

## Today's Topics

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16. Intro to Computer Animation

17. Computational Photography

Exam prep session:

7-9pm Wednesday, Dec 15th  
in BA 5256 (seminar room near my  
office)

## Topic 16:

# Computer Animation

- Keyframe animation
- Forward kinematics
- Inverse kinematics
- Motion capture
- Physics-based animation (dynamics)

## Keyframe Animation

Basic idea: Define model parameters at key frames and interpolate (often using cubic splines)

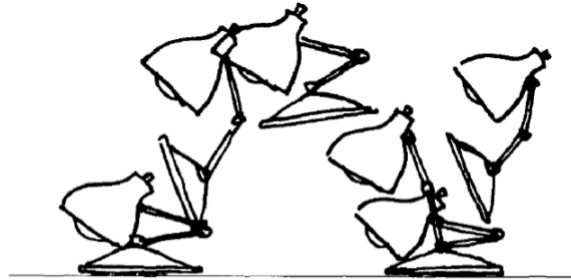


FIGURE 3. Squash & stretch in Luxo Jr.'s hop.  
J. Lasseter, "Principles of Traditional Animation Applied to 3D Computer Animation"  
Proc. SIGGRAPH, pp. 35-44, 1983

## Designing Plausible Motions

It is quite easy to end up with a physically impossible motion

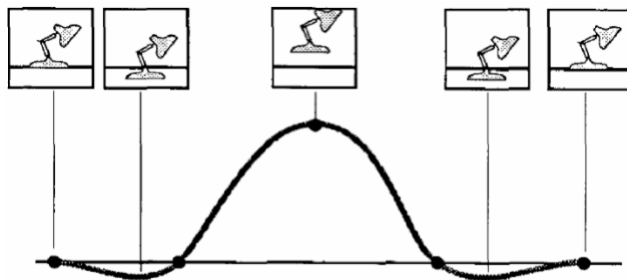
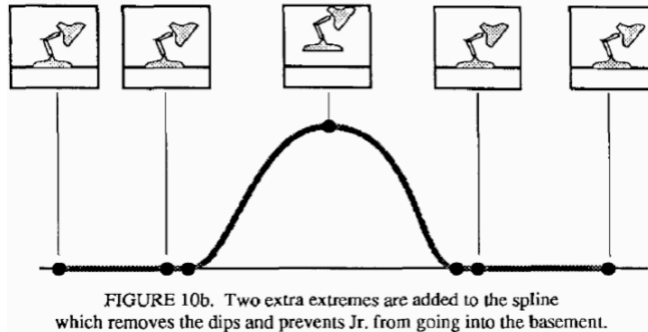


FIGURE 10a. This spline controls the Z (up) translation of Luxo Jr.  
Dips in the spline cause him to intersect the floor.

## Designing Plausible Motions

It is quite easy to end up with a physically impossible motion  $\Rightarrow$  add a sufficient # of keyframes to constrain the motion sufficiently



## Keyframe Animation

"Whether it is generated by hand or by computer, the first goal of the animator is to entertain. [...] Tools, in the sense of hardware & software, are simply not enough."  
- John Lasseter, Pixar

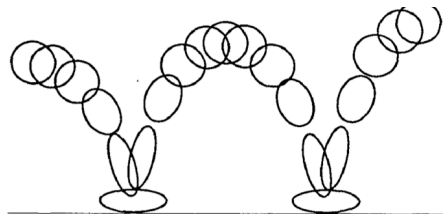


FIGURE 2. Squash & stretch in bouncing ball.

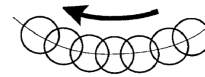


FIGURE 4a. In slow action, an object's position overlaps from frame to frame which gives the action a smooth appearance to the eye.

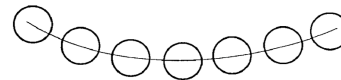


FIGURE 4b. Strobing occurs in a faster action when the object's positions do not overlap and the eye perceives separate images.

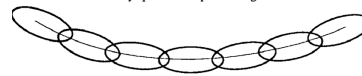


FIGURE 4c. Stretching the object so that its positions overlap again will relieve the strobing effect.

## Keyframe Animation

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"Whether it is generated by hand or by computer, the first goal of the animator is to entertain. [...] Tools, in the sense of hardware & software, are simply not enough."

- John Lasseter, Pixar

Luxo Jr.



## Keyframe Animation

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### Pros

Very expressive

Animator has full control of animation

### Cons

Very labor intensive

Difficult to create convincing physical realism  
(if that is a goal)

Used for practically anything except complex physical simulations (smoke, water, etc)

## Topic 16:

# Computer Animation

- Keyframe animation
- Forward kinematics
- Inverse kinematics
- Motion capture
- Physics-based animation (dynamics)

### Specifying & Interpolating Keyframes

- Instead of painstakingly specifying every little motion, specify very few keyframes (or just initial & goal)
- Interpolations done automatically

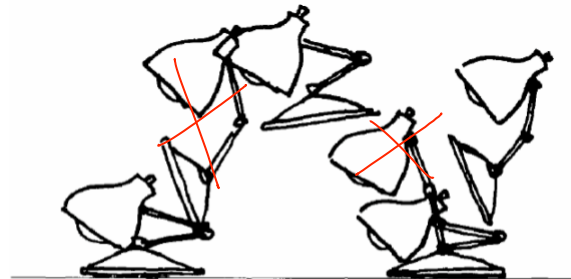


FIGURE 3. Squash & stretch in Luxo Jr.'s hop.

