

294 Let P and Q be specifications. Let A be an assertion and let A' be the same as A but with primes on all the variables. Prove the assertion law

$$P \cdot Q \iff P \wedge A'. A \Rightarrow Q$$

After trying the question, scroll down to the solution.

§ Let A'' be the same as A but with double-primed variables. Then

$$\begin{aligned} & P \wedge A'. A \Rightarrow Q \\ = & \exists \sigma'' \cdot \langle \sigma' \cdot P \wedge A' \rangle \sigma'' \wedge \langle \sigma \cdot A \Rightarrow Q \rangle \sigma'' \\ = & \exists \sigma'' \cdot \langle \sigma' \cdot P \rangle \sigma'' \wedge A'' \wedge (A'' \Rightarrow \langle \sigma \cdot Q \rangle \sigma'') \\ = & \exists \sigma'' \cdot \langle \sigma' \cdot P \rangle \sigma'' \wedge A'' \wedge \langle \sigma \cdot Q \rangle \sigma'' \\ \Rightarrow & \exists \sigma'' \cdot \langle \sigma' \cdot P \rangle \sigma'' \wedge \langle \sigma \cdot Q \rangle \sigma'' \\ = & P \cdot Q \end{aligned}$$

discharge
specialize