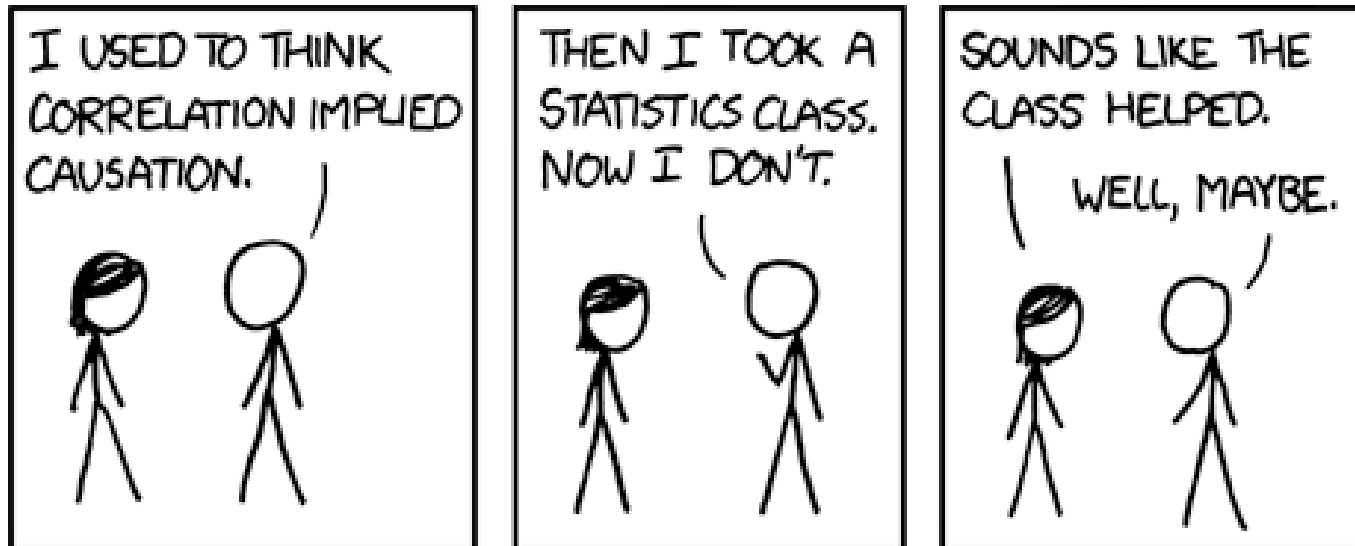
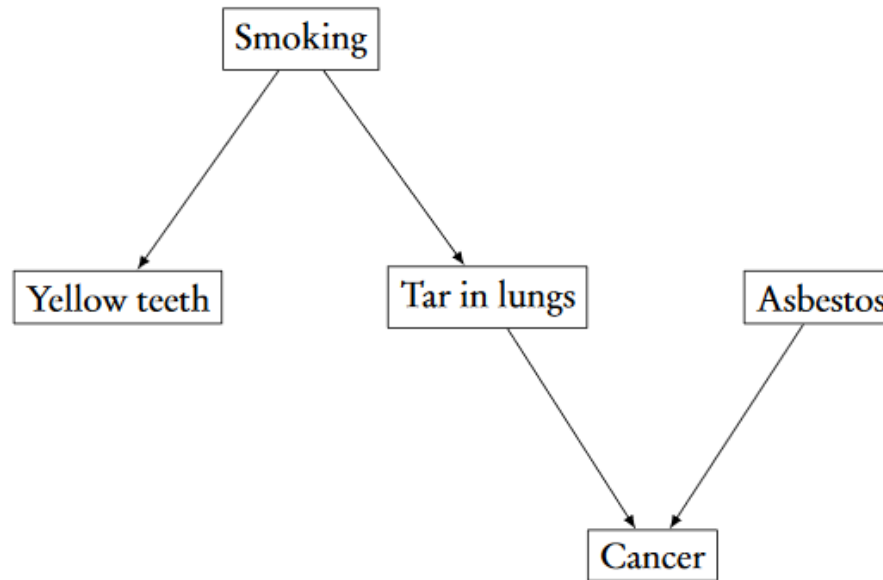


