Steps to a Recursive Predicate

1. Predicate Form:

- Choose a predicate name appropriate for something that is true or false.
- · Choose mnemonic argument names.
- 2. **Spec:** Write the specification in this form: pred succeeds iff ...

3. Base Cases:

- When is it so easy to tell the predicate is true that you needn't check any further?
- Write these base case(s).

4. Recursive Cases:

- When it's not trivial, what do you need to know is true before you can be sure the predicate is true?
- This is the antecedent of your rule.
- There may be several non-trivial cases, each needing a rule.

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Lists in Prolog

Two ways to describe a list:

1 [elements-with-commas]

```
Egs: [a, b, c]
[]
[a, [b, c], d, [], e]
[a, X, c, d]
```

2. [first | rest] (rest must be a list)

```
Egs: [a | [b, c]]
[a | Rest]
```

Question: Why use the second form with I?

Unifying Lists

```
?- [X, Y, Z] = [john, likes, fish].
?- [cat] = [X|Y].
?- [1,2] = [X|Y].
?- [a,b,c] = [X|Y].
?- [a,b|Z]=[X|Y].
?- [X,abc,Y]=[X,abc|Y].
```

?- [[the|Y]|Z] = [[X,hare] | [is,here]].

Let's Write Some List Predicates

```
1. member(X, List).
```

append(List, List2, Result).

swapFirstTwo(List, List2).

4. length(List).

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List Membership

```
Definition of member...
```

```
?- member(a,[a,b]).
Yes
?- member(a,[b,c]).
No
?- member(X,[a,b,c]).
X=a;
X=b;
X=c;
No
?- member(a,[c,b,X]).
X=a;
No
?- member(X,Y).
X=_G72, Y=[_G72|_G73];
X=_G76, Y=[_G72,_G74|_G76];
X=_G76, Y=[_G72,_G74,_G76|_G77];
...
```

Lazy evaluation of potentially infinite data structures

Trace of Member

```
[trace] ?- member(c,[a,b,c,d]).

Call: (7) lists:member(c, [a, b, c, d]) ? creep

Call: (8) lists:member(c, [b, c, d]) ? creep

Call: (9) lists:member(c, [c, d]) ? creep

Exit: (9) lists:member(c, [c, d]) ? creep

Exit: (8) lists:member(c, [b, c, d]) ? creep

Exit: (7) lists:member(c, [a, b, c, d]) ? creep

Yes
```

Append - More than "appending"

Definition of append

Append (cont.)

```
## Append (Cont.)

?-append(X,Y,[a,b].

X=[],Y=[a,b];

X=[a],Y=[b];

X=[a,b],Y=[];

No

Generate lists:
?-append(X,[b],Z).

X=[1,Z=[b];

X=[.G98],Z=[.G98,b];

X=[.G98,G102],Z=[.G98,G102,b];

...

Trace:

[trace] ?-append([a,b,c],[p,q,r],L).

(cal: (?) lists:append([b,c],[p,q,r],(426)? creep
(cal: (8) lists:append([c],[p,q,r],(426)? creep
(cal: (10) lists:append([c],[p,q,r],(426)? creep
(cal: (10) lists:append([c],[p,q,r],(426)? creep
Exit: (10) lists:append([c],[p,q,r],(2432)? creep
Exit: (9) lists:append([c],[p,q,r],[c,p,q,r])? creep
Exit: (9) lists:append([c],[p,q,r],[c,p,q,r])? creep
Exit: (10) lists:append([c],[p,q,r],[c,p,q,r])? creep
Exit: (11) lists:append([c],[p,q,r],[c,p,q,r])? creep
Exit: (11) lists:append([c],[p,q,r],[c,p,q,r])? creep

L = [a, b, c, p, q, r];

No

Try some other traces!
```

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Computing the Length of a List

Trace of Length:

Accessing More Than One Initial Element

Definition of length...

```
?- length([a,b,c],L).
L = 3
?- length([],L).
L = 0
?- length(X,3).
X = [_G66,_G68,_G70]
?- length(X,0).
X = []
NOTE: Use built-in length function!!
```

Observe why this doesn't work!

```
xlength([],0).
xlength([_|Y],N) :- xlength(Y,N-1).
[trace] ?- xlength([a,b,c,d],X).
  Call: (7) xlength([a, b, c, d], _G296) ? creep
  Call: (8) xlength([b, c, d], _G296-1) ? creep
  Call: (9) xlength([c, d], _G296-1-1) ? creep
  Call: (10) xlength([d], _G296-1-1-1) ? creep
  Call: (11) xlength([], _G296-1-1-1-1) ? creep
  Fail: (11) xlength([], _G296-1-1-1-1) ? creep
  Fail: (10) xlength([d], _G296-1-1-1) ? creep
  Fail: (9) xlength([c, d], _G296-1-1) ? creep
  Fail: (8) xlength([b, c, d], _G296-1) ? creep
  Fail: (7) xlength([a, b, c, d], _G296) ? creep
```

