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# RelaxedIK: Real-time Synthesis of Accurate and Feasible Robot Arm Motion

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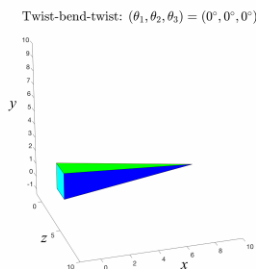
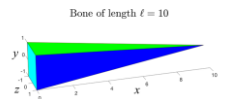
Tingwu Wang

University Of Toronto, CSC-2621, Paper Reading Seminar

# Recap: Forward Kinematics (FK)

## 1. Forward Kinematics

- a. A common robotic skeleton is a tree of rigid bones
- b. The relative Euler angles of all the bones determine the end-effectors
  - i. End-effectors? A tool that's connected to the end of a robot arm



# Recap: Inverse Kinematics (IK)

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## 1. Inverse Kinematics

- a. The indirect control of forward kinematics makes it hard to use in application
  - i. Achieve certain poses?
  - ii. Achieve certain velocities (reward)?
- b. We formulate the inverse kinematics function as:  $\Theta = IK(\mathbf{p})$ , which can be easily written in an analytic form for a simple tree skeleton.
  - i. Pose contains velocity?
  - ii. Hard to find feasible state space?
- c. In reality, IK is often treated as an optimization problem

$$\chi_p(\Theta) = || \mathbf{p}_g - FK(\Theta) ||_2$$



# Imitation Learning

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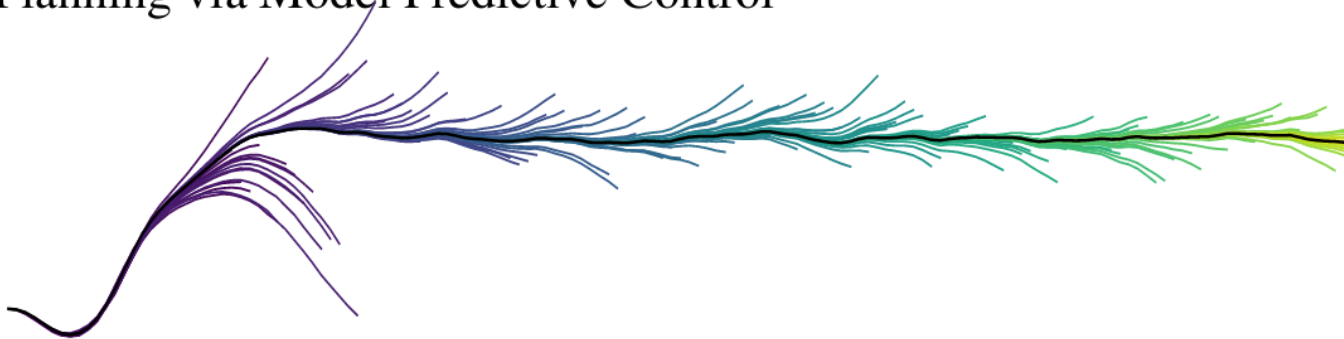
1. Imitation learning has been studied by different communities
  - a. Motion synthesis in character animation?
  - b. Inverse optimal control?
  - c. Imitation learning?

# Imitation Learning

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1. Imitation learning has been studied by different communities
2. Within the focus of this course, people worked on imitation learning using
  - a. Forward dynamics
    - i. Shooting method (optimize the actions)

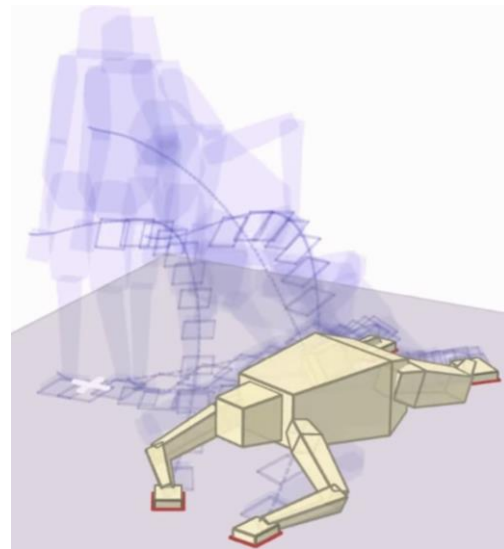
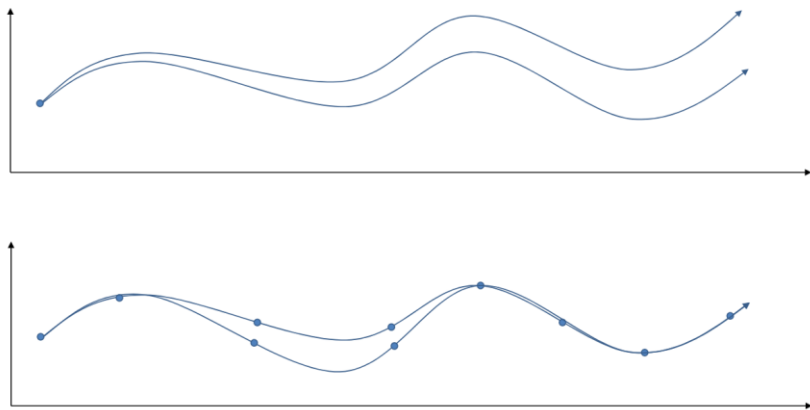
Planning via Model Predictive Control



