Bound Inference - Bounding

- Decompose $\phi(x, y)$ into potential with strictly positive weights and those with weights that are either zero or negative:

$$
w^{T} \phi(x, y)=w_{\text {neg }}^{T} \phi_{\text {neg }}(x, y)+w_{\text {pos }}^{T} \phi_{\text {pos }}(x, y)
$$

- Construct a lower bound set function $\bar{\phi}_{i, n e g}$ and an upper bound set function $\bar{\phi}_{j, p o s}$ such that

$$
\begin{array}{rlrl}
\bar{\phi}_{i, n e g}(x, Y) & \leq \phi_{i, n e g}(x, y) & & \forall y \in Y \\
\bar{\phi}_{j, p o s}(x, Y) \geq \phi_{j, p o s}(x, y) & & \forall y \in Y
\end{array}
$$

## Branch and Bound Inference - Bounding - Grass

Grass Potential:
$\phi_{G}(x, y)=\left(\frac{\# \text { of grass pixels in } F_{y}}{\text { total } \# \text { of grass pixels }}, \frac{\# \text { of non-grass pixels in } F_{y}^{c}}{\text { total } \# \text { of non-grass pixels }}\right)$

## Branch and Bound Inference - Bounding - Grass



## Branch and Bound Inference - Bounding - Grass

Note that for any field $y \in \mathcal{Y}$, we have

$$
F_{y_{\cap}} \subset F_{y} \subset F_{y \cup}
$$

The above relation implies that

$$
\# \text { of grass pixels inside } \begin{aligned}
F_{y \cap} & \leq \# \text { of grass pixels inside } F_{y} \\
& \leq \# \text { of grass pixels inside } F_{y \cup}
\end{aligned}
$$

## Branch and Bound Inference - Bounding - Grass

Hence, we can define the upper bound for the grass potential as:

$$
\bar{\phi}_{G, p o s}(x, Y)=\phi_{G}\left(x, y_{\cup}\right)
$$

Similarly, a lower bound can be defined as:

$$
\bar{\phi}_{G, n e g}(x, Y)=\phi_{G}\left(x, y_{\cap}\right)
$$

## Branch and Bound Inference - Bounding - Lines



## Branch and Bound Inference - Bounding - Ellipses



## Learning - Structural SVM

- The outputs $y=\left(y_{1}, \ldots, y_{4}\right)$ of equation (1) are discrete random variable with complex dependencies,
- Use SSVM
- Given a dataset of ground truth training pairs $\left\{x^{(i)}, y^{(i)}\right\}_{i=1}^{N}$ we learn the parameters $w$ by solving the following optimization problem
$\min _{w} \frac{1}{2}\|w\|^{2}+\frac{C}{N} \sum_{n=1}^{N} \max _{\hat{y} \in \mathcal{Y}}\left(\Delta\left(y^{(n)}, \hat{y}\right)+w^{T} \phi\left(x^{(n)}, \hat{y}\right)-w^{T} \phi\left(x^{(n)}, y^{(n)}\right)\right)$
where $\Delta: \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}^{+} \cup\{0\}$


## Learning - Structural SVM - $\Delta$

- A hypothesis field $\hat{y}$
- $T_{\hat{y}}$ be the collection of cells in the grid $\mathcal{Y}$ corresponding to the region inside the quadrilateral defined by $\hat{y}$
- $T_{\hat{y}}^{c}$ be the complement of $T_{\hat{y}}$ in the grid $\mathcal{Y}$

$$
\Delta(y, \hat{y})=1-\frac{\# \text { of GT cells in } T_{\hat{y}}+\# \text { of cells NGT in } T_{\hat{y}}^{c}}{\text { Total number of cells in } \mathcal{Y}}
$$

## Experiments:

Datasets:

- 395 images from 20 games from World Cup 2014
- 209 train/val from 10 games
- 186 test from the 10 other games
- 4000 images from 10 NHL games
- 2000 train/val
- 2000 test

