52 The compound axiom says

 $x: A, B = x: A \lor x: B$ 

There are 16 two-operand binary operators that could sit where v sits in this axiom if we just replace bunch union (,) by a corresponding bunch operator. Which of the 16 two-operand binary operators correspond to useful bunch operators?

After trying the question, scroll down to the solution.

What is "useful"? It's not a well-defined question. I suppose any non-degenerate operator is useful (which means it uses both its operands; on the theorem table below, if the comment to the right mentions both A and B then the operator is not degenerate). One could argue that the degenerate operators are useful for throwing away information, or that they aren't useful because there is a perfectly good zero-operand or one-operand operator that could be used in their place.

Let A be the complement of bunch A (those elements that are not in A, A has precedence 2), defined formally by r A = -r A

	$x: \forall A \equiv \neg x: A$			
	ΤΤ	Τ⊥	ΤT	
	Т	Т	Т	Т
v	Т	Т	Т	$\perp$
←	Т	Т	$\perp$	Т
	Т	Т	$\perp$	$\perp$
$\Rightarrow$	Т	$\bot$	Т	Т
	Т	$\bot$	Т	$\bot$
=	Т	$\bot$	$\bot$	Т
٨	Т	$\bot$	$\bot$	$\bot$
		Т	Т	Т
+		Т	Т	$\bot$
		Т	$\bot$	Т
		Т	$\bot$	$\bot$
		T	Т	Т
		T	Т	$\bot$
		T	$\bot$	Т
		T	$\bot$	$\bot$
	1			

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