CSC2542

# State-Space Planning 

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## Motivation

- Nearly all planning procedures are search procedures
- Different planning procedures have different search spaces
- Two examples:
- State-space planning
- Each node represents a state of the world
- A plan is a path through the space
- Plan-space planning
- Each node is a set of partially-instantiated operators, plus some constraints
- Impose more and more constraints, until we get a plan
Forward-search $\left(O, s_{0}, g\right)$

$$
s \leftarrow s_{0}
$$

$\pi \leftarrow$ the empty plan
loop
if $s$ satisfies $g$ then return $\pi$
$E \leftarrow\{a \mid a$ is a ground instance an operator in $O$, and precond $(a)$ is true in $s\}$
if $E=\emptyset$ then return failure
nondeterministically choose an action $a \in E$
$s \leftarrow \gamma(s, a)$
$\pi \leftarrow \pi \cdot a$


## Acknowledgements

Some the slides used in this course are modifications of Dana Nau's lecture slides for the textbook Automated Planning, licensed under the Creative Commons Attribution-NonCommercial-ShareAlike License:
http://creativecommons.org/licenses/by-nc-sa/2.0/
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## Outline

- State-space planning
- Forward search*
- Backward search*
- Lifting
- STRIPS
- Block-stacking
* You'll sometimes see these referred to as "progression" and "regression" in some of the automated planning literature, but these are alternative uses (some would argue misuses) relative to existing formal definitions within the RAC literature


## Properties

- Forward-search is sound
- for any plan returned by any of its nondeterministic traces, this plan is guaranteed to be a solution
- Forward-search also is complete
- if a solution exists then at least one of Forward-search's nondeterministic traces will return a solution.


## Deterministic Implementations

- Some deterministic implementations of forward search:
- breadth-first search
- depth-first search
- best-first search (e.g., $A^{*}$
- greedy search
- Breadth-first and best-first search are sound and complete
- But they usually aren't practical, requiring too much memory
- Memory requirement is exponential in the length of the solution
- In practice, more likely to use depth-first search or greedy search
- Worst-case memory requirement is linear in the length of the solution
- In general, sound but not complete
- But classical planning has only finitely many states
- Thus, can make depth-first search complete by doing cycle-checking


## Backward Search

- For forward search, we started at the initial state and computed state transitions
- new state $=\gamma(s, a)$
- For backward search, we start at the goal and compute inverse state transitions
- new set of subgoals $=\gamma^{-1}(g, a)$
- To define $\gamma^{-1}(g, a)$, must first define relevance:
- An action $a$ is relevant for a goal $g$ if
- a makes at least one of $g$ 's literals true

$$
\text { - } g \cap \operatorname{effects}(a) \neq \varnothing
$$

- a does not make any of g's literals false

$$
\text { - } g^{+} \cap \operatorname{effects}^{-}(a)=\varnothing \text { and } g^{-} \cap \operatorname{effects}^{+}(a)=\varnothing
$$

```
Backward-search(O, s0,g)
    \pi}\leftarrow\mathrm{ the empty plan
    loop
        if so satisfies g}\mathrm{ then return }
        A\leftarrow{a|a}\mathrm{ is a ground instance of an operator in O
                and }\mp@subsup{\gamma}{}{-1}(g,a)\mathrm{ is defined}
        if }A=\emptyset\mathrm{ then return failure
        nondeterministically choose an action }a\in
        \pi}\leftarrowa.
        g\leftarrow\mp@subsup{\gamma}{}{-1}(g,a)
```



## Branching Factor of Forward Search



- Forward search can have a very large branching factor
- Can have many applicable actions that don't progress toward goal
- Why this is bad
- Deterministic implementations can waste time trying lots of irrelevant actions
- Need a good heuristic function and/or pruning procedure (This will be a focus of later discussion)


## Inverse State Transitions

- If $a$ is relevant for $g$, then
- $\gamma^{-1}(g, a)=(g$-effects $(a)) \cup$ precond $(a)$
- Otherwise $\gamma^{-1}(g, a)$ is undefined
- Example: suppose that
- $g=\{\mathrm{on}(\mathrm{b} 1, \mathrm{~b} 2)$, on(b2,b3) $\}$
- $a=\operatorname{stack}(b 1, b 2)$
- What is $\gamma^{-1}(g, a)$ ?


## Efficiency of Backward Search



- Backward search can also have a very large branching factor
- E.g., an operator o that is relevant for $g$ may have many ground instances $a_{1}, a_{2}, \ldots, a_{n}$ such that each $a_{i}^{\prime}$ s input state might be unreachable from the initial state
- As before, deterministic implementations can waste lots of time trying all of them


## Lifting



- Can reduce the branching factor of backward search if we partially instantiate the operators
- this is called lifting

$$
\mathrm{p}\left(\mathrm{a}_{1}, y\right) \stackrel{\text { foo }\left(\mathrm{a}_{1}, y\right)}{\sim} \mathrm{q}\left(\mathrm{a}_{1}\right)
$$

## The Search Space is Still Too Large

- Lifted-backward-search generates a smaller search space than Backward-search, but it still can be quite large
- Suppose actions $a, b$, and $c$ are independent, action $d$ must precede all of them, and there's no path from $s_{0}$ to d's input state
- We'll try all possible orderings of $a, b$, and $c$ before realizing there is no solution
- Plan-space planning or the use of "landmarks" can help with this problem



