

231 (longest plateau) You are given a nonempty sorted list of numbers. A plateau is a segment (sublist of consecutive items) of equal items. Write a program to find

- (a) the length of a longest plateau.
- (b) the number of longest plateaus.

After trying the question, scroll down to the solution.

(a) the length of a longest plateau.

Let the list be L . Let $P i j$ mean that $L[i..j]$ is a plateau in $L[0..k]$. Formally,

$$P = \langle i, j \mid 0 \leq i \leq j \leq \#L \wedge \forall l: i..j \cdot L[i..j] = L[l] \rangle$$

Let Q say that $p = (\text{the length of a longest plateau in } L[0..k])$. Formally,

$$Q = (\exists i, j \cdot P i j \wedge p=j-i) \wedge (\forall i, j \cdot P i j \Rightarrow p \geq j-i)$$

The desired result is that $p' = (\text{the length of a longest plateau in } L)$. Let

$$R = Q' \wedge k=\#L$$

Then R implies the desired result. Now we can refine.

$$R \Leftarrow p := 1. k := 1. Q \Rightarrow R$$

$$Q \Rightarrow R \Leftarrow \text{if } k=\#L \text{ then } ok \text{ else } Q \wedge k < \#L \Rightarrow R \text{ fi}$$

$$Q \wedge k < \#L \Rightarrow R \Leftarrow \text{if } L(k-p) = L[k] \text{ then } Q \wedge k < \#L \wedge L(k-p) = L[k] \Rightarrow R \\ \text{else } Q \wedge k < \#L \wedge L(k-p) \neq L[k] \Rightarrow R \text{ fi}$$

$$Q \wedge k < \#L \wedge L(k-p) = L[k] \Rightarrow R \Leftarrow p := p+1. k := k+1. Q \Rightarrow R$$

$$Q \wedge k < \#L \wedge L(k-p) \neq L[k] \Rightarrow R \Leftarrow k := k+1. Q \Rightarrow R$$

We are finished, but we can do better. We re-refine one specification.

$$Q \wedge k < \#L \wedge L(k-p) = L[k] \Rightarrow R \Leftarrow p := p+1. k := k+1. Q \wedge L(k-p) = L(k-1) \Rightarrow R$$

$$Q \wedge L(k-p) = L(k-1) \Rightarrow R \Leftarrow$$

$$\text{if } k=\#L \text{ then } ok \text{ else } Q \wedge k < \#L \wedge L(k-p) = L(k-1) \Rightarrow R \text{ fi}$$

$$Q \wedge k < \#L \wedge L(k-p) = L(k-1) \Rightarrow R \Leftarrow$$

$$\text{if } L(k-p) = L[k] \text{ then } Q \wedge k < \#L \wedge L(k-p) = L[k] \Rightarrow R$$

$$\text{else } Q \wedge k < \#L \wedge L(k-p) = L(k-1) \neq L[k] \Rightarrow R \text{ fi}$$

$$Q \wedge k < \#L \wedge L(k-p) = L(k-1) \neq L[k] \Rightarrow R \Leftarrow$$

$$\text{if } k+p \geq \#L \text{ then } ok$$

$$\text{else } k := k+p. Q \wedge k < \#L \Rightarrow R \text{ fi}$$

We can step ahead p places because in a sorted list, there cannot be two separate plateaus of the same item.

(b) the number of longest plateaus.

no solution given