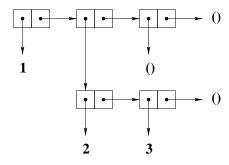
Lists

A simple but powerful general-purpose datatype. (How many datatypes have we seen so far?)

Building block: the cons cell.



Note: Sebesta uses NIL. That is LISP potation! In Scheme, we use ().

Creating lists

- Quote: '(1 (2 3) ()) => (1 (2 3) ()) or (quote (1 (2 3) ())) => (1 (2 3) ())
- list: (list 1 '(2 3) ()) => (1 (2 3) ())
- Build it, piece by piece:
 (cons 1 (cons (cons 2 (cons 3 ())))
 (cons () ())))
- Appending lists: (append 1st '(4 5)) => ((1 (2 3) () 4 5))

cons vs. list: The procedure cons actually builds pairs, and there is no reason that the cdr of a pair must be a list, as illustrated on the previous page.

The procedure list is similar to cons, except that it takes an arbitrary number of arguments and always builds a proper list.

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$$E.g.$$
, (list 'a 'b 'c) \rightarrow (a b c)

Things you should know about cons, pairs and lists

The pair or cons cell is the most fundamental of Scheme's structured object types.

A **list** is a sequence of **pairs**; each pair's cdr is the next pair in the sequence.

The cdr of the last pair in a **proper list** is the empty list. Otherwise the sequence of pairs forms an **improper list**. I.e., an empty list is a proper list, and and any pair whose cdr is a proper list is a proper list.

An improper list is printed in **dotted-pair notation** with a period (dot) preceding the final element of the list. A pair whose cdr is not a list is often called a **dotted pair**

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Useful predicates

Testing for equality

- (eq? a b): Returns #t iff a and b are the same Scheme object. (Don't use eq? with numbers!)
- (= a b): Returns #t iff a and b are numerically equal. Pre: a and b must evaluate to numbers.
- (eqv? a b): Similar to eq?, but works for numbers and characters. More expensive than eq?, however.
- (equal? a b): Returns #t iff a and b have the same structure and contents. Thus, equal? recursively tests for equality. The most expensive equality predicate.

Recommended Reading:

Dybvig §6.1, 2nd ed. (available online), or Dybvig §6.2, 3rd ed.

Equality Checking

The eq? predicate doesn't work for lists.

Why not?

- 1. (cons 'a '()) makes a new list
- 2. (cons 'a '()) makes a(nother) new list
- 3. eq? checks if its two args are the same
- 4. (eq? (cons 'a '()) (cons 'a '())) evaluates
 to () (ie, #f)

Lists are stored as pointers to the first element (car) and the rest of the list (cdr).

Symbols are stored uniquely, so eq? works on them.

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More pre-defined predicates

- (null? a): Returns #t iff a is the empty list (or #f, depending on the implementation).
- (pair? a): Returns #t iff a is a pair, i.e., a cons cell.
- (number? a): Returns #t iff a is a number.

Lots more in Dybvig §6.

Code as Data—Eval

Scheme code is simply data that is treated as code. If you build an expression, using any data processing technique, and you want to evaluate it as code, use eval:

```
(define a (+ 4 6))
a => 10
(define b '(+ 4 6))
b => (+ 4 6)
(eval b ()) => 10
```

More on this later...

Equality Checking for Lists

For lists, need a comparison procedure to check for the same **structure** in two lists. How might you write such a procedure?

- (equal? 'a 'a) evaluates to #t
- (equal? 'a 'b) evaluates to ()
- (equal? '(a) '(a)) evaluates to #t
- (equal? '((a)) '(a)) evaluates to ()

Note there is a built-in predicate procedure equal?. Play around with it!