# Imitation Learning

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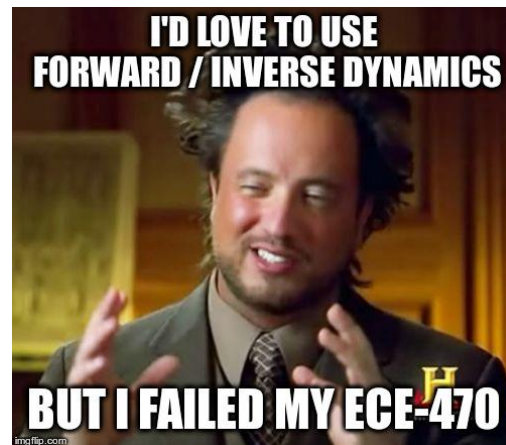
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  - a. Forward dynamics
  - b. Inverse dynamics
    - i. Collocation method (optimize states)



# Imitation Learning

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2. Within the focus of this course, people worked on imitation learning using
  - a. Forward dynamics
    - i. Shooting method
  - b. Inverse dynamics
    - i. Collocation method
  - c. Model-free method
    - i. GAIL
  - d. Motion synthesis with IK
    - i. Today's paper
    - ii. Old school but with new techniques



# Imitation Learning

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1. Imitation learning using IK
  - a. Basic idea: Using IK to bridge between target pose and agent's angles
  - b. Input: M (consecutive) expert (goal) poses
  - c. Output: M (consecutive) frames of agent's euler joints
  - d. Constraints:
    - i. IK constraints (goal constraints)
    - ii. Between-frames constraints
    - iii. Etc.



# Imitation Learning

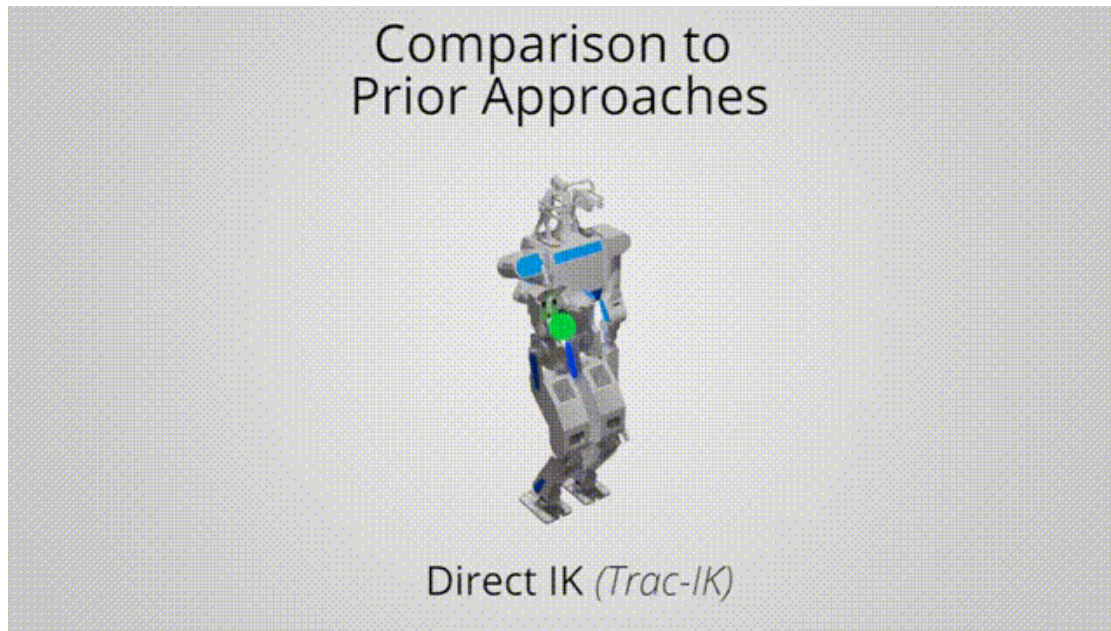
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1. Imitation learning using IK
  - a. Basic idea: minimize the difference of target pose and agent pose
2. Direct point-to-point approach
  - a. TRAC-IK (previous state-of-the-art)
  - b. Pose2pose / frame2frame imitation learning
    - i. Ignore most of the constraints between frames
  - c. Problems
    - i. Self-collision
      1. Time constraints

