Reasoning About Compositions of Concerns

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Abstract
In this paper we propose a framework for defining and reasoning about compositions of concerns, based on multi-valued logics. Rather than providing a small set of built-in composition operations, our framework provides a mechanism for constructing arbitrary types of composition. Our multi-valued logic model checker, χchek allows us to reason about the properties of compositions of concerns.

1 Introduction

Separation of concerns refers to the ability to identify, encapsulate and manipulate parts of software that are relevant to a particular concept, goal, task or purpose [18]. For example, sources of individual concerns can come from software engineers playing different roles in software development (e.g., UI builders and database builders), or from stakeholders with different views on the system (e.g., end users and performance engineers). An effective way to specify individual concerns is via viewpoints-based approaches [1, 15]. These approaches allow to gather and maintain (possibly inconsistent and incomplete) information gathered from multiple sources. They explicitly separate the descriptions provided by different stakeholders, and concentrate on identifying and resolving conflicts between them.

Clearly, concerns overlap and interact. To make the concept of separation of concerns truly general and usable, we need to reason about properties of the composed system, that is, reason about *compositions* of concerns. We might like to know whether all concerns from which the software is composed are *mutually consistent*, but an even more important problem is to determine whether the composed system is *correct*, that is, whether it satisfies certain agreed-upon properties. It is often impossible to assess properties of the composed system based only on descriptions of individual concerns. For example, if we describe a telephone system by describing separately the concerns of routing telephone calls and of billing for calls, then we have to compose these concerns to determine whether a subscriber would ever be billed for a call that the callee doesn't pick up.

Concerns may need to be composed in a variety of ways, depending in the roles they play in the overall system description. For example, concerns may represent parallel interacting devices, the views of different types of user (e.g., a bank manager and a teller), different levels of abstraction [17], different descriptions of the complete system (e.g., from the point of view of performance analysis and that of data management), etc. The goal of this paper is to address the problem of composing descriptions of overlapping concerns and reasoning about property preservation in the compositions.

Most specification languages have a small number of composition operators embedded in the language. These support standard types of composition for the types of entity that the language models. For example, a language based on process algebra will include sequential and parallel composition of processes, with some synchronization mechanisms. An architectural description language provides connectors for modules to interact through various mechanisms for data and control passing. Such language-specific compositions have proved essential in scaling specification languages for large systems. However, for composing separate concerns, we need a broader set of composition operations than any one language provides. This is because the set of concerns span different domains, and hence will often be described in different languages. More importantly, separate concerns usually provide different views of the same set of entities. The problem is not to connect together a set of entities, but to compose partial descriptions of each entity and of the relationships between entities.

As an alternative approach, category theory has been proposed as framework for adding compositionality to existing specification languages [16]. It has been successfully used for both algebraic [13] and temporal logic [14] specification languages. Category theory provides a rich body of theory for reasoning about structured sets of objects (in this case, specifications and their interconnections), without embedding this structure into the language. However, existing applications of category theory have provided only one type of specification interconnection, that of *refinement*. While some other types of composition can be expressed in terms of structures of refinement relations [13], this restriction has limited the application of category theory to program generation by refinement. The abstractness of category theory has also limited its appeal for practical software engineering.

Because separate concerns may interact in complex ways, we cannot hope to predict all the possible composition types

that may be useful in practice. Attempts to do so result in dozens of composition operators, which may be too hard to understand and use. In our framework, we provide a mechanism to define *arbitrary* compositions, that is, we lift composition to the first-class status in our specification/verification framework. We provide some templates for standard types of composition, and a general method for defining new compositions.

The choice of composition is determined by kind of analysis we wish to perform and by the desired level of abstraction. Suppose we wish to compose several individual descriptions of concerns, where each concern describes *some* of the attributes of each of a set of entities. Depending on the analysis, we may wish to preserve certain kinds of information in the composition:

- We may just wish to just identify which attributes the descriptions disagree about.
- We may wish to preserve information about *how many* of the descriptions agree whether a particular entity has a particular attribute (i.e., so '4 trues, 1 false' is distinct from '3 trues, 2 falses').
- We may wish to preserve information about the exact source of each piece of information (i.e. so that 'A said true, B said false' is distinct from 'A said false, B said true').
- We may wish to designate some concerns as taking priority so that their answers carry more weight in the final composition.

