

bunch

set

string

list

bunch

unpackaged

unindexed

set

string

list

bunch

unpackaged

unindexed

set

packaged

unindexed

string

list

bunch	unpackaged	unindexed
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set	packaged	unindexed
------------	----------	-----------

string	unpackaged	indexed
---------------	------------	---------

list

bunch	unpackaged	unindexed
set	packaged	unindexed
string	unpackaged	indexed
list	packaged	indexed

Bunch Theory

Bunches can be used to represent collections.

Bunch Theory

Bunches can be used to represent collections.

1, 3, 7

Bunch Theory

Bunches can be used to represent collections.

1, 3, 7 \top , \perp , 5, “a”

Bunch Theory

Bunches can be used to represent collections.

1, 3, 7 $\top, \perp, 5, \text{“a”}$ 2

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1, 3, 7



\top , \perp , 5, “a”

2

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1, 3, 7

\top , \perp , 5, "a"

2



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1, 3, 7

\top , \perp , 5, “a”

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1, 3, 7 \top , \perp , 5, “a” 2

Any number, character, binary, or set is an **elementary bunch**, or **element**.

Bunch Theory

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A, B union

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A, B union

$A \text{ ‘ } B$ intersection

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1, 3, 7 $\top, \perp, 5, \text{“a”}$ 2

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A, B	union
$A \cap B$	intersection
$\#A$	size, cardinality (number)

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Bunches can be used to represent collections.

1, 3, 7 $\top, \perp, 5, \text{“a”}$ 2

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A, B	union
$A \cap B$	intersection
$\#A$	size, cardinality (number)
$A : B$	inclusion (binary)

Bunch Theory

Bunch Theory

$$1, 3, 7 = 3, 1, 7, 1$$

Bunch Theory

$$1, 3, 7 = 3, 1, 7, 1$$

$$\phi(2) = 1$$

$$\phi(1, 3, 7) = 3$$

Bunch Theory

$$1, 3, 7 = 3, 1, 7, 1$$

$$\phi(2) = 1$$

$$\phi(1, 3, 7) = 3 = \phi(3, 1, 7, 1)$$

Bunch Theory

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$$2: 0, 2, 5, 9$$

Bunch Theory

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$$\phi(1, 3, 7) = 3 = \phi(3, 1, 7, 1)$$

$$2: 0, 2, 5, 9$$

$$2: 2$$

$$2, 9: 0, 2, 5, 9$$

Bunch Theory

axioms

$x: y = x=y$	elementary axiom
$x: A, B = x: A \vee x: B$	compound axiom
$A, A = A$	idempotence
$A, B = B, A$	symmetry
$A, (B, C) = (A, B), C$	associativity
$A' A = A$	idempotence
$A' B = B' A$	symmetry
$A' (B' C) = (A' B)' C$	associativity
$A, B: C = A: C \wedge B: C$	antidistributivity
$A: B' C = A: B \wedge A: C$	distributivity
$A: A, B$	generalization
$A' B: A$	specialization

Bunch Theory

axioms

\rightarrow	$x: y = x=y$	elementary axiom
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	$A' (B' C) = (A' B)' C$	associativity
	$A, B: C = A: C \wedge B: C$	antidistributivity
	$A: B' C = A: B \wedge A: C$	distributivity
	$A: A, B$	generalization
	$A' B: A$	specialization

Bunch Theory

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idempotence

$$A, B = B, A$$

symmetry

$$A, (B, C) = (A, B), C$$

associativity

$$A' A = A$$

idempotence

$$A' B = B' A$$

symmetry

$$A' (B' C) = (A' B)' C$$

associativity

$$A, B: C = A: C \wedge B: C$$

antidistributivity

$$A: B' C = A: B \wedge A: C$$

distributivity

$$A: A, B$$

generalization

$$A' B: A$$

specialization

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$$A, (B, C) = (A, B), C$$

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$$A: B' C = A: B \wedge A: C$$

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$$A: A, B$$

generalization

$$A' B: A$$

specialization

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$$x: A, B = x: A \vee x: B$$

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$$\rightarrow A, B = B, A$$

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$$A, (B, C) = (A, B), C$$

associativity

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$$A' B = B' A$$

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associativity

$$A, B: C = A: C \wedge B: C$$

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$$A: B' C = A: B \wedge A: C$$

