CSC2542 Representations for (Classical) Planning

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Acknowledgements

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Recall: Planning Problem $P = (\Sigma, s_0, G)$ $\Sigma: \text{ System Description}$ $s_o: \text{ Initial state}(s)$ $E.g., \text{ Initial state} = s_0$ G: Objective Goal state, Set of goal states, Set of tasks,"trajectory" of states, $\text{Objective function}, \dots$ $E.g., \text{ Goal state} = s_5$ The Dock Worker Robots (DWR) domain

Further Recall: System Description (as a state transition system)

 $\Sigma = (S, A, E, \gamma)$

- S = {states}
- A = {actions}
- $E = \{\text{exogenous events}\}$
- State-transition function $\gamma: S \times (A \cup E) \rightarrow 2^S$

Example: Dock Workers Robots from previous slide

- $S = \{s_0, ..., s_5\}$
- $A = \{\text{move1}, \text{move2}, \text{put}, \text{take}, \text{load}, \text{unload}\}$
- $E = \{\}$
- γ: as captured by the arrows mapping states and actions to successor states

Representational Challenge

How do we represent our planning problem is a way that supports exploration of the principles and practice of automated planning?

Approach:

- There isn't one answer.
- The textbook proposes representations that are suitable for generating classical plans.

Broad Perspective on Plan Representation

The right representation for the right objective.

Distinguish representation schemes for:

- 1. studying the principles of planning and related tasks.
- 2. specifying planning domains
- 3. direct use within (classical) planners

Summary: Broad Perspective

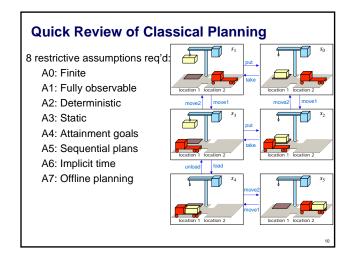
- 1. Studying the formal principles of planning and other related task
 - (First-order) logical languages
 - (e.g., situation calculus, A languages, event calculus, fluent calculus, PDL) Properties:
 - well-defined semantics, representational issues must be addressed in the language (not in the algorithm that interprets and manipulates them)
 - excellent for study and proving properties. Not ideal for 3 below.
- 2. Specifying planning domains
 - PDDL-n (PDDL2.1, PDDL2.2, PDDL3,)
 - Properties:
 - (reasonably) well-defined semantics
 - designed for input to planners translate to an internal representation for specific planners. Translators exist for most state-of-the-art planners
- 3. Direct use within (classical) planners
 - Classical representation (e.g., STRIPS)
 - Set-theoretic representation (basis for rep'ns used w/ SAT solvers)
 State-variable representation (e.g., SAS, SAS+)

 - Variants of these exist for particular planners (e.g., SAT solvers, model checkers, etc.)

This Lecture: 1. Studying the formal principles of planning and other related task • (First-order) logical languages calculus, PDL) dressed in the es them) **WILL COVER LATER** 2. Spec • PDDL-n (PDDL2.1, PDDL2.2, PDDL3,) (reasonably) well-defined semantics designed for input to planners – translate to an internal representation for specific planners. Translators exist for most state-of-the-art planners 3. Direct use within (classical) planners (what's in the text) Classical representation (e.g., STRIPS) Set-theoretic representation (basis for rep'ns used w/ SAT solvers) State-variable representation (e.g., SAS, SAS+) Variants of these exist for particular planners (e.g., SAT solvers, model checkers, etc.)

Outline

- Representation schemes for classical planning
 - 1. Classical representation
 - 2. Set-theoretic representation
 - 3. State-variable representation
- · Examples: DWR and the Blocks World
- Comparisons



Representation: Motivation for Approach

Default view:

- represent state explicitly
- represent actions as a transition system (e.g., as an incidence matrix)

Problem:

- explicit graph corresponding to transition system is huge
- direct manipulation of transition system is cumbersome

Solution:

Provide compact representation of transition system & induced graph

- 1. Explicate the structure of the "states"
 - e.g., states specified in terms of state variables
- Represent actions not as transition system/incidence matrices but as functions (e.g., operators) specified in terms of the state variables
 - An action is applicable to a state when some state variables have certain values. When applicable, it will change the values of certain (other) state variables
- з. To plan,
 - Just give the initial state
 - Use the operators to generate the other states as needed

Why is this more compact?

Why is this more compact than an explicit transition system?