## Animating Articulated Structures

### 1. Forward kinematics

specify how joints should move

### 2. Inverse kinematics

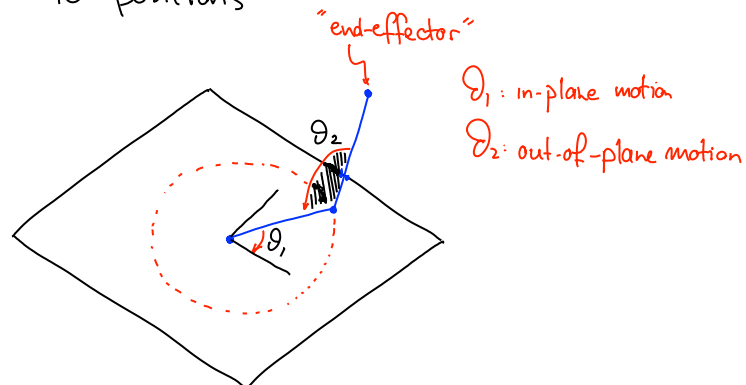
specify where character should go,  
then deduce joint motion

### 3. Motion capture

record motions of real people/objects,  
then transfer to digital characters

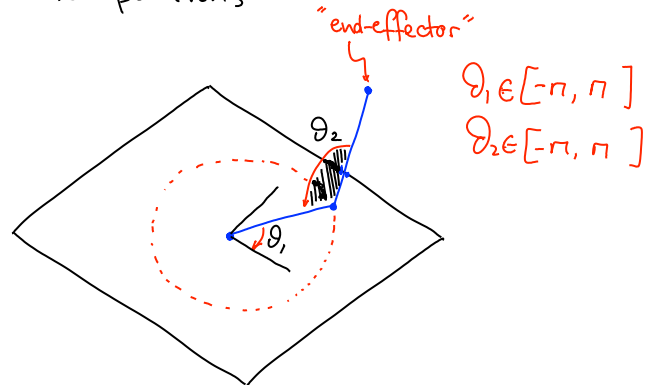
## Forward Kinematics

- Goals:
- determine space of possible motions
  - parameterize it
  - establish a mapping from joint angles to positions



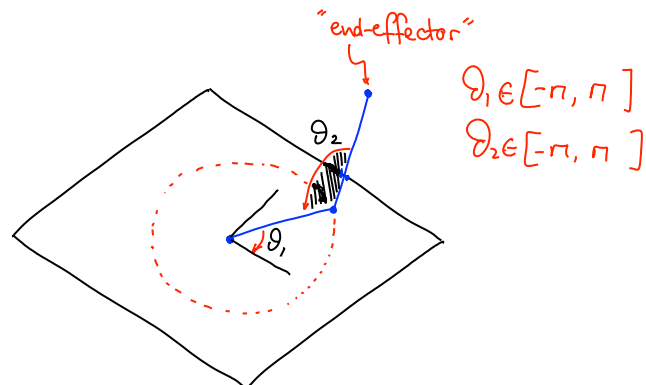
## Forward Kinematics

- Goals:
- determine space of possible motions
  - parameterize it
  - establish a mapping from joint angles to positions



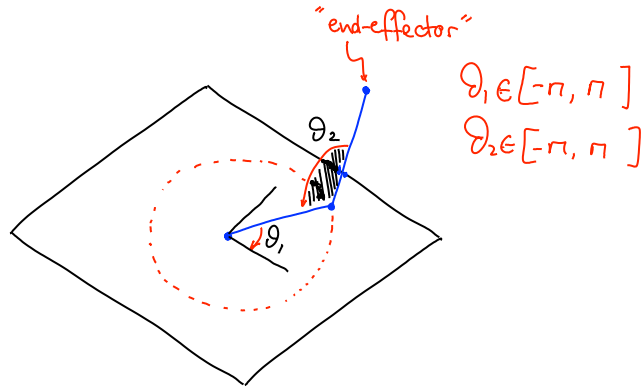
## End-Effector Space (aka "Configuration Space")

What is the set of points that are "reachable" by this 2-axis structure?