# Imitation Learning

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## 1. Self-collision



# Imitation Learning

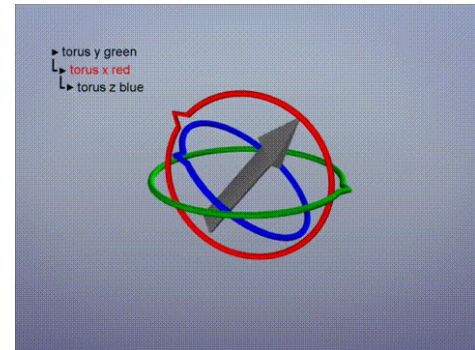
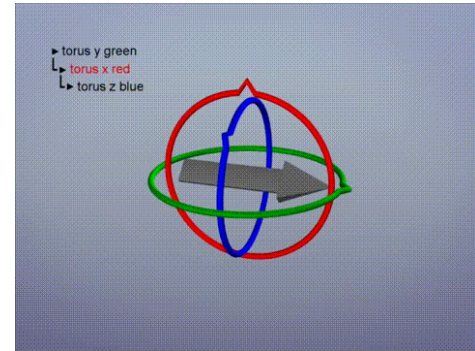
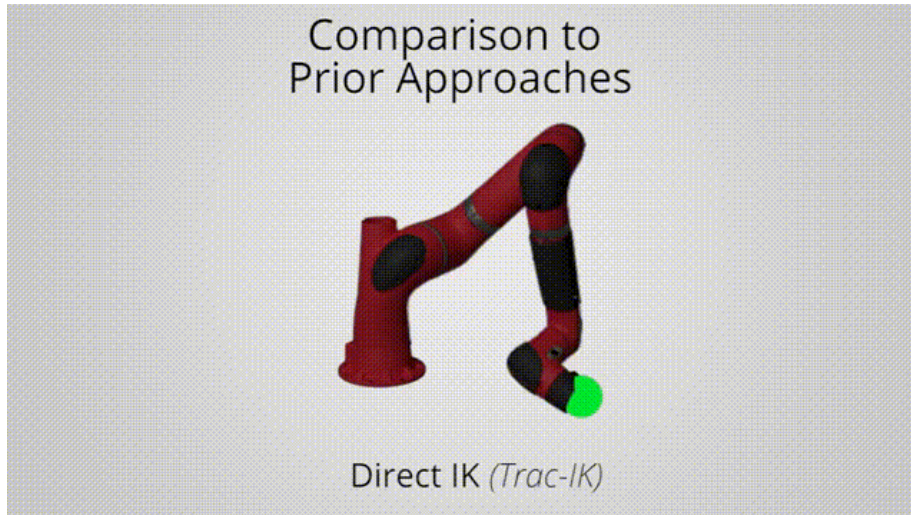
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  - c. Problems
    - i. Self-collision
    - ii. Singularities