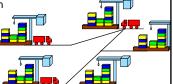
- In an explicit transition system, actions are represented as state-tostate transitions. Each action will be represented by an incidence matrix of size |S|x|S|
- In the proposed model, actions are represented only in terms of state variables whose values they care about, and whose value they affect. (It exploits the structure of the problem!)
- Consider a state space of 1024 states. It can be represented by log₂1024=10 state variables. If an action needs variable v1 to be true and makes v7 to be false, it can be represented by just 2 bits (instead of a 1024x1024 matrix)
 - Of course, if the action has a complicated mapping from states to states, in the worst case the action rep will be just as large
 - The assumption being made here is that the actions will have effects on a small number of state variables.

1. Classical Representation

- Start with a function-free first-order language
 - Finitely many predicate symbols and constant symbols, but no function symbols



- Locations: I1, I2, ...
- Containers: c1, c2, ...
- Piles: p1, p2, ...
- Robot carts: r1, r2, ...
- Cranes: k1, k2, ...



Quick review of terminology

- Atom: predicate symbol and args
 - Use these to represent both fixed and dynamic ("fluent") relations

adjacent(I,I') attached(p,I) belong(k,I)

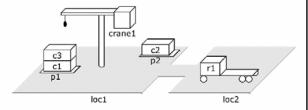
 $\begin{array}{lll} \text{occupied(I)} & \text{at(r,I)} \\ \text{loaded(r,c)} & \text{unloaded(r)} \\ \text{holding(k,c)} & \text{empty(k)} \\ \text{in(c,p)} & \text{on(c,c)} \\ \text{top(p,p)} & \text{top(pallet$,$\mathit{p}$)} \end{array}$

- Ground expression: contains no variable symbols e.g., in(c1,p3)
- Unground expression: at least one variable symbol e.g., in(c1,x)
- Substitution: $\theta = \{x_1 \leftarrow v_1, x_2 \leftarrow v_2, ..., x_n \leftarrow v_n\}$
 - Each x_i is a variable symbol; each v_i is a term
- Instance of e: result of applying a substitution θ to e
 - Replace variables of e simultaneously, not sequentially

. .

States

- State: a set s of ground atoms
 - $\bullet~$ The atoms represent the things that are true in one of $\Sigma \text{'s}$ states
 - Only finitely many ground atoms, so only finitely many possible states



 $\{ attached(p1,loc1), \ in(c1,p1), \ in(c3,p1), \ top(c3,p1), \ on(c3,c1), \ on(c1,pallet), \ attached(p2,loc1), \ in(c2,p2), \ top(c2,p2), \ on(c2,pallet), \ belong(crane1,loc1), \ empty(crane1), \ adjacent(loc1,loc2), \ adjacent(loc2,loc1), \ at(r1,loc2), \ occupied(loc2), \ unloaded(r1) \}.$

Operators

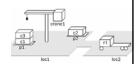
- Operator: a triple o=(name(o), precond(o), effects(o))
 - name(o) is a syntactic expression of the form $n(x_1,...,x_k)$
 - n: operator symbol must be unique for each operator
 - $x_1,...,x_k$: variable symbols (parameters)
 - must include every variable symbol in o
 - precond(o): preconditions
 - literals that must be true in order to use the operator
 - effects(o): effects
 - literals the operator will make true

 $\mathsf{take}(k, l, c, d, p)$

;; crane k at location l takes c off of d in pile p precond: $\mathsf{belong}(k,l)$, $\mathsf{attached}(p,l)$, $\mathsf{empty}(k)$, $\mathsf{top}(c,p)$, $\mathsf{on}(c,d)$ effects: $\mathsf{holding}(k,c)$, $\neg \mathsf{empty}(k)$, $\neg \mathsf{in}(c,p)$, $\neg \mathsf{top}(c,p)$, $\neg \mathsf{on}(c,d)$, $\mathsf{top}(d,p)$

Actions

Action: ground instance (via substitution) of an operator



 $\mathsf{take}(k,l,c,d,p)$

;; crane \boldsymbol{k} at location \boldsymbol{l} takes \boldsymbol{c} off of \boldsymbol{d} in pile \boldsymbol{p}

 $\begin{array}{ll} \text{precond: } \mathsf{belong}(k,l), \mathsf{attached}(p,l), \mathsf{empty}(k), \mathsf{top}(c,p), \mathsf{on}(c,d) \\ \text{effects: } & \mathsf{holding}(k,c), \neg \mathsf{empty}(k), \neg \mathsf{in}(c,p), \neg \mathsf{top}(c,p), \neg \mathsf{on}(c,d), \mathsf{top}(d,p) \end{array}$

take(crane1,loc1,c3,c1,p1)

