CSC2542
Planning-Graph Techniques

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Administrative Announcements

- **Discussion of tutorial time**

- Email me to set up a time to meet to discuss your project in the next week. Fridays are best

- Suggested readings for next week:
    - Part III introduction of GTN
    - Chapter 9 of GTN
    - A review paper that I will post on our web page.

- Other Issues?

END of
Administrative Announcements

Acknowledgements

History

- **GraphPlan** (Blum & Furst, 1995) was the first planner to use **planning-graph techniques**

- Before GraphPlan came out, most planning researchers were working on partial order planners (plan space planners *)
    - POP, SNLP, UCPOP, etc.

- GraphPlan caused a sensation because it was so much faster

- Many subsequent planning systems have used ideas from it either directly as close decendants of GraphPlan or by using the Planning Graph representation in some guise to improve the encoding of the planning problem most notably for SAT-based planning.

* Sometimes referred to as "PSP" planners, but "PSP" used for "partial satisfaction planners", nowadays

History

But most importantly…

- GraphPlan's place in history is secured by its critical role in the development of *reachability heuristics** for heuristic search planners by approximating the search tree rooted at a given state
- Heuristic search planners have dominated the "satisficing planner" track of IPC planning competitions but SAT based planners often dominate the optimal planning track. We'll discuss why.

* *Reachability heuristics aim to estimate the cost of a plan from the current search state to a goal state. We will talk about these more shortly*
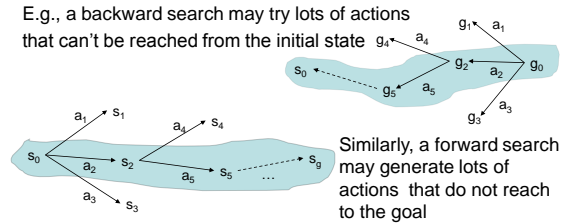
Outline

- Motivation
- The Graphplan algorithm
- Planning graphs
  - example
- Mutual exclusion
  - example (continued)
- Solution extraction
  - example (continued)
- Discussion

Motivation

- A big source of inefficiency in search algorithms is the *branching factor*
  - the number of children of each node

E.g., a backward search may try lots of actions that can't be reached from the initial state

Similarly, a forward search may generate lots of actions that do not reach to the goal

One way to reduce branching factor

- First create a *relaxed problem*
  - Remove some restrictions of the original problem
    - Want the relaxed problem to be easy to solve (polynomial time) ← **IMPORTANT**
  - The solutions to the relaxed problem will include all solutions to the original problem

- Then do a modified version of the original search
  - Restrict its search space to include only those actions that occur in solutions to the relaxed problem
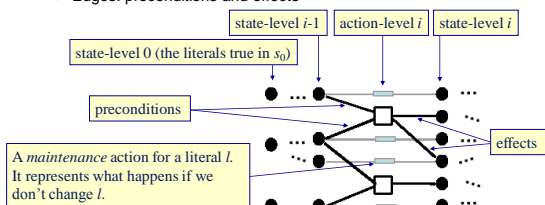
Graphplan

procedure Graphplan:

- for *k* = 0, 1, 2, …
  - *Graph Expansion:*
    - create a "planning graph" that contains *k* "levels"
  - Check whether the planning graph satisfies a necessary (but insufficient) condition for plan existence   relaxed problem
- If it does, then
  - do *Solution Extraction:*
    - backward search, modified to consider only the actions in the planning graph
    - if we find a solution, then return it

possible literals in state s_i possible actions in state s_i
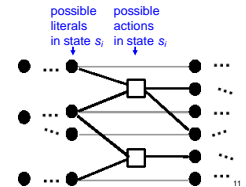
The Planning Graph

Search space for a relaxed version of the planning problem:

- Alternating layers of ground literals and actions
  - Nodes at action-level *i*: actions that might be possible to execute at time *i**
  - Nodes at state-level *i*: literals that might possibly be true at time *i*
  - Edges: preconditions and effects

state-level *i*-1   action-level *i*   state-level *i*

state-level 0 (the literals true in s_0)

preconditions

effects

A *maintenance* action for a literal *l*. It represents what happens if we don't change *l*.