Because we wish to provide automated analysis of compositions of concerns, we need to formalize our compositions. We use *paraconsistent logics* as an underlying formalism, as these support reasoning in the presence of inconsistency. In particular, we have adopted multi-valued logics as a natural way of modelling levels of (dis)agreement. We took our inspiration for these from Belnap's four-valued logic [2], which had values *True*, *False*, *Both* and *Neither* (see Figure 1d). Belnap intended his logic to be used in the context of reasoning about updates to a database, where new information may be inconsistent with existing information. Rather than adding information to a single view, we are concerned with the composition of multiple views. Hence we use a family of multiple valued logics, called *quasi-boolean multi-valued logics* [3]. We argue that these provide a natural way to specify and reason about many different types of composition of separate concerns.

The rest of this paper is organized as follows: in Section 2 we describe quasi-boolean multi-valued logics and give examples of their use on several compositions. In Section 3 we briefly describe the work we have done on proving support for automated verification of the composed system w.r.t. global correctness properties expressed in CTL – a branching-time temporal logic. We also address possible interpretations of verification results. We conclude in Section 4 with a brief discussion of the overall composition/verification framework.

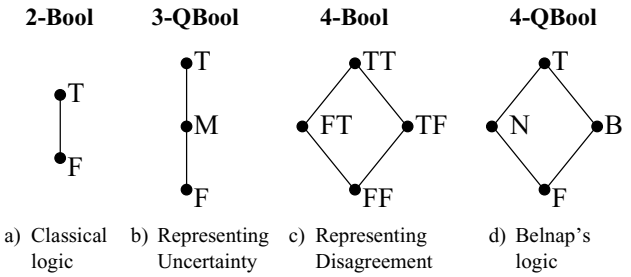

Figure 1: Four quasi-boolean logics.

2 Multi-Valued Logics

Multi-valued logics use additional truth values to represent levels of contradiction or uncertainly. For example, three-valued logic (see Figure 1b) has an additional value *Maybe* to represent uncertainty, and has been used by a number of researchers in the context of reasoning about abstractions (cf. [4, 11]).

We can define arbitrary multi-valued logics using tables to define conjunction, disjunction and negation over a finite set of truth values. However, to ensure our logics provide sensible reasoning patterns, we wish to retain many of the useful properties of classical logic, such as associativity, idempotency, distributivity, and De Morgan's laws. We therefore restrict ourselves to logics whose truth values form a lattice, with *True* at the top and *False* at the bottom, with the truth ordering $a \sqsubseteq b$ meaning that a is "less true than" b. Then conjunction and disjunction, defined as meet and join on elements of the lattice, are commutative, associative, and idempotent. Some examples appear in Figure 1. For example, for the logic **4-Bool**, we obtain:

$$FT \vee TF = FT \sqcup TF = TT$$
$$FT \wedge TF = FT \sqcap TF = FF$$

A logic is called *quasi-boolean* [3] if it has a negation operator $\neg$ with the following properties (a, b are elements of the lattice):

$$\begin{array}{rcll} \neg(a \sqcap b) & = & \neg a \sqcup \neg b & (\text{de Morgan}) \\ \neg(a \sqcup b) & = & \neg a \sqcap \neg b & \\ \neg\neg a & = & a & (\neg \text{ involution}) \\ a \sqsubseteq b & \Leftrightarrow & \neg a \sqsupseteq \neg b & (\neg \text{ antimonotonic}) \end{array}$$

For example, we can define $\neg FT = TF$ and $\neg TF = FT$, or, for the three-valued logic, $\neg M = M$. More information about these logics is available in [9]. Such logics do not necessarily preserve the law of excluded middle ($a \vee \neg a = \top$) or a law of non-contradition ($a \wedge \neg a = \bot$), and thus allow reasoning in the presence of inconsistencies and incompletenesses. Note that classical boolean logic is included in this family as a 2-valued lattice — we refer to it as **2-Bool**.