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Recursive Procedures: Counting

```
(define (atomcount x)
  (cond ((null? x) 0)
         ((atom? x) 1)
         (else (+ (atomcount (car x))
                   (atomcount (cdr x)))))
 • (atomcount '(1 2)) \Rightarrow 2
   (atomcount '(1 (2 (3)) (5))) \Rightarrow 4
(at '(1 (2 (3)) (5)))
(+ (at 1) (at ((2 (3)) (5))))
(+ 1 (+ (at (2 (3))) (at ((5)))))
(+ 1 (+ (at 2) (at ((3)))) (+ (at (5)) (at ()))))
(+ 1 (+ (+ 1 (+ (at (3)) (at ()))) (+ (+ (at 5) (at ())) 0)))
(+ 1 (+ (+ 1 (+ (at 3) (at ())) 0)) (+ (+ 1 0) 0)))
(+ 1 (+ (+ 1 (+ (+ 1 0) 0)) (+ 1 0)))
(+ 1 (+ (+ 1 (+ 1 0)) 1))
(+ 1 (+ (+ 1 1) 1))
(+1(+21))
(+13)
```

This is called "car-cdr-recursion."

Efficiency Issues

Problem: Evaluating the same expression twice.

Example:

What can you do if there is no assignment statement?

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Efficiency Issues

Solution 2: Use a let or let* construct, that binds variables to expression results.

Efficiency Issues

Solution 1: Bind values to parameters in a helper procedure.

Note: There is a built-in max function.

Note 2: Helper procedures are an important and useful tool!

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Polymorphic and Monomorphic Functions

- Polymorphic functions can be applied to arguments of many forms
- The function length is polymorphic: it works on lists of numbers, lists of symbols, lists of lists, lists of anything
- The function square is monomorphic: it only works on numbers

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Higher-Order Procedures

Procedures as input values:

Higher-Order Procedures

Procedures as returned values:

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Built-In Higher-Order Procedures:

- map takes two arguments: a function and a list
- map builds a new list whose elements are the result of applying the function to each element of the (old) list

Higher-order Procedures: map

Example:

```
(map abs '(-1 2 -3 4)) \Rightarrow (1 2 3 4)

(map (lambda (x) (+ 1 x)) '(-1 2 -3)) \Rightarrow (0 3 -2)
```

• Actually, the built-in map can take more than two arguments:

```
(map cons '(a b c) '((1) (2) (3))) \Rightarrow ((a 1) (b 2) (c 3))
```

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What's Wrong Here??

Why doesn't this work?

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Limitations of Using eval

BUT: eval only works in the current definition of atomcount because numbers evaluate to themselves.

```
1 ]=> (+ 1 2 3)
; Value: 6

1 ]=> (cons '+ '(1 2 3))
; Value 12: (+ 1 2 3)

1 ]=> (eval (cons '+ '(1 2 3)) '())
; Value: 6
```

Using eval to Correct the Problem

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Using eval to Evaluate Expressions

Too complicated!!

Applying Procedures with apply

Higher-order Procedures: reduce

A binary \mapsto n-ary procedure.

The reduce procedure takes a binary operation and applies it right-associatively to a list of an arbitrary number of arguments.

NOTE: reduce is not equivalent to apply.

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Higher-order Procedures: reduce

```
(reduce + '(1 2 3) 0) \Rightarrow 6:

(reduce + '(1 2 3) 0)

(+ 1 (reduce + '(2 3) 0))

(+ 1 (+ 2 (reduce + '(3) 0)))

(+ 1 (+ 2 (+ 3 (reduce + '() 0))))

(+ 1 (+ 2 (+ 3 0)))

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Note: (+ 1 2 3) \Rightarrow 6

(reduce / '(24 6 2) 1) \Rightarrow 8:

(reduce / '(24 6 2) 1)

(/ 24 (reduce / '(6 2) 1))

(/ 24 (/ 6 (reduce / '(2) 1)))

(/ 24 (/ 6 (/ 2 (reduce / '() 1))))

(/ 24 (/ 6 (/ 2 1)))

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Note: (/ 24 6 2) \Rightarrow 2
```

Higher-order Procedures: reduce

Given union, which takes two lists representing sets and returns their union:

```
1 ]=> (apply union '((1 3)(2 3 4)))
; Value 21: (1 2 3 4)

1 ]=> (apply union '((1 3)(2 3)(4 5)))
; The procedure #[compound-procedure union]
; has been called with 3 arguments;
; it requires exactly 2 arguments.

1 ]=> (reduce union '((1 3)(2 3)(4 5)) '())
; Value 22: (1 2 3 4 5)
```

Question: How would you have to change reduce to be able to take intersection as its function argument?