## Bayesian Inference about Everything



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## Model Everything

- What is the probability of me (ever) observing a horse that has a horn if unicorns exist?
  - P(I|U) = 0.9 (say)
- What is the probability of me (ever) observing a horse that has a horn if unicorns do not exist?
  - $P(I|\neg U) = 0.0001$  (say)
- How to compute those probabilities?
  - Model everything in the world: the probability that a quantum fluctuation would create an image of a unicorn on my retina (a physical process), the probability that someone would be able to play this prank on me (a sociological process), the probability that I an hallucinating a unicorn (a psychological process)...
  - In practice, just guess

## Prior Beliefs about the World

- What is the probability that unicorns exist?
  - My prior beliefs about the world, before observing the data
  - $P(U) = 10^{-10}$
- Now, having observed a unicorn, what do I think about unicorns?

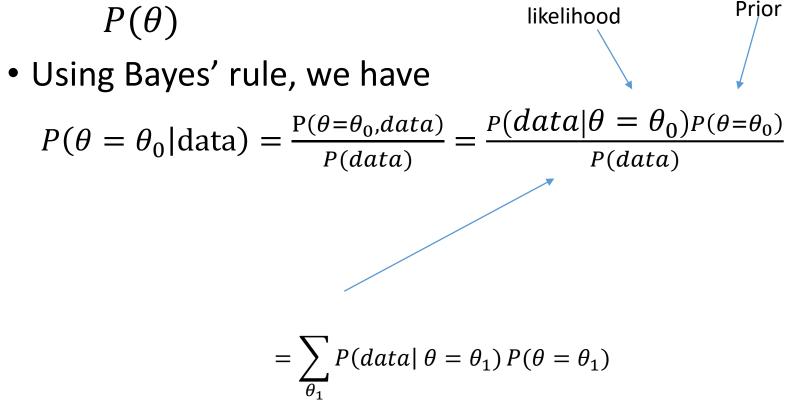
$$P(U|I) = \frac{P(I|U)P(U)}{P(I)} = \frac{P(I|U)P(U)}{P(I|U)P(U) + P(I|\neg U)P(\neg U)}$$

$$=\frac{0.9\times10^{-10}}{0.9\times10^{-10}+0.0001\times(1-10^{-10})}=9\times10^{-7}$$



## Reminder: Unicorns and Stats

 We can encode out beliefs about what the values of the parameters could be using



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