Causal Inference



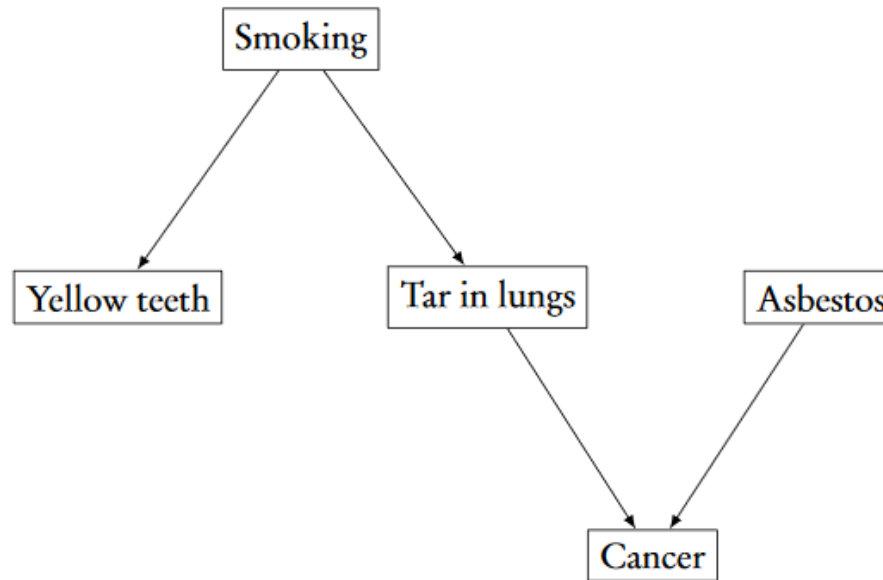
<https://xkcd.com/552/>

Directed Acyclical Graphs (DAG) for representing causal structure



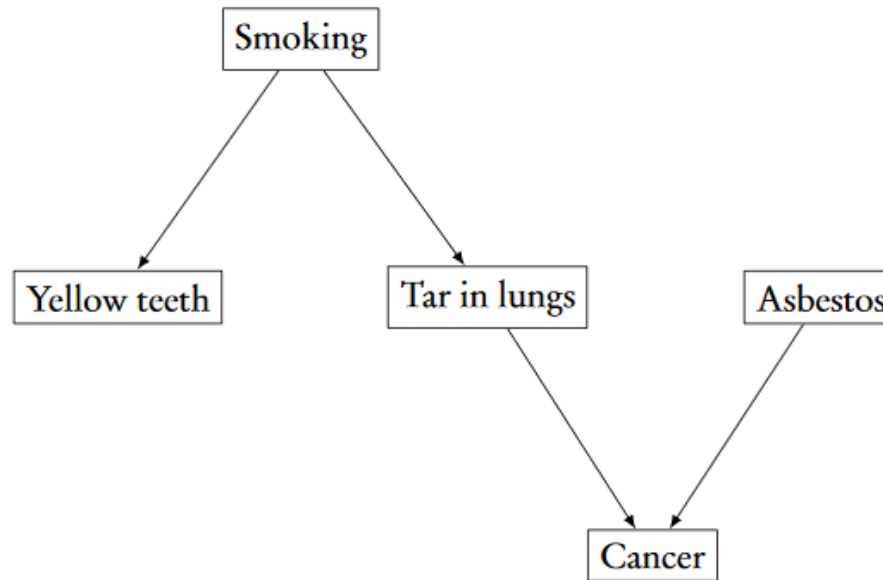
- If we know the value of *Smoking* (0 or 1), we can generate the value of *Yellow teeth* and *Tar in lungs*
- If we know the value of *Tar in lungs* and *Asbestos*, we can generate the value of *Cancer*
- A datapoint is generated by first generating *Smoking* and *Asbestos*, then *Yellow teeth* and *Asbestos*, then *Cancer*