;; crane crane1 at location loc1 takes c3 off c1 in pile p1

 ${\it precond:}\ {\it belong(crane1,loc1),\ attached(p1,loc1),}$

empty(crane1), top(c3,p1), on(c3,c1)

ffects: holding(crane1,c3), ¬empty(crane1), ¬in(c3,p1),

 $\neg top(c3,p1)$, $\neg on(c3,c1)$, top(c1,p1)

Notation

- Let a be an operator or action. Then
 - precond+(a) = {atoms that appear positively in a's preconditions}
 - precond⁻(a) = {atoms that appear negatively in a's preconditions}
 - effects*(a) = {atoms that appear positively in a's effects}
 - effects⁻(a) = {atoms that appear negatively in a's effects}

E.g.,

 $\mathsf{take}(k, l, c, d, p)$

;; crane k at location l takes c off of d in pile p

 $\mathrm{precond}\colon \mathsf{belong}(k,l), \mathsf{attached}(p,l), \mathsf{empty}(k), \mathsf{top}(c,p), \mathsf{on}(c,d)$

 $\text{effects:} \quad \mathsf{holding}(k,c), \neg \, \mathsf{empty}(k), \neg \, \mathsf{in}(c,p), \neg \, \mathsf{top}(c,p), \neg \, \mathsf{on}(c,d), \mathsf{top}(d,p)$

- effects*(take(k,l,c,d,p) = {holding(k,c), top(d,p)}
- effects⁻(take(k,l,c,d,p) = {empty(k), in(c,p), top(c,p), on(c,d)}

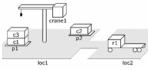
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Aside: Some things to note

- The state only explicitly represents what is true. The semantics of this representation is that any fluent not included in the state is false just like a database. (Recall that one of the assumptions of classical planning is complete initial (and subsequent) state. The problem would be a lot harder w/o this assumption!!)
- **Terminology:** an action is a ground operator. In the Knowledge Representation (KR) literature the concept of an "operator" is not used. Actions may be ground or unground.
- Classical planners generally operate over ground actions.

Applicability

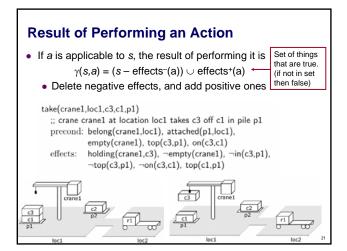
- An action a is applicable to a state s if s satisfies precond(a),
 - i.e., if precond+(a) \subseteq s and precond-(a) \cap s = \emptyset
- Here are an action and a state that it's applicable to:

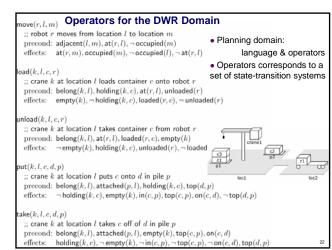


take(crane1,loc1,c3,c1,p1)

;; crane crane1 at location loc1 takes c3 off c1 in pile p1 precond: belong(crane1,loc1), attached(p1,loc1),

empty(crane1), top(c3,p1), on(c3,c1) effects: holding(crane1,c3), \neg empty(crane1), \neg in(c3,p1), \neg top(c3,p1), \neg on(c3,c1), top(c1,p1)





Planning Problems

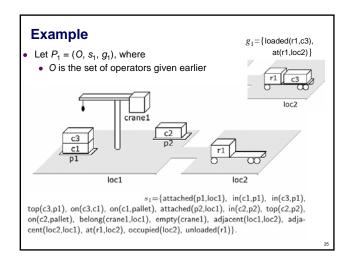
Given a planning domain (language L, operators O)

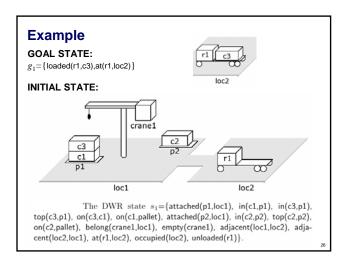
- Encoding of a planning problem: a triple $P=(O,s_0,g)$
 - O is the collection of operators
 - s_0 is a state (the initial state)
 - g is a set of literals (the goal formula)
- The actual planning problem: $P = (\Sigma, s_0, g)$
 - s_0 and g are as above
 - $\Sigma = (S,A,\gamma)$ is a state-transition system
 - S = {all sets of ground atoms in L}
 - A = {all ground instances of operators in O}
 - γ = state-transition function determined by the operators

