What is the difference between $\#[n^* \top] \text{ and } \varepsilon\{n^* \top\}$?

None. $\#[n^* \top] = \varepsilon\{n^* \top\} = n$. 