Directed Acyclical Graphs (DAG) for representing causal structure



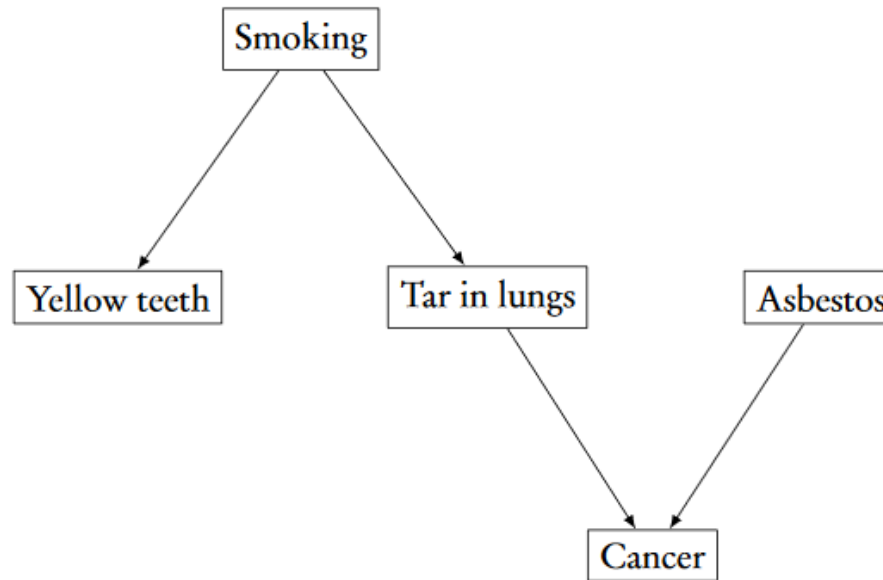
- The graph encodes our knowledge (or assumptions) about the causal structure of the data
- Can help with inference

Directed Acyclical Graphs (DAG) for representing causal structure



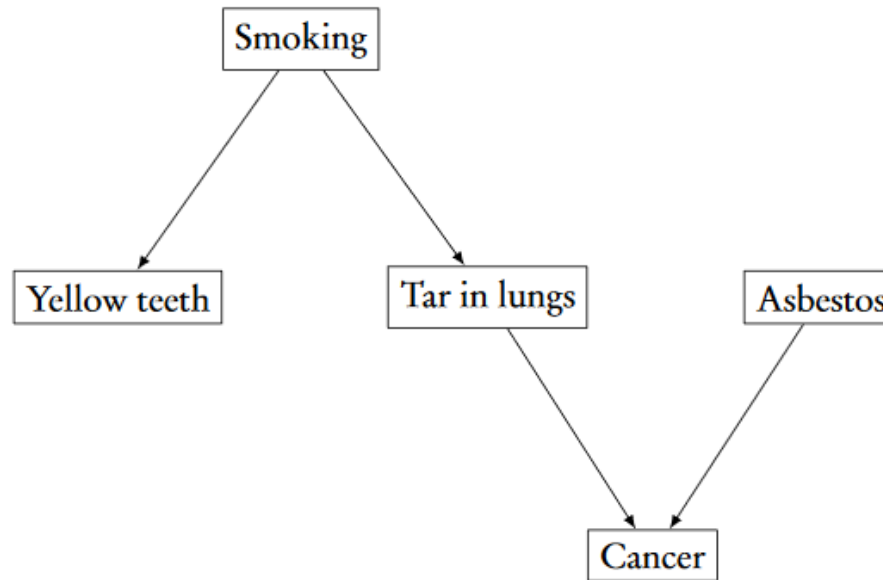
- *Tar* is independent of *Asbestos*
 - They are independently generated
- *Tar* is *not* independent of *Asbestos* given *Cancer*
 - Intuition: if *Cancer* = 1 and *Asbestos* = 1, then *Tar* = 1 is less likely than otherwise, since the cancer is already explained
 - This called “Explaining away”

Directed Acyclical Graphs (DAG) for representing causal structure



- *Yellow teeth* is not indep. of *Tar*
 - Both caused by *Smoking*
- *Yellow teeth* is indep. of *Tar* conditioned on *Smoking*

Directed Acyclical Graphs (DAG) for representing causal structure



- The right way to think of the arrows: *Tar might* cause *Cancer*, or have no effect
- *Smoking is definitely* independent of *Asbestos*