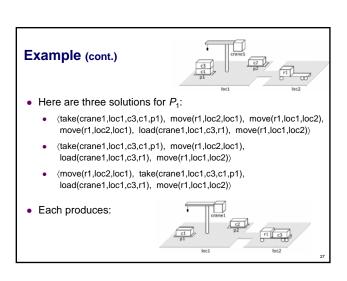
Plans and Solutions

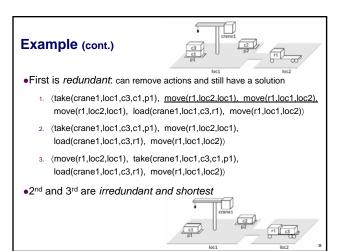
- *Plan*: any sequence of actions $\sigma = \langle a_1, a_2, ..., a_n \rangle$ such that each a_i is a ground instance of an operator in O
- The plan is a solution for P=(O,s₀,g) if it is executable and achieves g
 - i.e., if there are states $s_0, s_1, ..., s_n$ such that
 - $\gamma(s_0, a_1) = s_1$
 - $\gamma(s_1, a_2) = s_2$
 - ...

 - s_n satisfies g



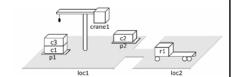






2. Set-Theoretic Representation

Like classical rep'n, but restricted to propositional logic.



- States:
 - Instead of a collection of ground atoms ...
 {on(c1,pallet), on(c1,r1), on(c1,c2), ..., at(r1,11), at(r1,12), ...}
 - ... use a collection of propositions (boolean variables): {on-c1-pallet, on-c1-r1, on-c1-c2, ..., at-r1-l1, at-r1-l2, ...}

Instead of operators like this one,

```
\begin{split} \mathsf{take}(k,l,c,d,p) \\ &\text{ ;; crane } k \text{ at location } l \text{ takes } c \text{ off of } d \text{ in pile } p \\ &\text{precond: } \mathsf{belong}(k,l), \mathsf{attached}(p,l), \mathsf{empty}(k), \mathsf{top}(c,p), \mathsf{on}(c,d) \\ &\text{effects: } \mathsf{holding}(k,c), \neg \mathsf{empty}(k), \neg \mathsf{in}(c,p), \neg \mathsf{top}(c,p), \neg \mathsf{on}(c,d), \mathsf{top}(d,p) \end{split}
```

Take all of the operator instances, E.g.:

```
 \begin{array}{l} take (crane1,loc1,c3,c1,p1) \\ ;; crane \ crane1 \ at \ location \ loc1 \ takes \ c3 \ off \ c1 \ in \ pile \ p1 \\ precond: \ belong (crane1,loc1), \ attached (p1,loc1), \\ empty (crane1), \ top (c3,p1), \ on (c3,c1) \\ effects: \ \ holding (crane1,c3), \ \neg empty (crane1), \ \neg in (c3,p1), \\ \neg top (c3,p1), \ \neg on (c3,c1), \ top (c1,p1) \end{array}
```

And rewrite ground atoms as propositions, E.g.:

```
take-crane1-loc1-c3-c1-p1
precond: belong-crane1-loc1, attached-p1-loc1,empty-crane1, top-c3-p1, on-c3-c1
delete: empty-crane1, in-c3-p1, top-c3-p1, on-c3-p1
add: holding-crane1-c3, top-c1-p1
```

Comparison

A set-theoretic representation is equivalent to a classical representation in which all of the atoms are ground

Problem: Exponential blowup

• If a classical operator contains n atoms and each atom has arity k, then it corresponds to c^{nk} actions where $c = |\{\text{constant symbols}\}|$

3. State-Variable Representation

- Non-fluents (properties that don't change) are ground relations:
 e.g., adjacent(loc1,loc2)
- Fluents are functions:

i.e., for properties that can change, assign values to state variables

 Classical and state-variable rep'ns take similar amounts of space each can be translated into the other in low-order polynomial time

, |

State-Variable Representation (cont.)

- Captures further information about the state. E.g., that state variables can only take on one of the values in the domain. This helps reduce the search space.
- Basis for the SAS and SAS+ formalisms (used most recently in the FastDownward Planner (FD)
- Basis for encodings further plan properties such as domain transition graphs (DTGs) and causal graphs (CG)

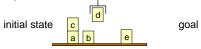
Example: The Blocks World (Review on your own)

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Example: The Blocks World

- Infinitely wide table, finite number of children's blocks
- Ignore where a block is located on the table
- A block can sit on the table or on another block
- Want to move blocks from one configuration to another

• e.a.

