

Prove that a language L is recognizable if and only if there exists a decidable language D such that

$$L = \{w \mid \exists t : \langle w, t \rangle \in D\}$$

Hint: For the “only if” direction, consider interpreting t as a sequence of instantaneous descriptions.