You are given a finite set of messages, and for each message, the probability of its occurrence.

(a) Write a program to find a binary code for each message. It must be possible to unambiguously decode any sequence of 0s and 1s into a sequence of messages, and the average code length (according to message frequency) must be minimum.

(b) Write the accompanying program to produce the decoder for the codes produced in part (a).