

# The FF Planning System

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# The Fast Forward (FF) Planning System

- Was proposed by Hoffmann & Nebel (2001).
- Was the winner of the 2000 planning competition.
- Its novel elements are the following:
  - Heuristic based on *relaxed plans*.
  - Enforced Hill Climbing Used as the Search Strategy.
- Its core ideas have had substantial impact.

# The Relaxed Plan Heuristic: Basic Definitions

## Definition (STRIPS planning problem)

Let  $P = \langle \text{Init}, \text{Ops}, \text{Goal} \rangle$  be a STRIPS planning problem where:

- $\text{Init}$  is the initial state.
- $\text{Goal}$  is the goal condition.
- Each  $o \in \text{Ops}$  of the form  $o = (\text{prec}(o), \text{add}(o), \text{del}(o))$

## Definition (Delete-Relaxation)

The delete relaxation of  $P$ , denoted  $P^+$ , is a instance just like  $P$  but in which operators in  $\text{Ops}$  have an **empty** delete list.

## Definition (Relaxed Plan)

A *relaxed plan* for  $P$  is any plan for  $P^+$ .

# Computing a Relaxed Plan

For a planning state  $s$ :

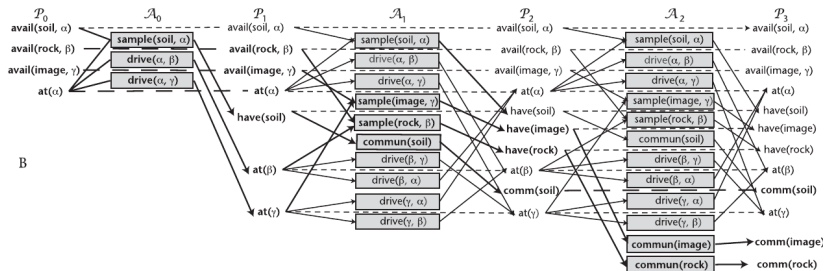
$$h_{FF}(s) = \text{“number of actions in a relaxed plan from } s\text{”}$$

The relaxed plan computed by FF:

- Is obtained using a version of Graphplan on  $P^+$ .
- Is not a shortest relaxed plan (since this is already NP-hard).

# Computing a Relaxed Plan: Intuition

For the general picture, we use Bryce & Kambhampati's figure:



Highlights of the relaxed plan extraction algorithm:

- Plan is extracted by regressing the goals (i.e. backwards)
- Iterates from the highest to the lowest level.
- Earliest achievers are always preferred.

# Computing a Relaxed Plan: Algorithm

## Extraction algorithm (Hoffmann & Nebel, 2001)

```
1: function EXTRACTPLAN(plan graph  $P_0A_0P_1 \cdots A_{n-1}P_n$ , goal  $G$ )
2:   for  $i = n \dots 1$  do
3:      $G_i \leftarrow$  goals reached at level  $i$ 
4:   end for
5:   for  $i = n \dots 1$  do
6:     for all  $g \in G_i$  not marked TRUE at time  $i$  do
7:       Find min-cost  $a \in A_{i-1}$  such that  $g \in \text{add}(A_{i-1})$ 
8:        $RP_{i-1} \leftarrow RP_{i-1} \cup \{a\}$ 
9:       for all  $f \in \text{prec}(a)$  do
10:         $G_{\text{layerof}(f)} = G_{\text{layerof}(f)} \cup \{f\}$ 
11:      end for
12:      for all  $f \in \text{add}(a)$  do
13:        mark  $f$  as TRUE at times  $i - 1$  and  $i$ .
14:      end for
15:    end for
16:  end for
17:  return RP
18: end function
```

# “Min-Cost” Actions

The “min-cost” action referred to in line 7 is the one that minimizes the following function:

$$\text{Cost}(a) = \sum_{p \in \text{Prec}(a)} \text{level}(p),$$

where  $\text{level}(p)$  is the first layer at which  $p$  appears, and  $\text{Prec}(a)$  are the preconditions of  $a$ .

Helpful actions are essential for FF's performance. Helpful actions are those that appear at the first level of the relaxed plan.

## Definition (Helpful action)

An action  $a$  of a relaxed plan from  $s$  is *helpful* iff it is a member of  $RP_0$ .

Note that helpful actions are a *subset* of the actions executable in  $s$ .

# Enforced Hill Climbing

## Enforced Hill Climbing (EHC) (Hoffmann & Nebel, 2001)

```
1: function EHC(initial state  $I$ , goal  $G$ )
2:    $plan \leftarrow EMPTY$ 
3:    $s \leftarrow I$ 
4:   while  $h(s) \neq 0$  do
5:     from  $s$ , search for  $s'$  such that  $h(s') < h(s)$ .
6:     if no such state is found then
7:       return fail
8:     end if
9:      $plan \leftarrow plan \circ$  "actions on the path to  $s'$ "
10:     $s \leftarrow s'$ 
11:  end while
12:  return  $plan$ 
13: end function
```

# Breadth-First Search for a New State

The breadth-first search (line 5) from  $s$  is implemented as follows:

```
1:  $queue \leftarrow$  empty-queue
2:  $closed \leftarrow$  {states visited by the plan}
3: PUSH(queue, {helpful successors of  $s$ })
4: while  $queue$  is not empty do
5:    $t \leftarrow pop(queue)$ 
6:   if  $t \in closed$  then
7:     continue                                 $\triangleright$  discard  $t$  and continue the iteration
8:   end if
9:   if  $h(t) < h(s)$  then
10:     $s' \leftarrow t$ 
11:    break                                     $\triangleright$  better state found, exit loop
12:   end if
13:   PUSH(queue, {helpful successors of  $s$ })
14:    $closed \leftarrow closed \cup \{t\}$ 
15: end while
```

EHC is an **incomplete** search algorithm and thus prone to failure. If EHC fails, FF falls back into *best-first search* (A search), in which the evaluation function for a state is:

$$f(s) = h_{FF}(s)$$

Note that this search is complete but greedy since the length of the plan is not considered.

**Now let's see how FF works in practice !**

Hoffmann, J., & Nebel, B. (2001). The FF planning system: Fast plan generation through heuristic search. *Journal of Artificial Intelligence Research*, 14, 253–302.