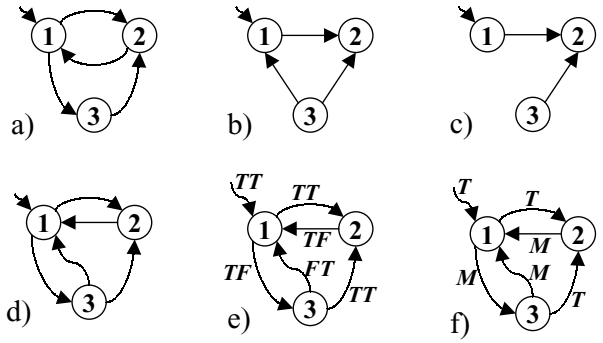

Figure 2: Two initial graphs (a)-(b) and their four compositions: (c) conjunction, (d) disjunction, (e) source preservation, (f) source abstraction.

We illustrate the role of multi-valued logics in specifying compositions using the example in Figure 2. Suppose Figure 2(a) and (b) represent views of Alice and Bob, respectively, expressed in some graph-based notation. To make the example more concrete, assume that the nodes and edges represent states and transitions of a state machine model. Alice and Bob agree on the set of states but disagree about the transitions between them. The logics used by these views, L_A and L_B, respectively, are the same – **2-Bool**, where omitted transitions are *False*, and the shown transitions are (implicitly) *True*. We can now compose Alice's and Bob's views; we start by defining L_C – the logic of the composed model. In Figure 2(c)-(d), L_C is classical logic – **2-Bool**. Now, for each $a \in L_A$, $b \in L_B$, we map (a, b) to some element of L_C. This determines the type of composition. For example, *conjunction* is a mapping **2-Bool** $\times$ **2-Bool** $\rightarrow$ **2-Bool** where (*T*, *T*) maps to *T*, and all other tuples map to *F*. The result of this merge is illustrated in Figure 2(c). *Disjunction* is a mapping where (*F*, *F*) maps to *F*, and all other tuples map to *T*. The result is given in Figure 2(d). Note that conjunction and disjunction abstract away the exact sources of information.

More interesting merges are also possible. For example, if we like to know which view contributed each edge in the merged model, we let L_C be **4-Bool**, with mappings (*T*, *T*) $\rightarrow$ *TT*, (*T*, *F*) $\rightarrow$ *TF*, etc. To denote these values on the resulting graph, we need to explicitly label the edges with values from the logic. Figure 2(e) gives an example of this type of composition. We can analyze the properties of this composition. For example, imagine we want to know whether the system can cycle between states **1** and **3**. We can express this as the query "transition(1,3) $\wedge$ transition(3,1)", which is False because $TF \wedge FT = FF$. In other words, Alice and Bob both agree that the cycle cannot occur, even though they disagree about the transitions between **1** and **3**.

Another useful type of composition identifies disagreement, but does not identify its source. In this case, we can use the logic **3-QBool**, with mappings (*T*, *T*) $\rightarrow$ *T*, (*F*, *F*) $\rightarrow$ *F*, and everything else to *M*. This composition is given in Figure 2(f). In this composition the above query cannot be answered conclusively, since $M \wedge M = M$.

As mentioned earlier, the choice of the resulting logic is usually determined by the task at hand. Furthermore, we need rules that help us determine how to interpret the results of our queries. For example, in our our last composition, the fact that the answer to the query about cycles between states **1** and **3** is answered with value *M* does not necessarily mean that the viewpoints disagree. Three-valued logic compactly encodes disagreement, but only *T* and *F* values can be trusted. Many *M* answers actually do not present disagreement [5]. On the other hand, our mapping into **4-Bool** is property-preserving: we can always correctly determine the interpretation of answers given by the merged model.

3 Multi-Valued Analysis

Although multi-valued logics provide a natural way for specifying compositions, we are mostly interested in analyzing resulting models w.r.t. preservation of desired properties. In addition, we are interested in being able to interpret results of this analysis correctly, since clearly the interpretation differs for the various types of composition performed. In this section we briefly describe the analysis we can perform if individual concerns are expressed as state machines. We describe the state machine models, the language for specifying properties and the multi-valued model-checking algorithm. This work is discussed in more detail in [12, 9, 6, 7].