* This is terminology from GNT and refers to the graph. The numbering is at odds with conventional numbering for action representations. Here, an action is possible to execute in i if it's preconditions are true in state level i-1 (as opposed to i)s. Its effects are reflected in the propositions of state level i (as opposed to i+1)

Example

- Due to Dan Weld, Univ. Washington [Weld, AIM-09]

- Suppose you want to prepare dinner as a surprise for your sweetheart (who is asleep)

  s_0 = {garbage, cleanHands, quiet}
  g = {dinner, present, ¬garbage}

Action	Preconditions	Effects
cook()	cleanHands	dinner
wrap()	quiet	present
carry()	*none*	¬garbage, ¬cleanHands
dolly()	*none*	¬garbage, ¬quiet

Also have the maintenance actions: one for each literal

Example (continued)

- state-level 0:
  {all atoms in s_0} U
    {negations of all atoms not in s_0}
- action-level 1:
  {all actions whose preconditions
    are satisfied and non-mutex in s_0}
- state-level 1:
  {all effects of all of the
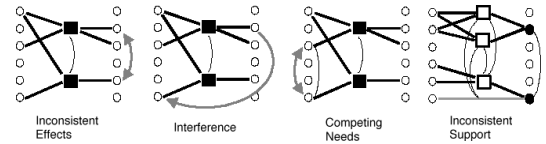   actions in action-level 1
    (including maintenance actions)}
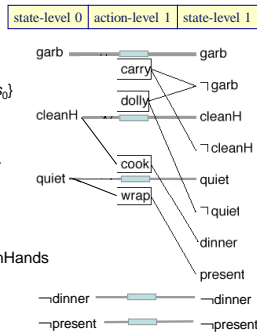
Action	Preconditions	Effects
cook()	cleanHands	dinner
wrap()	quiet	present
carry()	none	¬garbage, ¬cleanHands
dolly()	none	¬garbage, ¬quiet
Also have the maintenance actions		

state-level 0 | action-level 1 | state-level 1

garb — carry — garb / ¬garb
dolly
cleanH — cleanH / ¬cleanH
cook
quiet — quiet / ¬quiet
wrap
dinner
present
¬dinner — ¬dinner
¬present — ¬present

14

Mutual Exclusion

Inconsistent Effects   Interference   Competing Needs   Inconsistent Support

- Two actions at the same action-level are mutex if
  - *Inconsistent effects:* an effect of one negates an effect of the other
  - *Interference:* one deletes a precondition of the other
  - *Competing needs:* **they have mutually exclusive preconditions**
- Otherwise they don't interfere with each other
  - Both may appear in a solution plan
- Two literals at the same state-level are mutex if
  - *Inconsistent support:* one is the negation of the other,
    or all ways of achieving them are pairwise mutex

Recursive propagation of mutexes

15

Example (continued)

- Augment the graph to indicate mutexes
- *carry* is mutex with the maintenance action for *garbage* (inconsistent effects)
- *dolly* is mutex with *wrap*
  - interference
- ¬*quiet* is mutex with *present*
  - inconsistent support
- each of *cook* and *wrap* is mutex with a maintenance operation
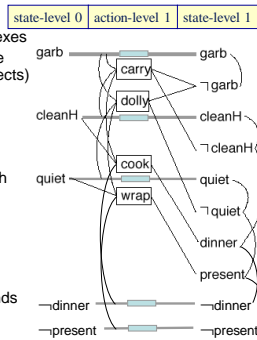
Action	Preconditions	Effects
cook()	cleanHands	dinner
wrap()	quiet	present
carry()	none	¬garbage, ¬cleanHands
dolly()	none	¬garbage, ¬quiet
Also have the maintenance actions		

state-level 0 | action-level 1 | state-level 1

16

Example (continued)

- Check to see whether there's a possible solution
- Recall that the goal is
  {¬*garbage, dinner, present*}
- Note that in state-level 1,
  - All of them are there
  - None are mutex with each other
- Thus, there's a chance that a plan exists
- Try to find it
  - Solution extraction

state-level 0 | action-level 1 | state-level 1
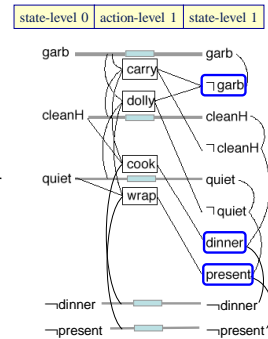
17

Recall what the algorithm does

procedure Graphplan:
- for *k* = 0, 1, 2, …
  - *Graph Expansion:*
    - create a "planning graph" that contains *k* "levels"
  - Check whether the planning graph satisfies a necessary (but insufficient) condition for plan existence
  - If it does, then
    - do *Solution Extraction:*
      - backward search, modified to consider only the actions in the planning graph
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18