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$$A: A, B$$

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$$\rightarrow A, (B, C) = (A, B), C$$

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$$A' A = A$$

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symmetry

$$A' (B' C) = (A' B)' C$$

associativity

$$A, B: C = A: C \wedge B: C$$

antidistributivity

$$A: B' C = A: B \wedge A: C$$

distributivity

$$A: A, B$$

generalization

$$A' B: A$$

specialization

Bunch Theory

axioms

Bunch Theory

axioms

$A: A$	reflexivity
$A: B \wedge B: A = A=B$	antisymmetry
$A: B \wedge B: C \Rightarrow A: C$	transitivity
$\phi x = 1$	size
$\phi(A,B) + \phi(A' B) = \phi A + \phi B$	size
$\neg x: A \Rightarrow \phi(A' x) = 0$	size
$A: B \Rightarrow \phi A \leq \phi B$	size

Bunch Theory

axioms

→	$A: A$	reflexivity
→	$A: B \wedge B: A = A=B$	antisymmetry
→	$A: B \wedge B: C \Rightarrow A: C$	transitivity
	$\wp x = 1$	size
	$\wp(A,B) + \wp(A' B) = \wp A + \wp B$	size
	$\neg x: A \Rightarrow \wp(A' x) = 0$	size
	$A: B \Rightarrow \wp A \leq \wp B$	size

Bunch Theory

Bunch Theory

laws

$A, (A' B) = A$	absorption
$A' (A, B) = A$	absorption
$A: B \Rightarrow C, A: C, B$	monotonicity
$A: B \Rightarrow C' A: C' B$	monotonicity
$A: B = A, B = B = A = A' B$	inclusion
$A, (B, C) = (A, B), (A, C)$	distributivity
$A, (B' C) = (A, B)' (A, C)$	distributivity
$A' (B, C) = (A' B), (A' C)$	distributivity
$A' (B' C) = (A' B)' (A' C)$	distributivity
$A: B \wedge C: D \Rightarrow A, C: B, D$	conflation
$A: B \wedge C: D \Rightarrow A' C: B' D$	conflation

Bunch Theory

laws

$$A,(A'B) = A$$

absorption

$$A'(A,B) = A$$

absorption

$$\rightarrow A: B \Rightarrow C, A: C, B$$

monotonicity

$$\rightarrow A: B \Rightarrow C'A: C'B$$

monotonicity

$$A: B = A, B = B = A = A'B$$

inclusion

$$A,(B,C) = (A,B),(A,C)$$

distributivity

$$A,(B'C) = (A,B)'(A,C)$$

distributivity

$$A'(B,C) = (A'B), (A'C)$$

distributivity

$$A'(B'C) = (A'B)'(A'C)$$

distributivity

$$A: B \wedge C: D \Rightarrow A, C: B, D$$

conflation

$$A: B \wedge C: D \Rightarrow A'C: B'D$$

conflation

Bunch Theory

Bunch Theory

<i>null</i>			the empty bunch
<i>bin</i>	=	\top, \perp	the binary values
<i>nat</i>	=	$0, 1, 2, \dots$	the natural numbers
<i>int</i>	=	$\dots, -2, -1, 0, 1, 2, \dots$	the integer numbers
<i>rat</i>	=	$\dots, -1, 0, 2/3, \dots$	the rational numbers
<i>real</i>	=	$\dots, 2^{1/2}, \dots$	the real numbers
<i>xnat</i>	=	$0, 1, 2, \dots, \infty$	the extended natural numbers
<i>xint</i>	=	$-\infty, \dots, -2, -1, 0, 1, 2, \dots, \infty$	the extended integer numbers
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<i>xreal</i>	=	$-\infty, \dots, \infty$	the extended real numbers
<i>char</i>	=	$\dots, \text{"a"}, \text{"A"}, \dots$	the character values


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Bunch Theory

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	<i>real</i>	=	..., $2^{1/2}$, ...	the real numbers
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 <i>char</i>	=	$\dots, \text{"a"}, \text{"A"}, \dots$	the character values

Bunch Theory

$x,..y$

Bunch Theory

$x..y$ “ x to y ”