In this work we assume that individual concerns are described as multi-valued finite-state machines (we call them χviews). Conventionally, a state machine model consists of a set of states, a set of transitions between states, and a set of variables whose values vary from state to state. We extend this model by associating each χview with a specific quasi-boolean logic. 'Boolean' variables now range over the values of the logic, rather than just being *True* or *False*. Transitions between states are also labeled with values from the logic. For example, in Figure 2(e), the value of (**1**,**3**) is *TF*. Figure 3 gives more realistic examples of χviews. Figure 3(a) depicts an aspect of a thermostat system that runs a heater when the temperature falls below desired. The system has one indicator (`Below`), a switch to turn it off and on (`Running`) and a variable indicating whether the heater is running (`Heat`). Figure 3(b) describes another aspect of the thermostat system – running the air conditioner. The behavior is similar, but this system handles the failure of the temperature indicator. If the temperature reading cannot be obtained in states `AC` or $\texttt{IDLE}_2$, the system transitions into state $\texttt{IDLE}_1$. Finally, Figure 3(c) contains a merged model, describing the behavior of the thermostat that can run both the heater and the air conditioner. The logic of these three models is **3-QBool**.

Since our χviews represent behavioural models, we would like to be able to ask them questions expressed in temporal logic. The language we chose for it is χCTL [9] – an extension of branching-time temporal logic CTL [10][1]. Properties

[1] A multi-valued extension of LTL is also available and described in [8].

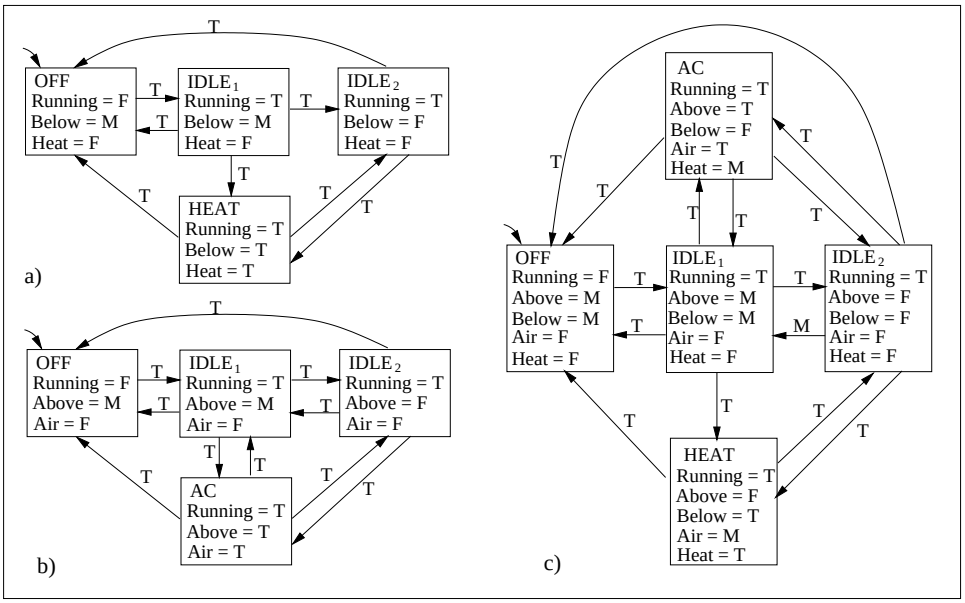

Figure 3: Models of the thermostat. (a) Heat only; (b) AC only; (c) combined model.

expressed in CTL are evaluated on a tree of infinite computations produced from the finite-state machine. The syntax of χCTL is the same as that of CTL:

1. Every atomic proposition $a \in A$ is a CTL formula.
2. If φ and ψ are CTL formulas, then so are $\neg\varphi$, $\varphi \wedge \psi$, $\varphi \vee \psi$, $EX\varphi$, $AX\varphi$, $EF\varphi$, $AF\varphi$, $E[\varphi U \psi]$, $A[\varphi U \psi]$, $EG(\varphi)$, $AG(\varphi)$.

The temporal quantifiers have two components: A and E quantify over paths, while X, F, U and G indicate "next state", "eventually (*future*)", "until", and "always (*globally*)", respectively. Hence, $AX\varphi$ is *True* in state s if φ is *True* in the *next* state on *all paths* from s. $E[\varphi U \psi]$ is *True* in state s if *there exists* a path from s on which φ is *True* at every step *until* ψ becomes *True*. In χCTL, the semantics of quantification is different – "exists" is evaluated as a disjunction over paths, and "forall" is evaluated as a conjunction. For example, some properties of the thermostat system are:

1. Can the system transition into $\texttt{IDLE}_1$ from everywhere?
   $AG\ EX\ \texttt{IDLE}_1$
2. Is the heat on only if air conditioning is off?
   $AG\ (\texttt{Heat} \leftrightarrow \texttt{Air})$
3. Can heat be on when the temperature is above desired?
   $AG\ (\texttt{Above} \rightarrow \neg\texttt{Heat})$

Note that the last two properties can only be expressed on a combined model. [9] gives the full semantics of χCTL.