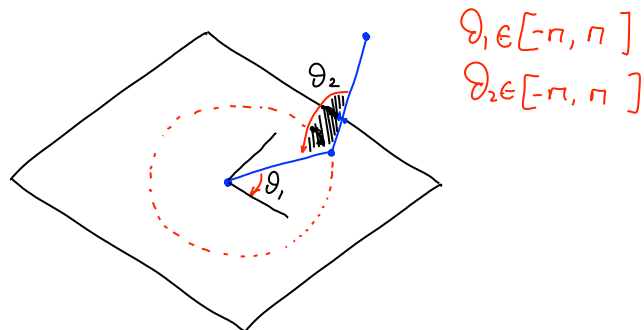
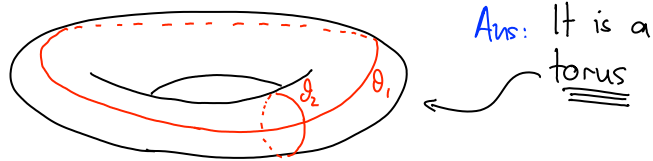


## End-Effector Space (aka "Configuration Space")

What is the set of points "traced" by the end-effector as  $\theta_1, \theta_2$  go through all angles?

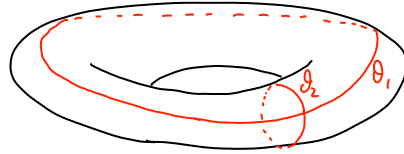


## End-Effector Space (aka "Configuration Space")



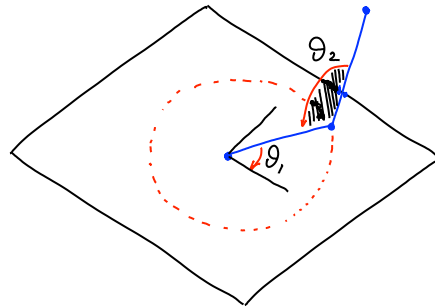


## End-Effector Space (aka "Configuration Space")



Q: How can we parameterize the torus?

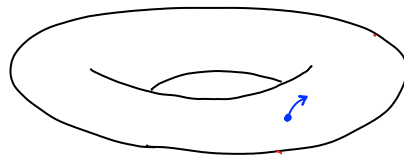
Hint: it is a surface of revolution!



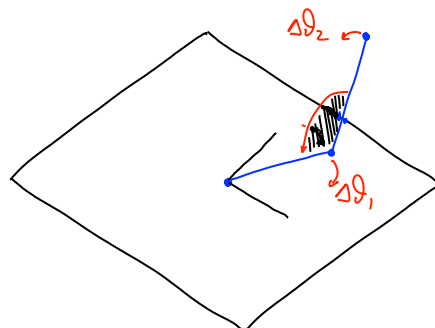
$$\theta_1 \in [-\pi, \pi]$$

$$\theta_2 \in [-\pi, \pi]$$

## Motion in Joint Space vs. Configuration Space



Motion on the torus in the end-effector domain



$$\theta_1 \in [-\pi, \pi]$$

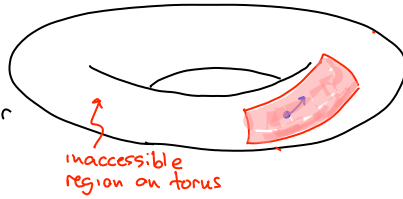
$$\theta_2 \in [-\pi, \pi]$$

Motion in the joints domain

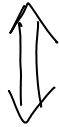


## Motion in Joint Space vs. Configuration Space

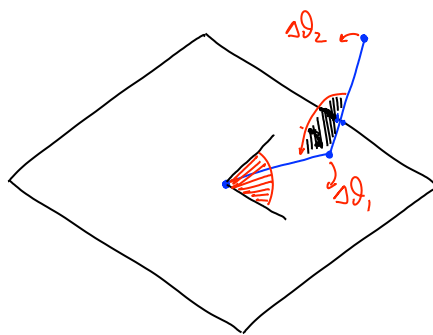
Inaccessible regions in the end-effector domain



Motion on the torus in the end-effector domain



Joint limits in the joints domain



$$\theta_1 \in [0, \theta_1^{\max}]$$

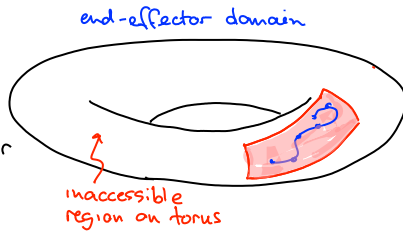
$$\theta_2 \in [0, \theta_2^{\max}]$$

Motion in the joints domain



## Key-Framing with Forward Kinematics

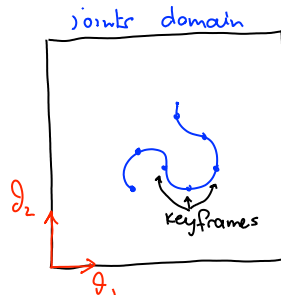
Inaccessible regions in the end-effector domain



... and it determines motion in the end-effector domain



Joint limits in the joints domain



Motion is defined in the joints domain



## Key-Framing with Forward Kinematics

### Pros

Very easy to specify & implement

### Cons

- Often we care more about where the character should go, not how to get there
- Very hard to know how to move joints of a complicated figure in order to get the desired pose (esp. in presence of obstacles)