Solution Extraction

The set of goals we are trying to achieve

The level of the state s_i

procedure Solution-extraction(*g*,*i*)
  if *i*=0 then return the solution
  for each literal *l* in *g*
    nondeterministically choose an action
      to use in state s_{i-1} to achieve *l*
  if any pair of chosen actions are mutex
    then backtrack
  g' := {the preconditions of
    the chosen actions}
  Solution-extraction(*g', i*–1)
end Solution-extraction

A real action or a maintenance action

state-level i-1 | action-level i | state-level i

19

Example (continued)
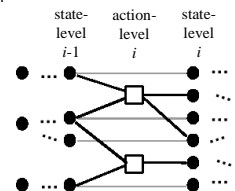
| state-level 0 | action-level 1 | state-level 1 |

- Recall that the goal is
  {¬*garbage, dinner, present*}

- Two sets of actions for the goals at state-level 1

- Neither of them works
  - Both sets contain actions that are mutex

garb — carry — garb
dolly — ¬garb
cleanH — cleanH
¬cleanH
cook — quiet
quiet — wrap
¬quiet
dinner
present
¬dinner — ¬dinner
¬present — ¬present

20

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    - create a "planning graph" that contains *k* "levels"
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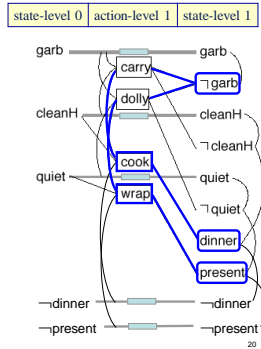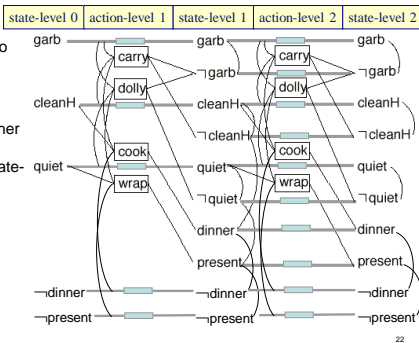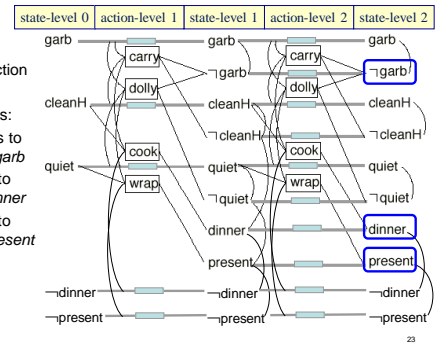   - if we find a solution, then return it

21

Example (continued)

| state-level 0 | action-level 1 | state-level 1 | action-level 2 | state-level 2 |

- Go back and do more graph expansion

- Generate another action-level and another state-level

garb — carry — garb — carry — garb
¬garb — ¬garb
dolly — dolly
cleanH — cleanH — cleanH
¬cleanH — ¬cleanH
cook — cook
quiet — quiet — quiet
wrap — wrap
¬quiet — ¬quiet
dinner — dinner
present — present
¬dinner — ¬dinner — ¬dinner
¬present — ¬present — ¬present

22

Example (continued)

| state-level 0 | action-level 1 | state-level 1 | action-level 2 | state-level 2 |

- Solution extraction

- Twelve combos:
  - Three ways to achieve ¬*garb*
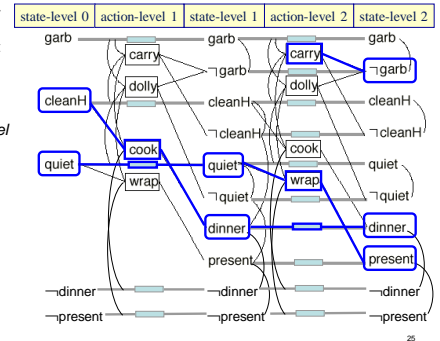 - Two ways to achieve *dinner*
  - Two ways to achieve *present*

garb — carry — garb — carry — garb
¬garb — ¬garb
dolly — dolly
cleanH — cleanH — cleanH
¬cleanH — ¬cleanH
cook — cook
quiet — quiet — quiet
wrap — wrap
¬quiet — ¬quiet
dinner — dinner
present — present
¬dinner — ¬dinner — ¬dinner
¬present — ¬present — ¬present