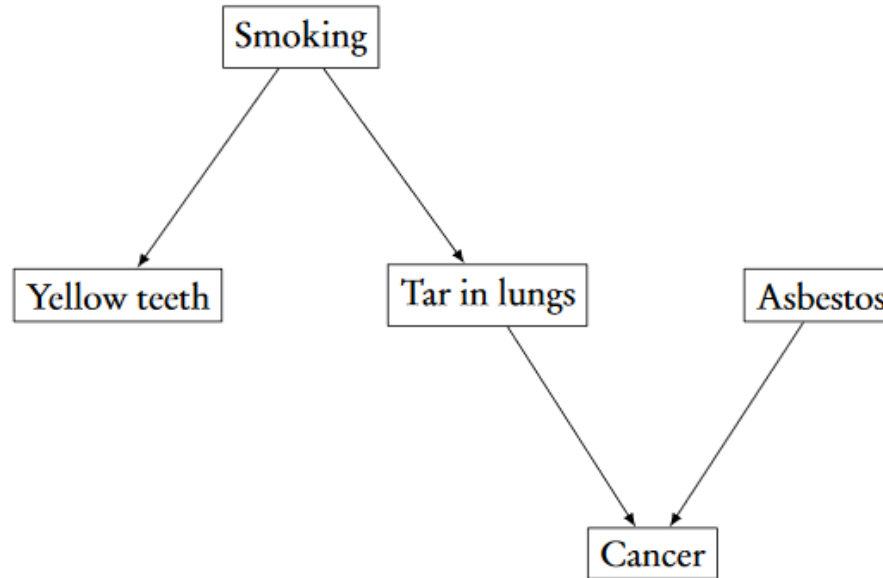
Causation

- Define “A caused B”

Causation

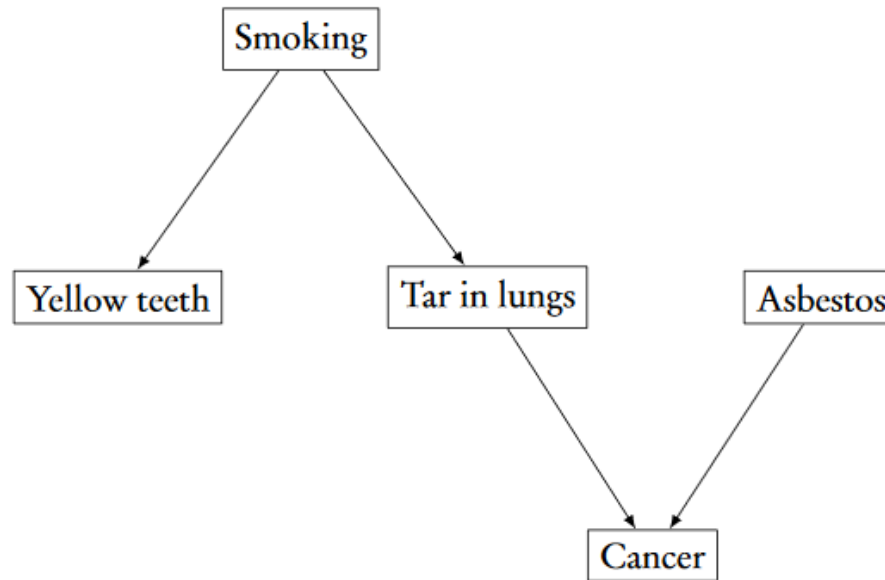
- Counterfactual: we say that A causes B if B *would not have happened* if A had not happened
- Causal inference: trying to answer causal questions from empirical data
 - Difficult to derive counter-factual conclusions from factual premises

Effect of causes



- *What is the causal relationship between exposure to asbestos and yellow teeth?*
 - There is none!
 - *Yellow* and *Asbestos* are not indep. conditioned on *Cancer*
 - Explaining away phenomenon
 - Can predict *Yellow* from $\{Asbestos, Cancer\}$

