## Functional Programming— Illustrated in Scheme

#### References:

- Dybvig, (available online and in the library)
- Sebesta Chapter 15.2-15.6, 15.9, 15.10.

Lisp slides © D. Horton 200. Scheme slides © S. Stevenson, D. Inkpen 2001. Adapted for Scheme © E. Joanis 2000, 2002. Modified and updated © S. McIlraith 2004. Additional slides use material taken from © G. Baumgartner 2001.

#### Scheme on CDF

Invoking: scheme

Exiting: (exit) or Ctrl-D Loading filename.scm: (load ''filename'')

(load ''filename.scm'')

Tracing: (trace proc\_name)

Transcript:

(transcript-on <my\_trans>) (transcript-off)

saves a transcript of a session to <my\_trans>.

Debugger:

help: -go back (read-eval-print level): (restart 1)

Ctrl-C Ctrl-C

-quit:

## **Pure Functional Languages**

Fundamental concept: application of (mathematical) functions to values

- 1. Referential transparency: The value of a function application is independent of the contex t in which it occurs (i.e., given the same parameters, it always returns the same results). Or alternatively, a language is referentially transparent if we may replace one expression with another of equal value anywhere in a program without changing the meaning of the program. This is achieved by not having side effects in programs, e.g.,
  • value of f(a,b,c) depends only on the values of
  - f, a, b and c
     It does not depend on the global state of com-
  - putation

    ⇒ all vars in function must be parameters

Main advantage: facilitates reasoning about programs and applying program transformations.

See http://en.wikipedia.org/wiki/Referential\_transparency

#### A Scheme procedure

Jumping right in

```
(define increment
    (lambda (n)
        (+ n 1)
(define (increment n)
    (+ n 1)
```

#### A call to the procedure

(increment 21)

## The Spirit of Lisp-like Languages

We shall first define a class of symbolic expressions in terms of ordered pairs and lists. Then we shall define five elementary functions and predicatend build from them by composition, conditional expressions and recursive definitions an extensive class of functions of which we shall give a number of examples. We shall then show how these functions can themselves be expressed as symbolic expression and we shall give a universal function apply that allows us to compute from the expressions for a given function its value for given arguments. Finally, we shall define some functions with functions as arguments and give some useful examples.

McCarthy, J, [1960]. Recursive functions of symbolic expressions and their computation by machine, Part I. Comm. ACM 3:4; quoted in Sethi.

## Pure Functional Languages (cont.)

- 2. The concept of assignment is not part of functional programming
  - no explicit assignment statements
  - · variables bound to values only through the association of actual parameters to formal parameters in function calls
  - function calls have no side effects
  - thus no need to consider global state
- 3. Control flow is governed by function calls and conditional expressions
  - ⇒ no iteration
  - ⇒ recursion is widely used

## Pure Functional Languages (cont.)

- 4. All storage management is implicit
  - needs garbage collection
- 5. Functions are First Class Values
  - . Can be returned as the value of an expression
  - Can be passed as an argument
  - Can be put in a data structure as a value
  - Unnamed functions exist as values

## A Functional Program

A program includes:

- 1. A set of function definitions
- 2. An expression to be evaluated

```
E.a. in Scheme:
```

```
1 ]=> (define (abs-val x)
       (if (>= x 0)
          х
          (-x))
```

; Value: abs-val

1 ]=> (abs-val (- 3 5))

;Value: 2

## Jumping Back In

#### The MIT Scheme Interface

```
werewolf 1% scheme
Scheme Microcode Version ...
1 ]=> (+ 8 3 5 16 9)
:Value: 41
1 ]=> (define increment (lambda (n) (+ n 1)))
; Value: increment
1 ]=> (increment 21)
:Value: 22
1 ]=> (load "incr")
;Loading "incr.scm" -- done
; Value: increment-list
1 ]=> (increment-list (1 32 7))
; The object 1 is not applicable.
;To continue, call RESTART with an option number:
; (RESTART 2) => Specify a procedure to use in its place.
; (RESTART 1) => Return to read-eval-print level 1.
2 error> (restart 1)
1 ]=> (increment-list '(1 32 7))
; Value 1: (2 33 8)
```

```
1 ]=> (trace increment-list)
;Unspecified return value
1 ]=> (increment-list '(1 32 7))
```

```
[Entering #[compound-procedure 2 increment-list]
Args: (1 32 7)]
[Entering #[compound-procedure 2 increment-list]
Args: (32 7)]
[Entering #[compound-procedure 2 increment-list]
Args: (7)]
[Entering #[compound-procedure 2 increment-list]
Args: ()]
```