23

Example (continued)

| state-level 0 | action-level 1 | state-level 1 | action-level 2 | state-level 2 |

- Several of the combinations look OK at level 2

- Here's one of them

garb — carry — garb — carry — garb
¬garb — ¬garb
dolly — dolly
cleanH — cleanH — cleanH
¬cleanH — ¬cleanH
cook — cook
quiet — quiet — quiet
wrap — wrap
¬quiet — ¬quiet
dinner — dinner
present — present
¬dinner — ¬dinner — ¬dinner
¬present — ¬present — ¬present

24
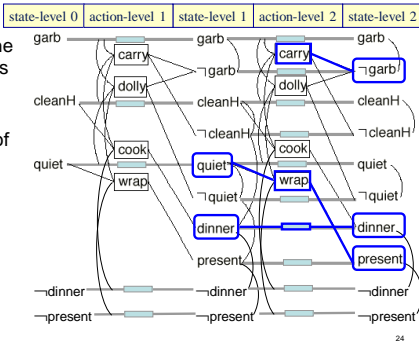
Example (continued)

- Call Solution-Extraction recursively at level 2
- **It succeeds**
- Solution whose *parallel length* is 2

| state-level 0 | action-level 1 | state-level 1 | action-level 2 | state-level 2 |

garb — carry — garb — carry — garb
¬garb — ¬garb
dolly — dolly
cleanH — cleanH — cleanH
¬cleanH — ¬cleanH
cook — cook
quiet — quiet — quiet
wrap — wrap
¬quiet — ¬quiet
dinner — dinner
present — present
¬dinner — ¬dinner — ¬dinner
¬present — ¬present — ¬present

25

Observation

- The solution is a sequence of *sets of actions* (as opposed to simply a sequence of actions)

- To generate a sequential plan, the solution can be serialized (in a variety of ways)

Properties of GraphPlan

- Graphplan is sound and complete
  - If Graphplan returns a plan, then it is a solution to the planning pblm.
  - If solutions exist, then Graphplan will return one of them.

- The size of the planning graph Graphplan generates is polynomial in the size of the planning problems.

- Solutions extraction is still exponential in the worst case.

For many problems, Graph Expansion dominates problem solving time.

- The planning algorithm always terminates
  - There is a fixpoint on the number of levels of the planning graphs such that the algorithm either generates a solution or returns failure

Further Analysis

- (+) The backward-search part of Graphplan—which is the hard part—will only look at the actions in the planning graph – a smaller search space than the original one.

- (-) To generate the planning graph, Graphplan creates a huge number of ground atoms
- Many of them may be irrelevant
- Can alleviate (but not eliminate) this problem by assigning data types to the variables and constants

Optimizations and Extensions

Optimizations to the original Graphplan model:
- Improvements to solution extraction (e.g., forward checking, memoization, EBL)
- Improvements to graph expansion (e.g., closed-world assumption, compilation of action schemata w/ type analysis, in-place graph expansion)

Most of the **extensions** relate to language extensions:
- E.g., Universal quantification, conditional effects, negated preconditions and goals, …
- Addressed by compilation ➔large increases in problem size, or
- Addressed by changing (complicating) the expansion, mutex determination and extraction
- *See [Weld, AIM-99] posted on our web page.*

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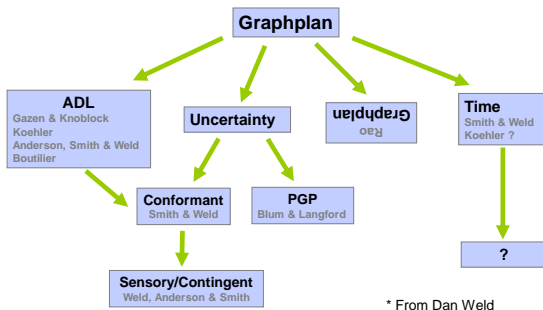- *See [Weld, AIM-99] posted on our web page.*

Graphplan and Its Descendants

- **Graphplan** (Blum & Furst,1995) – C implementation
- **IPP** (Koehler et al. 1997) – highly optimized C implementation, extended to handle universal quantification and conditional effects
- **STAN** (Long & Fox, 1998)- highly optimized C, implementation – uses in-place graph rep'n and performs sophisticated type analysis
- **SGP** (Weld et al., 1998) – Lisp implementation – extended to handl universal quantification, conditional effects, and uncertainty

Perverting Graphplan*

* From Dan Weld

33