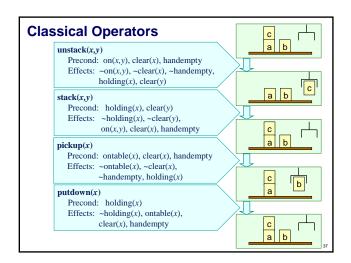


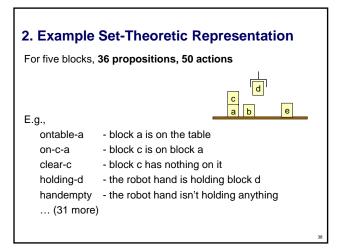
 Classical, set-theoretic, and state-variable formulations for the case of FIVE BLOCKS follow.

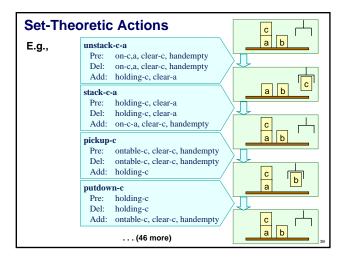
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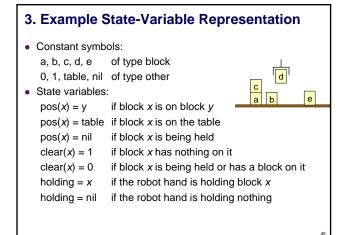
1. Example Classical Representation

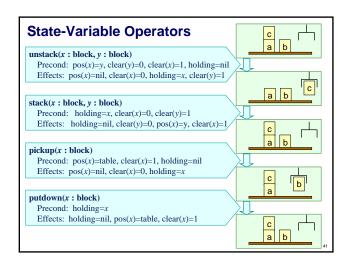
- Constant symbols:
 - The blocks: a, b, c, d, e
- Predicates:
 - ontable(x) block x is on the table
 - on(x,y) block x is on block y
 - clear(x) block x has nothing on it
 - ullet holding(x) the robot hand is holding block x
 - handempty- the robot hand isn't holding anything

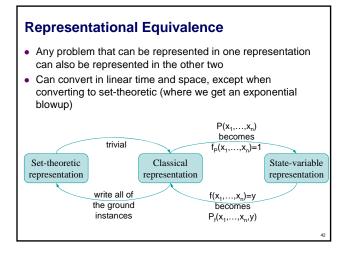












Comparison

- Classical representation
 - Most popular for classical planning, basis of PDDL
- Set-theoretic representation
 - Can take much more space than classical representation
 - Useful in algorithms that manipulate ground atoms directly
 e.g., planning graphs, SAT
 - Useful for certain kinds of theoretical studies
- State-variable representation (e.g., SAS, SAS+)
 - Equivalent to classical representation in expressive power
 - · Arguably less natural to conceive
 - Useful in non-classical planning problems as a way to handle numbers, functions, time

Extending Expressivity: ADL

- Previous representations were so-called "STRIPS" rep'ns.
 These have useful properties for automatically generating classical plans, but are not always sufficient to express the behaviour of more complex domains.
- ADL is a richer, and thus more compact, representation language that allows for
 - Disjunction and Quantification in preconditions and goals
 - Effects that are Quantified, and/or Conditional (effect is conditioned on state)
- PDDL supports STRIPS and ADL, but not all planners support ADL, and not all planners even support a so-called Classical Representation
- In the KR community ADL or greater is common.

Pros/Cons: Compiling to Canonical Action Rep'n

Possible to compile down ADL actions into STRIPS actions

- Quantification -> conjunctions/disjunctions over finite universes
- Actions with conditional effects -> multiple (exponentially more) actions without conditional effects
- Actions with disjunctive effects -> multiple actions, each of which take one of the disjuncts as their preconditions
- Domain axioms (ramifications) -> the individual effects of the actions; so all actions satisfy STRIPS assumption

Compilation is not always a win-win.

- By compiling down to canonical form, we can concentrate on highly efficient planning for canonical actions
 - However, often compilation leads to an exponential blowup and makes it harder to exploit the structure of the domain
- By leaving actions in non-canonical form, we can often do more compact encoding of the domains <u>as well as more efficient search</u>
 - However, we will have to continually extend planning algorithms to handle these representations