What is the difference between $\#[n^\times \top]$ and $\varphi[n^\times \top]$?

None. $\#[n^\times \top] = \varphi[n^\times \top] = n$. 