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#### 1 ]=> (exit)

#### Formal Roots: $\lambda$ -Calculus

- Defined by Alonzo Church, a logician, in 1930s as a computational theory of recursive functions
- $\lambda$ -calculus is equivalent in computational power to Turing machines
- Recall: what's a Turing machine?
  Turing machines are abstract machines that
  emphasize computation as a series of state
  transitions driven by symbols on an input
  tape (which leads naturally to an imperative style of programming based on assignment)
- How is  $\lambda$ -calculus different?
  - $-\lambda$ -calculus emphasizes typed expressions and functions (which naturally leads to a functional style of programming).
  - No state transitions.

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## $\lambda$ -Calculus (cont.)

 $\lambda$ -calculus is a formal system for defining recursive functions and their properties.

- Expressions are called λ-expressions.
- Every λ-expression denotes a function.
- A λ-expression consists of 3 kinds of terms:

Variables: x, y, z etc

 ${\it V}$  denotes arbitrary variables

Abstractions:  $\lambda V.E$ 

where V is some variable and E is another  $\lambda$ -term.

**Applications:** ( $E1\ E2$ ) where  $E1\ \text{and}\ E2$  are  $\lambda$ -terms. Applications are sometimes called combinations.

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## $\lambda$ -Calculus (cont.)

Formal Syntax in BNF

<variable> ::= x | y | z | ...

Or more compactly

Where v is an arbitrary variable and E is an arbitrary  $\lambda$ -expression. We call  $\lambda v$  the **head** of the  $\lambda$ -expressions and E the **body**.

#### $\lambda$ -Calculus: Functional Forms

A higher-order function (functional form):

- Takes functions as parameters
- Yields a function as a result

E.g.: Given

f(x) = x + 2, g(x) = 3 \* xthen, h(x) = f(g(x)) and

h(x) is called a higher-order function.

### Types of Functional Forms:

h(x) = (3 \* x) + 2

Construction form: E.g.,

$$g(x) = x * x, h(x) = 2 * x, i(x) = x / 2$$
  
 $[g,h,i]$  (4) = (16,8,2)

Apply-to-all form: E.g,

$$h(x) = x * x$$
  
y(h, (2,3,4)) = (4,9,16)

## $\lambda$ -Calculus Is it really Turing Complete?

Can we represent the class of Turing computable functions?

Yes, we can represent:

- Boolean and conditional functions
- Numerical and arithmetic functions
- Data structures: ordered pairs, lists, etc.
- Recursion

But, doing so in  $\lambda$ -calculus is tedious;

- Need syntactic sugar to simplify task,
- $\lambda$ -calculus more suitable as an abstract model of a programming language rather than a practical programming language.

Both Turing machines and calculus are idealized, mathematical models of computatio.

# Scheme: A Functional Programming Language

1958: Lisp

1975: Scheme (revised over the years)

1980: Common Lisp ("CL")

1980s: Lisp Machines (e.g, Symbolics, TI Explorer, etc.)

Lisp, Scheme and CL contrasted on following pages.

Some features of Scheme:

- denotational semantics based on the  $\lambda$ -calculus. I.e., the meaning of programming constructs in the language is de-
- fined in terms of mathematical functions.
- lexical scoping

i.e., all free variables in a  $\lambda$ -expression are assigned values at the time that the  $\lambda$ is defined (i.e., evaluated and returned).

- arbitrary ctrl structures w/ continuations.
- functions as first-class values
- automatic garbage collection.

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## LISP

- Functional language developed by John Mc-Carthy in 1958.
- Semantics based on  $\lambda$ -Calculus
- All functions operate on lists or atomic symbols: (called "S-expressions")
- Only five basic functions: list functions cons, car, cdr, equal, atom and one conditional construct: cond
- Uses dynamic scoping
- Useful for list-processing applications
- Programs and data have the same syntactic form: S-expressions
- Used in Artificial Intelligence

## SCHEME

- Developed in 1975 by G. Sussman and G. Steele
- A version of LISP
- Consistent syntax, small language
- Closer to initial semantics of LISP
- Provides basic list processing tools
- Allows functions to be first class objects
- Provides support for lazy evaluation
- lexical scoping of variables

## COMMON LISP (CL)

- Implementations of LISP did not completely adhere to semantics
- Semantics redefined to match implementations
- COMMON LISP has become the standard
- Committee-designed language (1980s) to unify LISP variants
- Many defined functions
- Simple syntax, large language

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