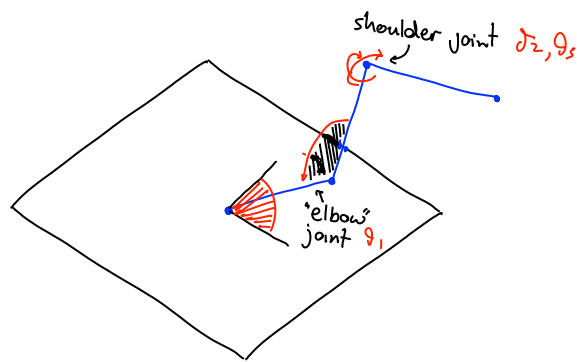
## Key-Framing with Forward Kinematics

End-effector spaces quickly become very complicated!

Example: What is the end-effector space of an arm?

Ans A 3-torus embedded in  $\mathbb{R}^3$  ...

$$\begin{array}{ccc} (\theta_1, \theta_2, \theta_3) & \longrightarrow & \mathbb{R}^3 \\ \text{joint angles} & & \text{end-effector} \end{array}$$

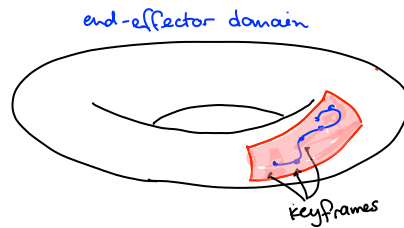


# Topic 16:

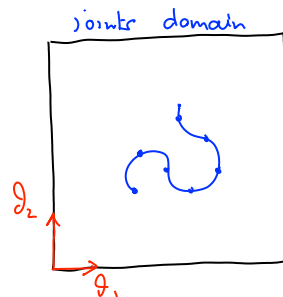
## Computer Animation

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- Forward kinematics
- Inverse kinematics
- Motion capture
- Physics-based animation (dynamics)

### Key-Framing with Inverse Kinematics

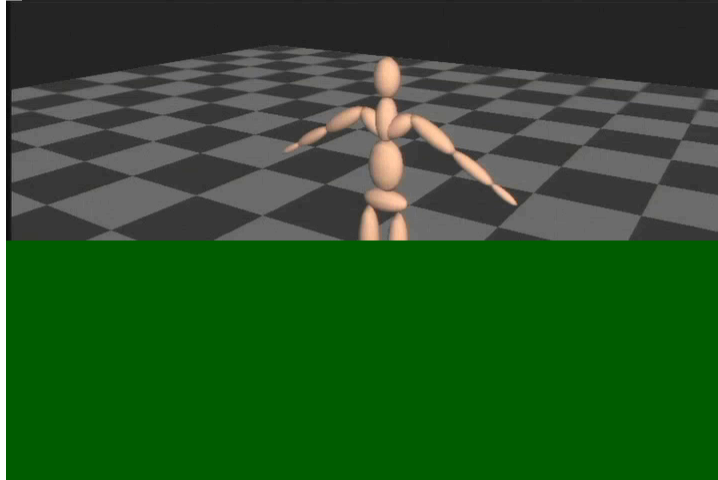


We specify where the end-effector should move in the domain



The joint motion to achieve this is computed automatically.

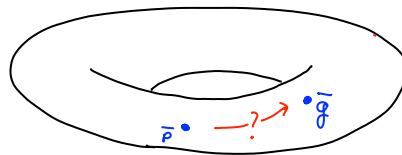
## Key-Framing with Inverse Kinematics



Grochow et al, SIGGRAPH04

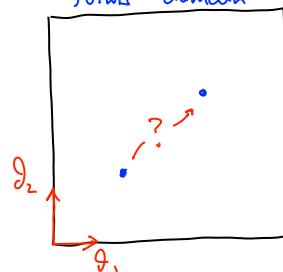
## Inverse Kinematics

end-effector domain



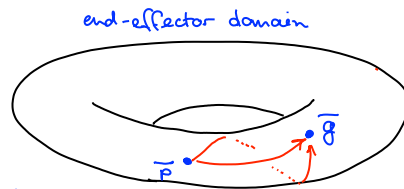
We specify where the end-effector should move in the domain

joint domain



The joint motion to achieve this is computed automatically.

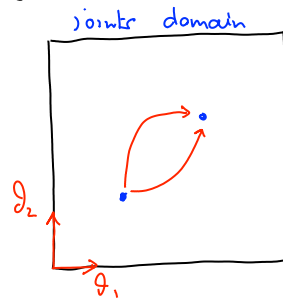
## Inverse Kinematics: Difficulties



We specify where the end-effector should move in the domain

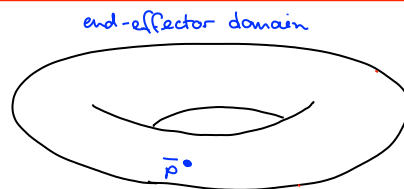
### Major difficulties

- many ways to go from  $\bar{p}$  to  $\bar{g}$  (solution not unique!)