# Imitation Learning

## 1. Singularities

- a. E.g. Losing a DoF
- b. Infinite control signals



# Imitation Learning

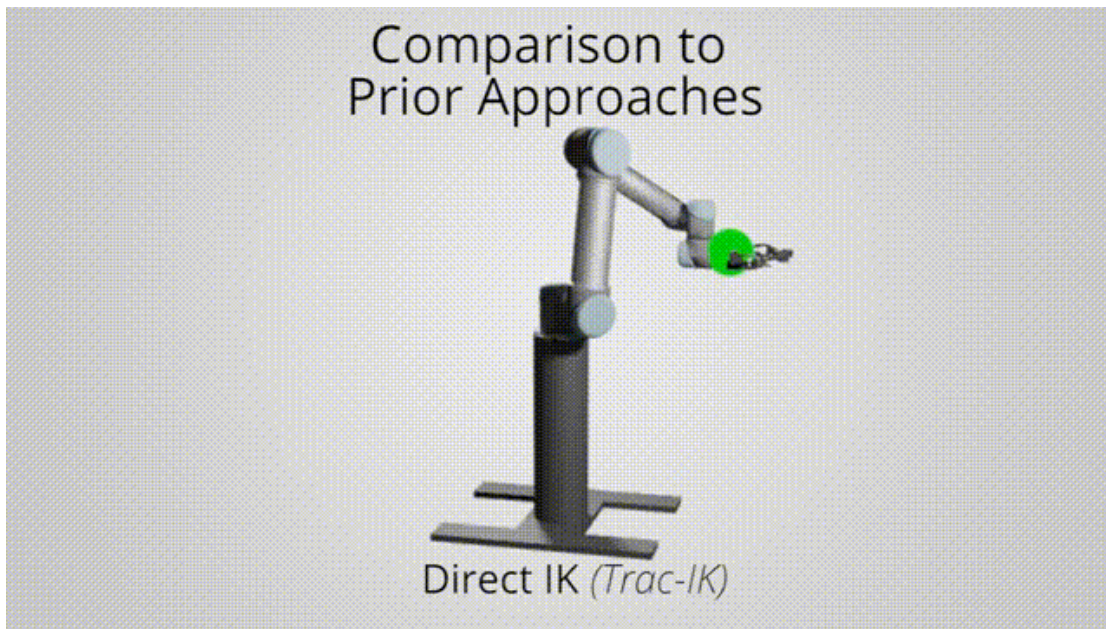
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    - i. Self-collision
    - ii. Singularities
    - iii. Discontinuity

# Imitation Learning

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## 1. Discontinuity



# Imitation Learning

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1. Imitation learning using IK
  - a. Basic idea: minimize the difference of target pose and agent pose
2. Direct point-to-point approach
3. Real-time motion planning approach
  - a. Output the (conservative) solutions real-time
    - i. Always meet the control & collision constraints
    - ii. Soft goal constraints
  - b. Problems
    - i. Goal mistracking



# Imitation Learning

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## 1. Goal mistracking





# Imitation Learning

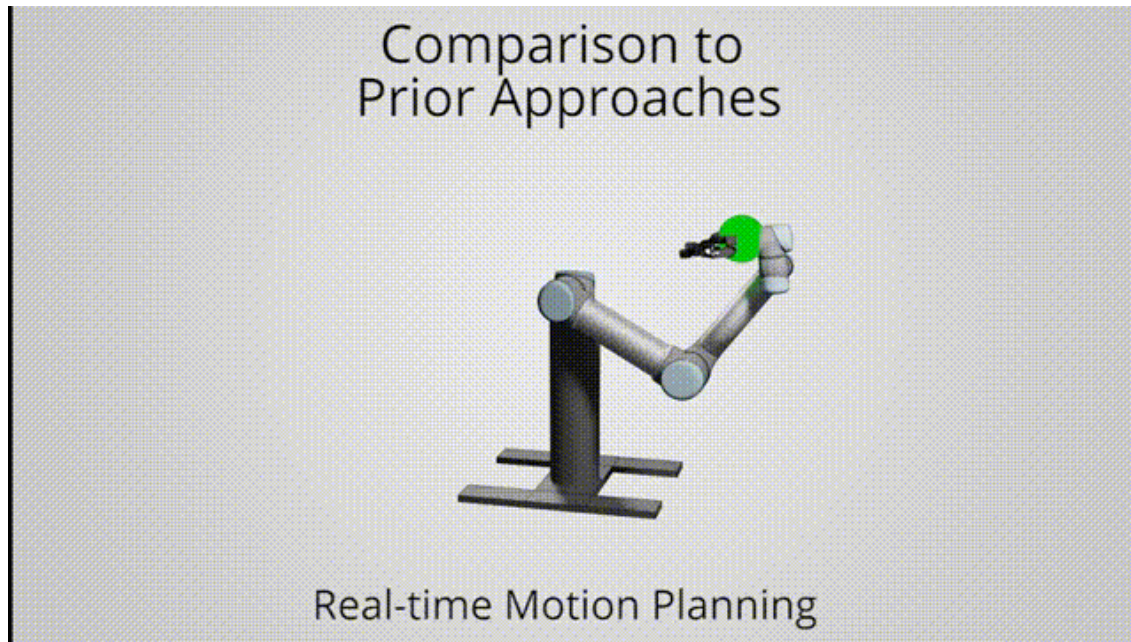
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  - b. Problems
    - i. Goal mistracking
    - ii. Unpredictable behaviors