But this does work

Yes

```
mylength([],0).
mylength([_|Y],N) := mylength2(Y,M), N is M+1.
[trace] ?- mylength([a,b,c,d],X).
   Call: (7) mylength([a, b, c, d], _G296) ? creep
   Call: (8) mylength([b, c, d], _L206) ? creep
   Call: (9) mylength([c, d], _L225) ? creep
   Call: (10) mylength([d], _L244) ? creep
   Call: (11) mylength([], _L263) ? creep
   Exit: (11) mylength([], 0) ? creep
  Call: (11) _L244 is O+1 ? creep
^ Exit: (11) 1 is 0+1 ? creep
   Exit: (10) mylength([d], 1) ? creep
  Call: (10) L225 is 1+1 ? creep
^ Exit: (10) 2 is 1+1 ? creep
   Exit: (9) mylength([c, d], 2) ? creep
^ Call: (9) L206 is 2+1 ? creep
^ Exit: (9) 3 is 2+1 ? creep
   Exit: (8) mylength([b, c, d], 3) ? creep
^ Call: (8) _G296 is 3+1 ? creep
^ Exit: (8) 4 is 3+1 ? creep
  Exit: (7) mylength([a, b, c, d], 4) ? creep
X = 4
```

Trace of Length (cont)

Definition of swap_first_two...

```
?- swap_first_two([a,b], [b,a]).
?- swap_first_two([a,b], [b,c]).
?- swap_first_two([a,b,c], [b,a,c]).
?- swap_first_two([a,b,c], [b,a,d]).
?- swap_first_two([a,b,c], X).
X = [b,a,c];
?- swap_first_two([a,b|Y], X).
Y = _56, X = [b,a|_56];
?- swap_first_two([],X).
?- swap_first_two([a],X).
?- swap_first_two([a,b],X).
X = [b,a];
```

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Lists of a Specified Length

Lists of a Specified Length

Beyond Horn Logic

Arithmetic in Prolog

Definition of list_of_elem...

```
New definition of list_of_elem...
```

```
?- list_elem(X,b,3).
X = [b,b,b];
ERROR: Out of global stack
?- list_of_elem(X,Y,2).
X = [_50,_50]
Y = _50;
ERROR: Out of global stack
```

```
?- working_list_elem(X,b,3).
X = [b,b,b];
?- working_list_elem(X,Y,2).
X = [50, 50]
Y = _{50};
No
```

. So far, we have studied what is known as pure logic programming, in which all the rules are Horn.

- For some applications, however, we need to go beyond this.
- · For instance, we often need
 - Arithmetic
 - Negation
- · Fortunately, these can easily be accomodated by simple extensions to the logicprogramming framework,

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What is the result of these queries:

```
?-X = 97-65, Y = 32-0, X = Y.
?- X = 97-65, Y = 67, Z = 95-Y, X = Z.
```

To get an expression evaluated, use X is expression where expression

• is an arithmetic expression, and

• is fully instantiated.

Examples:

```
?- X is 10+17.
?- Y is 7, Z is 3+4, Y=Z.
```

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Let's Write Some Predicates with Arithmetic

- 1. factorial(N, Ans).
- 2. sumlist(List, Total).

Factorial

factorial(0,1).

factorial(X,Y) :- W is X-1, factorial(W,Z), Y is Z*X.

What are the preconditions for factorial?

factorial2(0,X,X).

factorial2(N.A.F) :-N > 0, A1 is N*A, N1 is N -1, factorial2(N1,A1,F).

What are the preconditions?

Factorial with an Accumulator:

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Arithmetic Predicates may not be Invertible

We may not be able to "invert" a predicate

sumlist([],0).

sumlist([X|Rest],Ans) :- sumlist(Rest,Partial), Ans is Partial+X.

Sum of List

Trace:

```
[trace] ?- sumlist([5,10,3],Y).
Call: (7) sumlist([5, 10, 3], _G293) ? creep
   Call: (8) sumlist([10, 3], L207) ? creep
Call: (9) sumlist([3], L227) ? creep
Call: (10) sumlist([], L227) ? creep
Ext: (10) sumlist([], 0) ? creep
^ Call: (10) L227 is 0+3 ? creep
   Exit: (10) 3 is 0+3 ? creep
    Exit: (9) sumlist([3], 3) ? creep
   Call: (9) L207 is 3+10 ? creep
^ Exit: (9) 13 is 3+10 ? creep
    Exit: (8) sumlist([10, 3], 13) ? creep
^ Call: (8) _G293 is 13+5 ? creep
^ Exit: (8) 18 is 13+5 ? creep
    Exit: (7) sumlist([5, 10, 3], 18) ? creep
```

Y = 18

Yes

That is, we may not be able to put a variable in a different place.

that involves arithmetic.

