

96 Formalize and disprove the statement “There is a natural number that is not equal to any natural number.”.

After trying the question, scroll down to the solution.

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$\exists n: \text{nat} \cdot \forall m: \text{nat} \cdot n \neq m$

Leaving the domain nat implicit,

$\exists n \cdot \forall m \cdot n \neq m$

$\Rightarrow \exists n \cdot n \neq n$

$= \exists n \cdot \perp$

$= \perp$

specialization: replace m with n
 \neq is irreflexive
Identity