# Imitation Learning

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1. Unpredictable behaviors



# Relaxed IK

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1. Basic Idea: Using soft (Relaxed) IK loss that considers self-collision and singularity for faster optimization

$$\mathbf{f}(\Theta) = \sum_{i=1}^k w_i f_i(\Theta, \Omega_i)$$

1. Loss functions
  - a. End-effector position & orientation matching
  - b. Minimize joint velocity, acceleration, jerk
  - c. Self-collision loss (fast)
  - d. Singularity loss

# Relaxed IK

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1. Self-collision loss
  - a. Common approach: very slow
  - b. Relaxed IK:
    - i. Approximate how imminent the robot is to a collision state
    - ii. Using simulated data to train a network to predict the distances between links

$$col(\Theta) = \sum_{i,j} b * exp(\frac{-dis(l_i, l_j)^2}{2c^2})$$



# Relaxed IK

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1. Singularity loss
  - a. Kinematic singularities are well studied in robotics
  - b. Relaxed IK:
    - i. Find a metric that can approximate distance to a singularity
    - ii. Jacobian's condition number is used as a proxy distance to singularity
      1. Why?

$$\dot{\mathbf{x}} = \mathbf{J}(\Theta)\dot{\Theta}$$

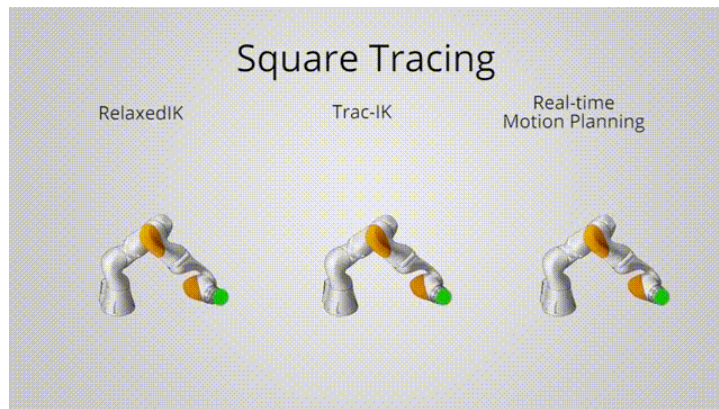
- i. Penalize condition values less than mean - b \* std
  1. Estimate mean, std from simulated data

# Relaxed IK

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## 1. Pros

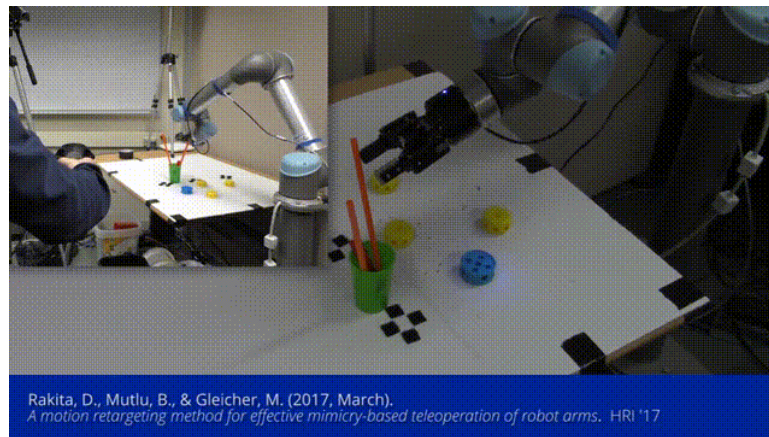
- a. Much faster and smoother performance
  - i. combining neural network and traditional robotics
- b. Data driven, less human-engineering
  - i. Novel singularity metric
- c. Easy to deploy
  - i. Sim2Real



# Relaxed IK

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1. Pros
2. Cons
  - a. No safety / convergence guarantee
  - b. Weak experiments section
    - i. Under-tuned baseline
    - ii. Limited ablation study
  - c. Slower than point2point methods
  - d. Hyper-parameter sensitive



# Q&A

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1. Thanks for listening ;P