

The FF Planning System

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- Was proposed by Hoffmann & Nebel (2001).
- Was the winner of the 2000 planning competition.
- Its novel elements are the following:
  - Heuristic based on *relaxed plans*.
  - Enforced Hill Climbing Used as the Search Strategy.
- Its core ideas have had substantial impact.

The Relaxed Plan Heuristic: Basic Definitions

Definition (STRIPS planning problem)

Let  $P = \langle Init, Ops, Goal \rangle$  be a STRIPS planning problem where:

- *Init* is the initial state.
- *Goal* is the goal condition.
- Each  $o \in Ops$  of the form  $o = (prec(o), add(o), del(o))$

Definition (Delete-Relaxation)

The delete relaxation of  $P$ , denoted  $P^+$ , is a instance just like  $P$  but in which operators in  $Ops$  have an **empty** delete list.

Definition (Relaxed Plan)

A *relaxed plan* for  $P$  is any plan for  $P^+$ .

Computing a Relaxed Plan

For a planning state  $s$ :

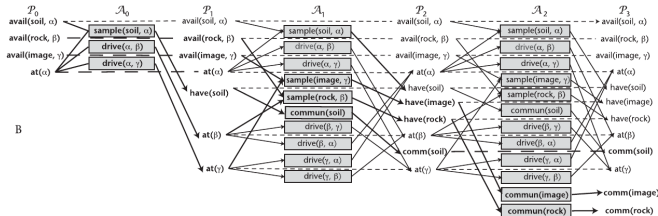
$$h_{FF}(s) = \text{“number of actions in a relaxed plan from } s\text{”}$$

The relaxed plan computed by FF:

- Is obtained using a version of Graphplan on  $P^+$ .
- Is not a shortest relaxed plan (since this is already NP-hard).

Computing a Relaxed Plan: Intuition

For the general picture, we use Bryce & Kambhampati’s figure:



Highlights of the relaxed plan extraction algorithm:

- Plan is extracted by regressing the goals (i.e. backwards)
- Iterates from the highest to the lowest level.
- Earliest achievers are always preferred.

Computing a Relaxed Plan: Algorithm

Extraction algorithm (Hoffmann & Nebel, 2001)

```

1: function EXTRACTPLAN(plan graph  $P_0A_0P_1 \dots A_{n-1}P_n$ , goal  $G$ )
2:   for  $i = n \dots 1$  do
3:      $G_i \leftarrow$  goals reached at level  $i$ 
4:   end for
5:   for  $i = n \dots 1$  do
6:     for all  $g \in G_i$  not marked TRUE at time  $i$  do
7:       Find min-cost  $a \in A_{i-1}$  such that  $g \in add(A_{i-1})$ 
8:        $RP_{i-1} \leftarrow RP_{i-1} \cup \{a\}$ 
9:       for all  $f \in prec(a)$  do
10:         $G_{layerof(f)} = G_{layerof(f)} \cup \{f\}$ 
11:       end for
12:       for all  $f \in add(a)$  do
13:        mark  $f$  as TRUE at times  $i - 1$  and  $i$ .
14:       end for
15:     end for
16:   end for
17: return RP
18: end function
    
```

## “Min-Cost” Actions

The “min-cost” action referred to in line 7 is the one that minimizes the following function:

$$\text{Cost}(a) = \sum_{p \in \text{Prec}(a)} \text{level}(p),$$

where  $\text{level}(p)$  is the first layer at which  $p$  appears, and  $\text{Prec}(a)$  are the preconditions of  $a$ .

## Helpful Actions

Helpful actions are essential for FF’s performance. Helpful actions are those that appear at the first level of the relaxed plan.

### Definition (Helpful action)

An action  $a$  of a relaxed plan from  $s$  is *helpful* iff it is a member of  $RP_0$ .

Note that helpful actions are a *subset* of the actions executable in  $s$ .

## Enforced Hill Climbing

### Enforced Hill Climbing (EHC) (Hoffmann & Nebel, 2001)

```
1: function EHC(initial state  $I$ , goal  $G$ )
2:    $plan \leftarrow \text{EMPTY}$ 
3:    $s \leftarrow I$ 
4:   while  $h(s) \neq 0$  do
5:     from  $s$ , search for  $s'$  such that  $h(s') < h(s)$ .
6:     if no such state is found then
7:       return fail
8:     end if
9:      $plan \leftarrow plan \circ \text{“actions on the path to } s'\text{”}$ 
10:     $s \leftarrow s'$ 
11:  end while
12:  return plan
13: end function
```

## Breadth-First Search for a New State

The breadth-first search (line 5) from  $s$  is implemented as follows:

```
1:  $queue \leftarrow \text{empty-queue}$ 
2:  $closed \leftarrow \{\text{states visited by the plan}\}$ 
3: PUSH( $queue, \{\text{helpful successors of } s\}$ )
4: while  $queue$  is not empty do
5:    $t \leftarrow \text{pop}(queue)$ 
6:   if  $t \in closed$  then
7:     continue ▷ discard  $t$  and continue the iteration
8:   end if
9:   if  $h(t) < h(s)$  then
10:     $s' \leftarrow t$ 
11:    break ▷ better state found, exit loop
12:  end if
13:  PUSH( $queue, \{\text{helpful successors of } s\}$ )
14:   $closed \leftarrow closed \cup \{t\}$ 
15: end while
```

## FF’s search strategy

EHC is an **incomplete** search algorithm and thus prone to failure. If EHC fails, FF falls back into *best-first search* (A search), in which the evaluation function for a state is:

$$f(s) = h_{FF}(s)$$

Note that this search is complete but greedy since the length of the plan is not considered.

**Now let’s see how FF works in practice !**

## References I

Hoffmann, J., & Nebel, B. (2001). The FF planning system: Fast plan generation through heuristic search. *Journal of Artificial Intelligence Research*, 14, 253–302.