Effect of causes



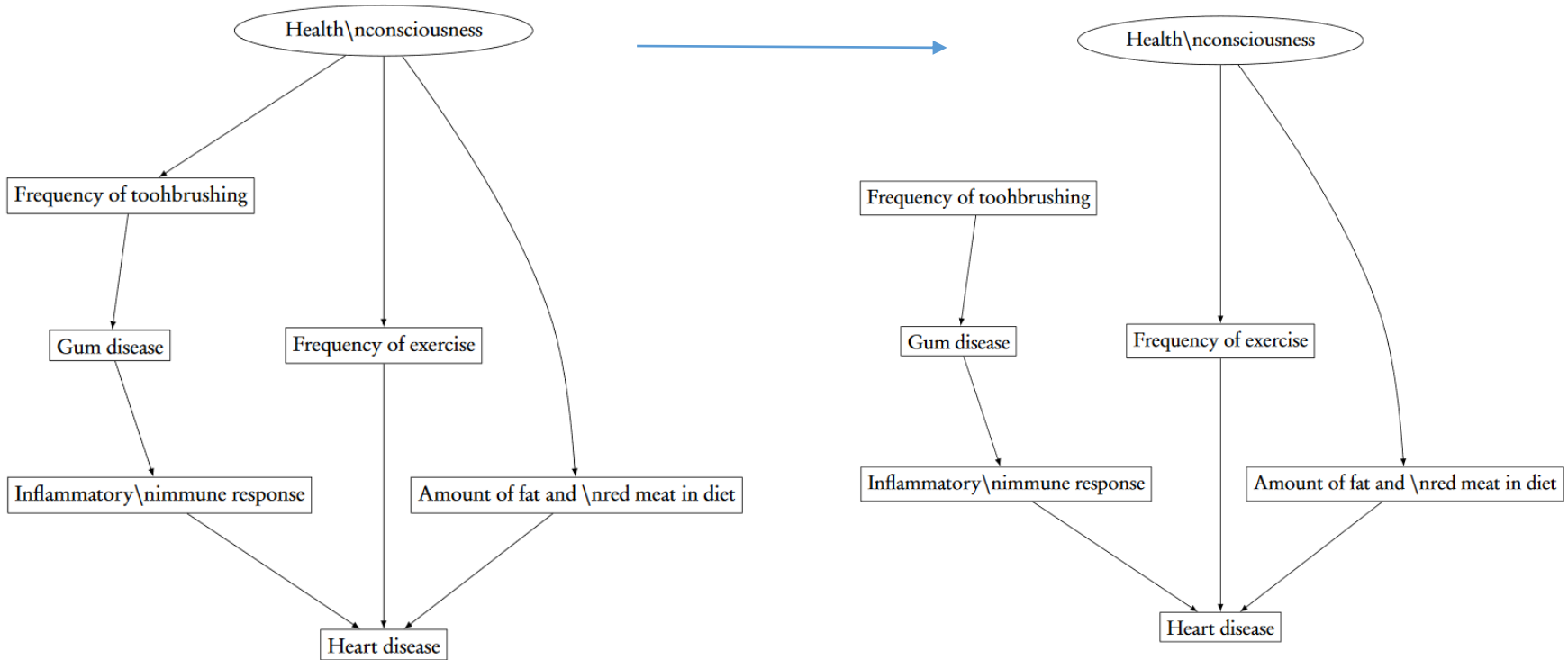
- A way of thinking about this:

$$P(\text{Yellow} | \text{Asbestos} = 1, \text{Cancer} = 1) \neq P(\text{Yellow} | \text{Cancer} = 1)$$

$$P(\text{Yellow} | \text{Asbestos} = 1, \text{do}(\text{Cancer} = 1)) = P(\text{Yellow} | \text{do}(\text{Cancer} = 1)) = P(\text{Yellow})$$

- $\text{do}(\text{Cancer} = 1)$ sets Cancer to 1, and changes the causal graph eliminating the mechanism that generates Cancer

do(brushing)



Again, $P(\text{Heart disease} | \text{Brushing} = b) \neq P(\text{Heart disease} | \text{do}(\text{Brushing} = b))$

Identifying Causal Effects from Observations

- The most straightforward way to compute $P(Y|do(X = x))$ is to manipulate x physically and see what happens to Y
 - Run an experiment
 - Hold all other variables constant
 - Or
 - Randomize all other variables

Identification

- Want to calculate the causal effect of X on Y (i.e., $P(Y|do(X = x))$), but can't run an experiment.
- Can do this if we have the causal graph and observe all the variables
 - Saw this in the toothbrushing example
- Can *sometimes* do this if not all variables are observed
 - Need to carefully look at the graph