was written with the intention to swap the values of \( i \) and \( A \) \( i \). Assume that all variables and array elements are of type \( \text{nat} \), and that \( i \) has a value that is an index of \( A \).

(a) In variables \( x, i, \) and \( A \), specify that \( i \) and \( A \) \( i \) should be swapped, the rest of \( A \) should be unchanged, but \( x \) might change.

\[
i' = A \iff i \to i \mid A
\]

(b) Find the exact precondition for which the program refines the specification of part (a).

\[
\forall x', i', A' \mid \exists i \iff i = i \to i \mid A \\
\Rightarrow \forall x', i', A', i = i \to i \mid A \\
\Rightarrow \exists i \iff i = i \to i \mid A
\]

So \( i \) and \( A \) \( i \) will be swapped if and only if they have the same value to start with, making the swap useless.

(c) Find the exact postcondition for which the program refines the specification of part (a).

\[
\exists x, i, A' \mid i = i \to i \mid A \\
\Rightarrow \forall x, i, A' \mid i = i \to i \mid A
\]