The joint motion to achieve this is computed automatically.

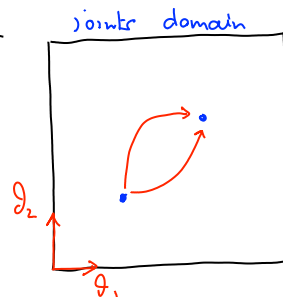
## Inverse Kinematics: Difficulties



We specify where the end-effector should move in the domain

### Major difficulties

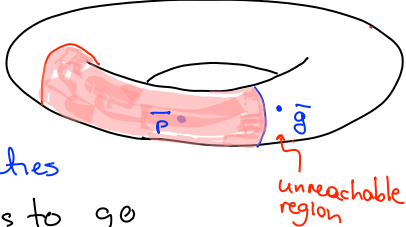
- many ways to go from  $\bar{p}$  to  $\bar{g}$
- position may not be reachable!



The joint motion to achieve this is computed automatically.

## Inverse Kinematics: Difficulties

end-effector domain

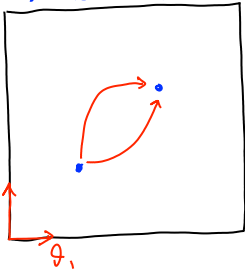


We specify where the end-effector should move in the domain

Major difficulties

- many ways to go from  $\bar{p}$  to  $\bar{g}$
- position may not be reachable!
- mapping to/from joint space is highly non-linear!

joint domain



The joint motion to achieve this is computed automatically.

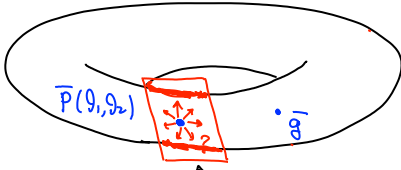
## Numerical Inverse Kinematics

### Linearization

Given current position  $\bar{p}(\theta_1, \theta_2)$  take a small step toward goal position

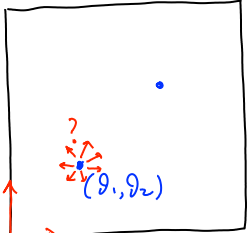
Q: How should we move joints differentially to make positive progress toward goal?

end-effector domain



tangent plane at  $\bar{p}(\theta_1, \theta_2)$

joint domain



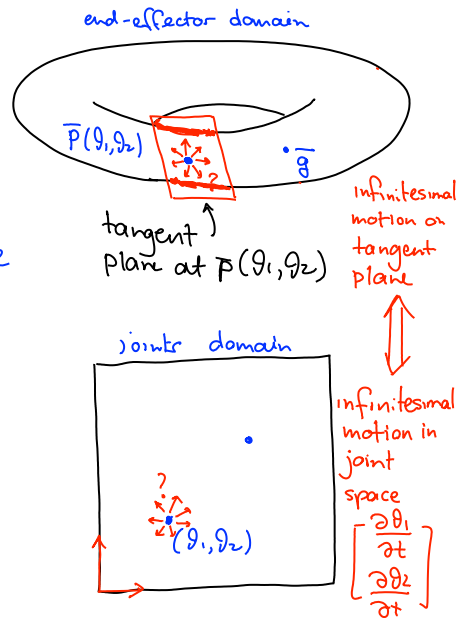
## Numerical Inverse Kinematics

### Linearization

Given current position  $\bar{P}(\theta_1, \theta_2)$  take a small step toward goal position  
 how do we move on tangent plane to minimize distance to goal?

Q: How should we move joints differentially to make positive progress toward goal?

translation to goal:  
 $\bar{g} - \bar{P}(\theta_1, \theta_2)$



## Inverse Kinematics & the Jacobian

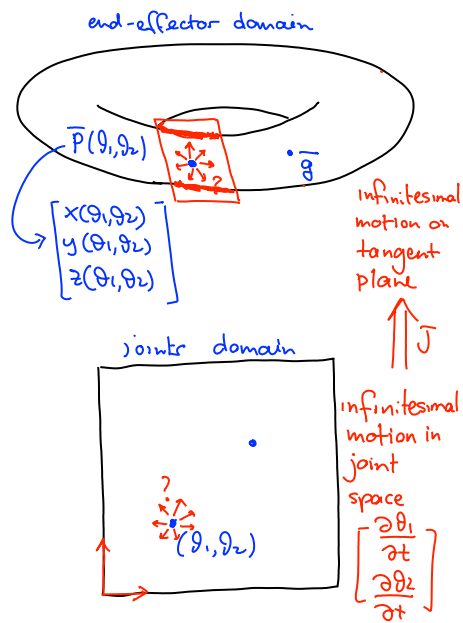
### Linearization

$$\begin{bmatrix} \frac{\partial x}{\partial t} \\ \frac{\partial y}{\partial t} \\ \frac{\partial z}{\partial t} \end{bmatrix} = \begin{bmatrix} \frac{\partial x}{\partial \theta_1} & \frac{\partial x}{\partial \theta_2} \\ \frac{\partial y}{\partial \theta_1} & \frac{\partial y}{\partial \theta_2} \\ \frac{\partial z}{\partial \theta_1} & \frac{\partial z}{\partial \theta_2} \end{bmatrix} \begin{bmatrix} \frac{\partial \theta_1}{\partial t} \\ \frac{\partial \theta_2}{\partial t} \end{bmatrix}$$