We have developed a symbolic multi-valued χCTL model checker χchek [9, 6, 7] for analyzing χviews. The model checker takes as input a χview, including the definition of its quasi-boolean logic, and a temporal logic property expressed in χCTL, and returns a value from the logic representing the value that the χCTL property takes in the initial state of the χview, together with a counter-example, if applicable.

Once the answer is received, we would like to know its meaning w.r.t. individual descriptions of concerns. Suppose the model-checker returned *F* as the value of the first property of the thermostat. Does this mean that the property is *False* in both viewpoints? at least one viewpoint? cannot be concluded? To understand the meaning of some of the compositions, let us turn our attention back to the graphs in Figure 2. Under the "conjunction" composition (Figure 2(c)), we have a path in the composed graph only if this path is present in both of the initial graphs (that is why this composition is often called "conservative"). Thus, if an existential property is *True* in the composition, it is also *True* in each individual model. For example, "state **2** is reachable from the initial state", expressed in CTL as EF **2**, is *True* in the combined model and in the original models. However, if an existential property is *False* in the composition, in general no information is known about it in the original models. Universally-quantified properties have the opposite effect: *False*s are preserved, whereas *True*s are not. It is interesting to note that if both viewpoints agree on values of a property, it is not guaranteed that the property will have the same value in the combined model. For example, an existential property is *True* in a combined model only if individual viewpoints agree that it is *True* AND agree on the individual path that makes this property *True*. Otherwise no information about the value of the property in the combined model can be deduced.

The "disjunction" composition (Figure 2(d)) is often called "optimistic", because it includes all paths of the individual viewpoints (and possibly a few others). Thus, if a universally-quantified property is *True* on the combined model, it is *True* on each viewpoint. For example, "only states **2** and **3** are immediately reachable from **1**", formalized as AX (**2** $\vee$ **3**), is *True* in the graph in Figure 2(d), and also in

the individual graphs. Further, if an existentially-quantified property is *False* in the combined model, it is *False* in each viewpoint.

The "abstraction" composition (Figure 2(f)) ends up preserving more properties than either "optimistic" or "pessimistic" compositions. If a property, either universal or existential, is *True* (*False*) in a combined system, it is *True* (*False*) on both individual systems. Consider, for example, a property "**2** is immediately reachable from **1**", expressed in CTL as EX **2**. This property is *False* in the combined model, and in graphs in Figure 2(a)-(b). However, no information is known when a property yields *M* on the combined model. Furthermore, the more concerns we compose, and the more interesting properties we want to verify, the more often will the answers be *M*. When most properties of interest are *M* in the combined model, then the abstraction is not effective, and other means of combining information should be explored. For example, we can go from a relatively compact 3-valued logic to more-valued logics, e.g. **4-Bool**, **8-Bool**, etc., which preserve the source of individual information and thus preserve more properties.

4 Discussion and Conclusion

In this paper we argued for the need to bring composition operators into first-class status for reasoning about concerns. Multi-valued logics can form the basis of such a language of compositions because they allow specification of all classical compositions and many other interesting compositions. Furthermore, over the past year we have developed an automated verification engine for checking multi-valued systems against temporal properties. This engine, χchek, is part of χbel[2] (Multi-Valued **B**elief **E**xploration **L**ogics) framework for merging and reasoning about individual concerns. The framework additionally includes support for merging namespaces of individual viewpoint descriptions, a few templates for the merge, and strategies for using the results of the analysis for negotiation.

Although χbel provides interpretations for several common compositions, more compositions will clearly be necessary. New compositions (merges) can be defined easily; however, the interpretation of property preservation is somewhat more difficult, and often requires considerable formal methods expertise. We are maintaining a library of useful compositions, and as our experience with the framework matures, the library will grow. The use of all compositions from the library is simple, and does not require formal methods expertise. The library will also include some domain-specific compositions, e.g., those occurring in the analysis of feature interactions in telecom, or reasoning about high assurance systems.

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[2] pronounced "Ki-bel"

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