## Lifted Backward Search

- More complicated than Backward-search
- Have to keep track of what substitutions were performed
- But it has a much smaller branching factor

```
Lifted-backward-search \(\left(O, s_{0}, g\right)\)
    \(\pi \leftarrow\) the empty plan
    loop
        if \(s_{0}\) satisfies \(g\) then return \(\pi\)
        \(A \leftarrow\{(o, \theta) \mid o\) is a standardization of an operator in \(O\),
            \(\theta\) is an mgu for an atom of \(g\) and an atom of effects \(^{+}(o)\),
            and \(\gamma^{-1}(\theta(g), \theta(o))\) is defined \(\}\)
    if \(A=\emptyset\) then return failure
    nondeterministically choose a pair \((o, \theta) \in A\)
    \(\pi \leftarrow\) the concatenation of \(\theta(o)\) and \(\theta(\pi)\)
    \(g \leftarrow \gamma^{-1}(\theta(g), \theta(o))\)
```


## Pruning the Search Space

Pruning the search space can really help.
Two techniques we will discuss:

- Sound pruning using branch-and-bound heuristic search
- Domain customization that prunes actions and states

For now, just two examples:

- STRIPS
- Block stacking


## STRIPS

- $\pi \leftarrow$ the empty plan
- do a modified backward search from $g$
- instead of $\gamma^{-1}(s, a)$, each new set of subgoals is just precond(a)
- when you find an action that's executable in the current state, then go forward on the current search path as far as possible, executing actions and appending them to $\pi$
- repeat until all goals are satisfied


```
Ground-STRIPS(O,s,g)
    \pi}\leftarrow\mathrm{ the empty plan
    loop
            if s satisfies }g\mathrm{ then return }
            A \leftarrow \{ a \| a \text { is a ground instance of an operator in O,}
                and a is relevant for g}
            if }A=\emptyset\mathrm{ then return failure
            nondeterministically choose any action }a\in
            \mp@subsup{\pi}{}{\prime}}\leftarrow\mathrm{ Ground-STRIPS(O, s, precond(a))
            if }\mp@subsup{\pi}{}{\prime}=\mathrm{ failure then return failure
            # if we get here, then }\mp@subsup{\pi}{}{\prime}\mathrm{ achieves precond(a) from s
            s}\leftarrow\gamma(s,\mp@subsup{\pi}{}{\prime}
            ;}s\mathrm{ now satisfies precond(a)
            s}\leftarrow\gamma(s,a
            \pi\leftarrow\pi.\mp@subsup{\pi}{}{\prime}.a
```


## Quick Review of Blocks World



## The Register Assignment Problem

- State-variable formulation:

Initial state: $\{$ value $(r 1)=3$, value $(r 2)=5$, value $(r 3)=0\}$
Goal: $\quad\{$ value $(r 1)=5$, value $(r 2)=3\}$
Operator: $\quad \operatorname{assign}\left(r, v, r^{\prime}, v\right)$
precond: value $(r)=v$, value $(r)=v^{\prime}$
effects: value $(r)=v^{\prime}$

- STRIPS cannot solve this problem at all


## Domain-Specific Knowledge

- A blocks-world planning problem $P=\left(O, s_{0}, g\right)$ is solvable if $s_{0}$ and $g$ satisfy some simple consistency conditions
- $g$ should not mention any blocks not mentioned in $s_{0}$
- a block cannot be on two other blocks at once
- etc.
- Can check these in time $\mathrm{O}(n \log n)$
- If $P$ is solvable, can easily construct a solution of length $\mathrm{O}(2 m)$, where $m$ is the number of blocks
- Move all blocks to the table, then build up stacks from the bottom
- Can do this in time $\mathrm{O}(n)$
- With additional domain-specific knowledge can do even better ...


## The Sussman Anomaly



- On this problem, STRIPS can't produce an irredundant solution
- Try it and see


## How to Handle Problems like These?

## Several ways:

- Do something other than state-space search - e.g., Chapters 5-8
- Use forward or backward state-space search, with domain-specific knowledge to prune the search space
- Can solve both problems quite easily this way
- Example: block stacking using forward search


## Additional Domain-Specific Knowledge

A block $x$ needs to be moved if any of the following is true:

- s contains ontable $(x)$ and $g$ contains on $(x, y)$ - see a below
- $s$ contains on $(x, y)$ and $g$ contains ontable $(x)$ - see d below
- scontains on $(x, y)$ and $g$ contains on $(x, z)$ for some $y \neq z$ - see c below
- scontains on $(x, y)$ and $y$ needs to be moved - see e below



## Domain-Specific Algorithm

loop
if there is a clear block $x$ such that
$x$ needs to be moved and
$x$ can be moved to a place where it won't need to be moved then move $x$ to that place
else if there is a clear block $x$ such that $x$ needs to be moved then move $x$ to the table
else if the goal is satisfied then return the plan
else return failure
repeat


## Easily Solves the Sussman Anomaly

loop
if there is a clear block $x$ such that
$x$ needs to be moved and
$x$ can be moved to a place where it won't need to be moved then move $x$ to that place
else if there is a clear block $x$ such that $x$ needs to be moved then move $x$ to the table
else if the goal is satisfied then return the plar
else return failure
repeat


## Properties

The block-stacking algorithm:

- Sound, complete, guaranteed to terminate
- Runs in time $O\left(n^{3}\right)$
- Can be modified to run in time $O(n)$
- Often finds optimal (shortest) solutions
- But sometimes only near-optimal (Exercise 4.22 in the book)
(Note: PLAN LENGTH for the blocks world is NP-complete)