↑ end-effector motion      Jacobian J      ↑ joint motion

Q: How should we move joints differentially to make positive progress toward goal?

translation to goal:  
 $\bar{g} - \bar{P}(\theta_1, \theta_2)$





## Inverse Kinematics & the Jacobian

### Linearization

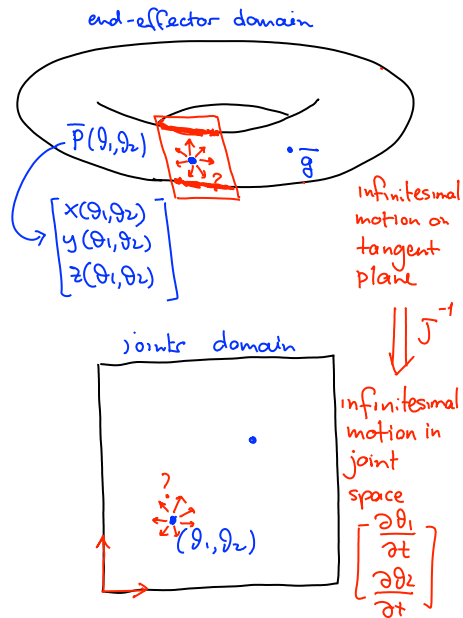
$$\frac{d\bar{p}}{dt} = J \frac{d\bar{\theta}}{dt}$$

end-effector motion ← Jacobian ← joint motion

$$\frac{d\bar{\theta}}{dt} = J^{-1} \frac{d\bar{p}}{dt}$$

Q: How should we move joints differentially to make positive progress toward goal?

translation to goal:  
 $\bar{g} - \bar{p}(\theta_1, \theta_2)$



## Inverse Kinematics Using the Jacobian

### Linearization

$$\frac{d\bar{p}}{dt} = J \frac{d\bar{\theta}}{dt}$$

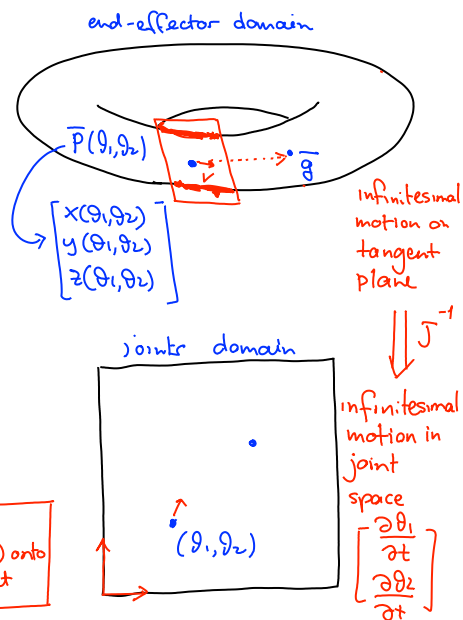
end-effector motion ← Jacobian ← joint motion

$$\frac{d\bar{\theta}}{dt} = J^{-1} \frac{d\bar{p}}{dt}$$

Q: How should we move joints differentially to make positive progress toward goal?

$$\frac{d\bar{\theta}}{dt} = \alpha J^{-1} \bar{v}$$

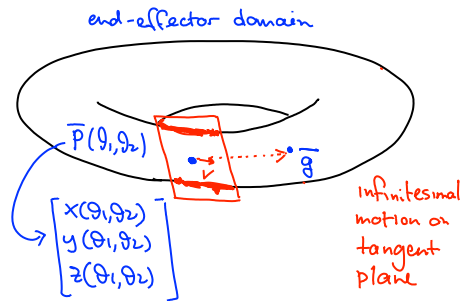
$\alpha$ : small step length  
 $\bar{v}$ : projection of  $\bar{g} - \bar{p}(\theta_1, \theta_2)$  onto tangent plane at  $\bar{p}(\theta_1, \theta_2)$



## Inverse Kinematics Using the Jacobian

### Linearization

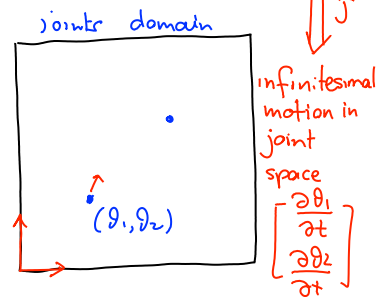
- $J$  is different at each  $(\theta_1, \theta_2) \Rightarrow$  must recompute after each step
- $J$  may not be invertible  $\Rightarrow$  take pseudo inverse