Tip: Every time you write is, you must be sure the expression will be fully instantiated. If necessary, put a precondition on your predi-

Trace of Factorial

```
Call: (7) factorial(3, _G284) ? creep
  Call: (8) L205 is 3-1 ? creep
^ Exit: (8) 2 is 3-1 ? creep
Call: (8) factorial(2, _L206) ? creep
^ Call: (9) _L224 is 2-1 ? creep
 Exit: (9) 1 is 2-1 ? creep
  Call: (9) factorial(1, _L225) ? creep
  Call: (10) L243 is 1-1 ? creep
^ Exit: (10) 0 is 1-1 ? creep
  Call: (10) factorial(0, _L244) ? creep
  Exit: (10) factorial(0, 1) ? creep
  Call: (10) _L225 is 1*1 ? creep
^ Exit: (10) 1 is 1*1 ? creep
   Exit: (9) factorial(1, 1) ? creep
  Call: (9) _L206 is 1*2 ? creep
  Exit: (9) 2 is 1*2 ? creep
  Exit: (8) factorial(2, 2) ? creep
 Call: (8) _G284 is 2*3 ? creep
^ Exit: (8) 6 is 2*3 ? creep
  Exit: (7) factorial(3, 6) ? creep
Yes
```

[trace] ?- factorial(3,X).

Trace of Factorial w/ an **Accumulator**

```
[trace] ?- factorial2(3,1,Z).
Call: (8) factorial2(3,1,_G288) ? creep
^ Call: (9) 3>0 ? creep
^ Exit: (9) 3>0 ? creep
^ Call: (9) _L206 is 3*1 ? creep
^ Exit: (9) 3 is 3*1 ? creep
^ Call: (9) _L207 is 3-1 ? creep
^ Exit: (9) 2 is 3-1 ? creep
Call: (9) factorial2(2, 3, _G288) ? creep
 ^ Call: (10) 2>0 ? creep
    Exit: (10) 2>0 ? creep
Call: (10) _1226 is 2*3 ? creep
Exit: (10) 6 is 2*3 ? creep
^ Call: (10) _L227 is 2-1 ? creep
    Exit: (10) 1 is 2-1 ? creep
Call: (10) factorial2(1, 6, G288) ? creep
    Call: (11) 1>0 ? creep
^ Exit: (11) 1>0 ? creep
   Call: (11) _L246 is 1*6 ? creep
Exit: (11) 6 is 1*6 ? creep
^ Call: (11) _L247 is 1-1 ? creep
^ Exit: (11) 0 is 1-1 ? creep
    Call: (11) factorial2(0, 6, _G288) ? creep
Exit: (11) factorial2(0, 6, 6) ? creep
    Exit: (10) factorial2(1, 6, 6) ? creep
Exit: (9) factorial2(2, 3, 6) ? creep
    Exit: (8) factorial2(3, 1, 6) ? creep
```

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Negation as Failure

No equivalent of logical not in Prolog:

- Prolog can only assert that something is true.
- Prolog cannot assert that something is false.
- Prolog can assert that the given facts and rules do not allow something to be proven true.

Negation as Failure

Assuming that something unprovable is false is called negation as failure.

(Based on a closed world assumption.)

The goal $\backslash +(G)$ succeeds whenever the goal G fails.

```
?- member(b,[a,b,c]).
 ?- \+(member(b,[a,b,c]).
?- \+(member(b,[a,c]).
```

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```
Example: Disjoint Sets
```

```
overlap(S1,S2) :- member(X,S1),member(X,S2).
disjoint(S1,S2) :- \+(overlap(S1,S2).

?- overlap([a,b,c],[c,d,e]).
Yes
?- overlap([a,b,c],[d,e,f]).
No
?- disjoint([a,b,c],[c,d,e]).
Yes
?- disjoint([a,b,c],[d,e,f]).
Yes
?- disjoint([a,b,c],X).
No %<------Not what we wanted</pre>
```

Example: Disjoint Sets (cont.)

overlap(S1,S2) :- member(X,S1),member(X,S2).

Proper use of Negation as Failure

 $\backslash +(G)$ works properly only in the following cases:

1. When G is fully instantiated at the time prolog processes the goal \+(G).

(In this case, $\backslash +(G)$ is interpreted to mean "goal G does not succeed".)

When all variables in G are unique to G, i.e., they don't appear elsewhere in the same clause.

(In this case, $\backslash +(G(X))$ is interpreted to mean "There is no value of X that will make G(X) succeed".)

Safety

Consider the following rule:

*) hates(tom, X) :- not loves(tom, X).

This may NOT be what we want, for several reasons:

The answer is infinite, since for any person p not mentioned in the database, we cannot infer loves(tom,p), so we must infer hates(tom,p).

Rule (*) is therefore said to be unsafe.

• The rule does not require X to be a person. e.g., since we cannot infer

loves(tom,hammer)
loves(tom,verbs)
loves(tom,green)
loves(tom,abc)

we must infer that tom hates all these things.

No

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Safety (Cont'd)

To avoid these problems, rules with negation should be <u>guarded</u>:

i.e., Tom hates every green vegetable that he does not love.

Here, vegetable and green are called <u>guard literals</u>. They guard against safety problems by binding X to specific values in the database.