Bunch Theory

$x..y$ “ x to y ” for $x \leq y$

Bunch Theory

$x,..y$

Bunch Theory

$$i: x, ..y \quad = \quad x \leq i < y$$

Bunch Theory

$$i: x,..y = x \leq i < y$$

$$\phi(x,..y) = y-x$$

Bunch Theory

$$i: x,..y = x \leq i < y$$

$$\phi(x,..y) = y-x$$

$$0,..3 = 0, 1, 2$$

Bunch Theory

$$i: x,..y = x \leq i < y$$

$$\phi(x,..y) = y-x$$

$$0,..3 = 0, 1, 2$$

$$0,..2 = 0, 1$$

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$$\phi(x,..y) = y-x$$

$$0,..3 = 0, 1, 2$$

$$0,..2 = 0, 1$$

$$0,..1 = 0$$

Bunch Theory

$$i: x,..y \quad = \quad x \leq i < y$$

$$\phi(x,..y) \quad = \quad y-x$$

$$0,..3 \quad = \quad 0, 1, 2$$

$$0,..2 \quad = \quad 0, 1$$

$$0,..1 \quad = \quad 0$$

$$0,..0 \quad = \quad \textit{null}$$

Bunch Theory

$$i: x,..y = x \leq i < y$$

$$\#(x,..y) = y-x$$

$$0,..3 = 0, 1, 2$$

$$0,..2 = 0, 1$$

$$0,..1 = 0$$

$$0,..0 = \textit{null}$$

$$0,..∞ = \textit{nat}$$

Bunch Theory

distribution

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

$$\text{null} + 10 =$$

Bunch Theory

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Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

$$\mathit{null} + 10 = \mathit{null}$$

$$\mathit{nat} + 2 = 2, 3, 4, 5, 6, \dots$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

$$\mathit{null} + 10 = \mathit{null}$$

$$\mathit{nat} + 2 = 2, 3, 4, 5, 6, \dots$$

$$\mathit{nat} \times 2 = 0, 2, 4, 6, 8, \dots$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

$$\mathit{null} + 10 = \mathit{null}$$

$$\mathit{nat} + 2 = 2, 3, 4, 5, 6, \dots$$

$$\mathit{nat} \times 2 = 0, 2, 4, 6, 8, \dots$$

$$\mathit{nat}^2 = 0, 1, 4, 9, 16, \dots$$

Bunch Theory

distribution

$$-(1, 3, 7) = -1, -3, -7$$

$$(1, 2) + (10, 20) = 11, 12, 21, 22$$

$$(1, 2) + 10 = 11, 12$$

$$1 + 10 = 11$$

$$\mathit{null} + 10 = \mathit{null}$$

$$\mathit{nat} + 2 = 2, 3, 4, 5, 6, \dots$$

$$\mathit{nat} \times 2 = 0, 2, 4, 6, 8, \dots$$

$$\mathit{nat}^2 = 0, 1, 4, 9, 16, \dots$$

$$2^{\mathit{nat}} = 1, 2, 4, 8, 16, \dots$$

Set Theory

provides nested structure (things within things)

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

1, 3, 7

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

$\{1, 3, 7\}$

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

$\{1, 3, 7\}, 8$

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

$\{\{1, 3, 7\}, 8\}$

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

$\{\{1, 3, 7\}, 8\}$

$\{\text{null}\}$

the empty set

Set Theory

provides nested structure (things within things)

$\{A\}$

“set containing A ”

$\sim S$

“contents of S ”

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size, cardinality

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size, cardinality

$\mathcal{P}(0, 1) = \{\text{null}\}, \{0\}, \{1\}, \{0, 1\}$

power

Set Theory

axioms

$$\{\sim S\} = S$$

$$\sim\{A\} = A$$

$$\{A\} \neq A$$

$$\$\{A\} = \emptyset A$$

$$A \in \{B\} = A: B$$

$$\{A\} \subseteq \{B\} = A: B$$

$$\{A\}: \not\subseteq B = A: B$$

$$\{A\} \cup \{B\} = \{A, B\}$$

$$\{A\} \cap \{B\} = \{A \text{ ' } B\}$$

$$\{A\} = \{B\} = A = B$$

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