Q: How should we move joints differentially to make positive progress toward goal?

$$\frac{d\bar{\theta}}{dt} = \alpha \bar{J}^{-1} \bar{v}$$

$\alpha$ : small step length  
 $\bar{J}^{-1}$ : projection of  $\bar{v} - \bar{P}(\theta_1, \theta_2)$  onto tangent plane at  $\bar{P}(\theta_1, \theta_2)$



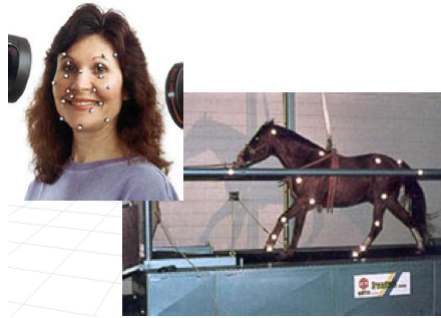
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## Marker-Based Motion Capture

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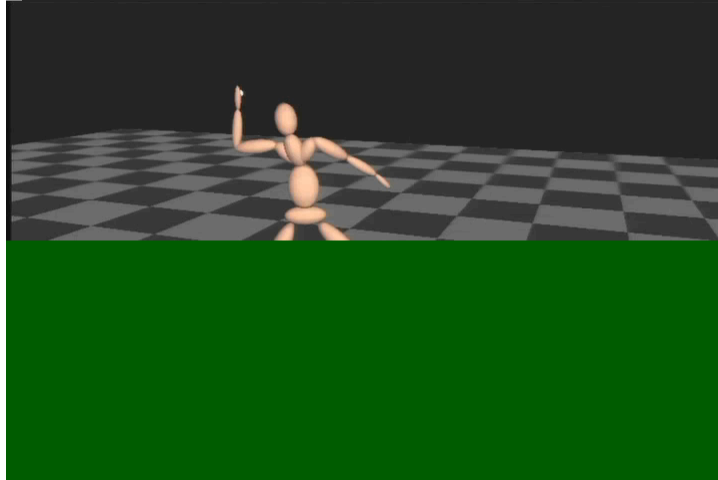


## What the Camera Sees ...

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## Manipulating & Re-Targeting MoCap Data...



*Grochow et al, SIGGRAPH'04*

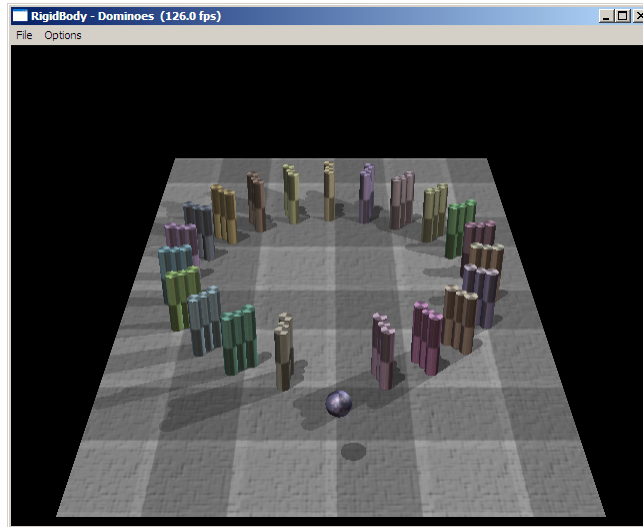
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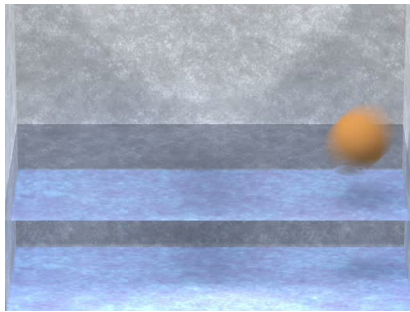
## Simulating Rigid-Body Physics

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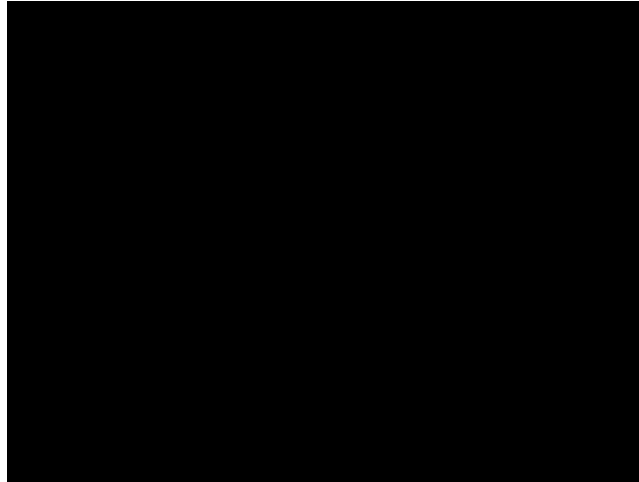


## Simulating Physics of Fluids & Rigid Bodies

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## Simulating Physics of Fluids & Rigid Bodies



## Topic 17:

# Computational Photography

- Keyframe animation
- Forward kinematics
- Inverse kinematics
- Motion capture
- Physics-based animation (dynamics)

## Three Converging Trends

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digital cameras



## Three Converging Trends

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digital cameras + computation

**Canon's first wide angle Digital IXUS includes DIGIC III and Face Detection**

Two Canon Digital IXUS 850 IS cameras are shown side-by-side. The camera on the left is shown from the back, highlighting the LCD screen and control buttons. The camera on the right is shown from the front, highlighting the lens and flash. Both cameras are silver and black.

**Amstelveen, The Netherlands, 14 September, 2006:** Canon today debuts its latest offering for the style-conscious photo enthusiast – the Digital IXUS 850 IS. The 7.1 Megapixel camera introduces wide-angle zoom capability to the Digital IXUS range for the first time with an optical Image Stabilizer and 28mm (35mm equivalent) 3.8x optical zoom lens.

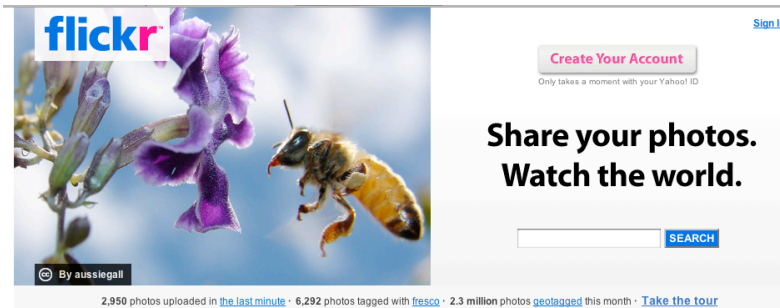
Geared to satisfy serious photographers, the ultra-compact Digital IXUS 850 IS stays true to its design heritage with a smoothly sculpted curvature design and all-metal finish. Enhanced performance and image quality are assured through Canon's latest DIGIC III image processor, which also enables low-noise ISO 1600 shooting and new Face Detection AF/AE – a Canon technology that detects up to nine faces in a frame and automatically optimises the focus and exposure for great people shots.

The Digital IXUS 850 IS will be available from early October.

## Three Converging Trends

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digital cameras + computation + web



## Digital post-processing

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### Photoshop

replacing traditional darkroom techniques

also replacing exposure compensation, color filtering, and other specialized shooting techniques

### second generation tools

warping images, stitching panoramas

will eventually replace the view and panoramic camera

### around the bend

high-X imaging (resolution, dynamic range, focus, etc.)

techniques based on multiple images

Slide by Marc Levoy



## SIGGRAPH Videos

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Nishino & Nayar, "Eyes for Relighting," Proc. SIGGRAPH 2004

Bitouk et al, "Face swapping: Automatically replacing faces in photographs," Proc. SIGGRAPH 2008

Ballan et al, "Unstructured Video-based Rendering: Interactive Exploration of Casually-Captured Videos," Proc. SIGGRAPH 2010

Liu et al, "Content-preserving warps for 3D video stabilization," Proc. SIGGRAPH 2009

Yuan et al, "Image deblurring from blurred/noisy image

## Eyes for Relighting

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# Eyes for Relighting

Ko Nishino Shree K. Nayar  
Columbia University

## Face swapping

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### Face Swapping: Automatic Face Replacement in Photographs

Dmitri Bitouk, Neeraj Kumar, Samreen Dhillon,  
Peter N. Belhumeur, Shree K. Nayar

Columbia University

## Unstructured Video-based Rendering

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### Unstructured Video-Based Rendering: Interactive Exploration of Casually Captured Videos

L. Ballan   G. J. Brostow   J. Puwein   M. Pollefeys  
ETHZ   UCL   ETHZ   ETHZ

*SIGGRAPH 2010*

## 3D Video Stabilization

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CONTENT-PRESERVING WARPS FOR  
3D VIDEO STABILIZATION

FENG LIU  
MICHAEL GLEICHER  
UNIVERSITY OF WISCONSIN-MADISON

HAILIN JIN  
ASEEM AGARWALA  
ADOBE SYSTEMS, INC.

*SIGGRAPH '09*

## Image deblurring

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**Image Deblurring with  
Blurred/Noisy Image Pairs**

Lu Yuan            Jian Sun  
Long Quan        Heung-Yeung Shum

*Siggraph 2007*

## What Comes Next...

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### Computer Graphics

- 2521 Human Motion Modeling
- 2522 Advanced Image Synthesis
- 2529 Facial Animation
- 2530 Computational Photography

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