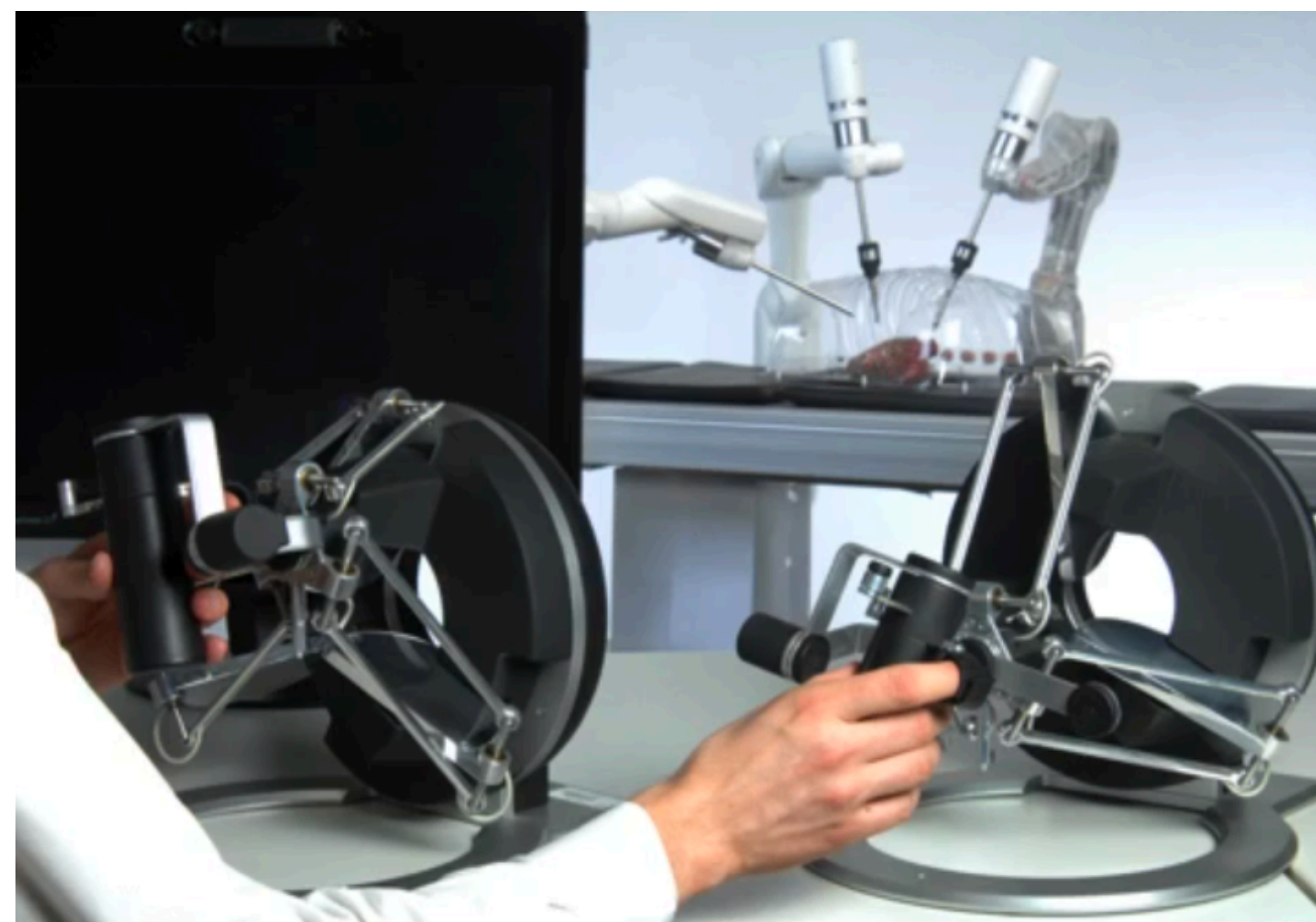
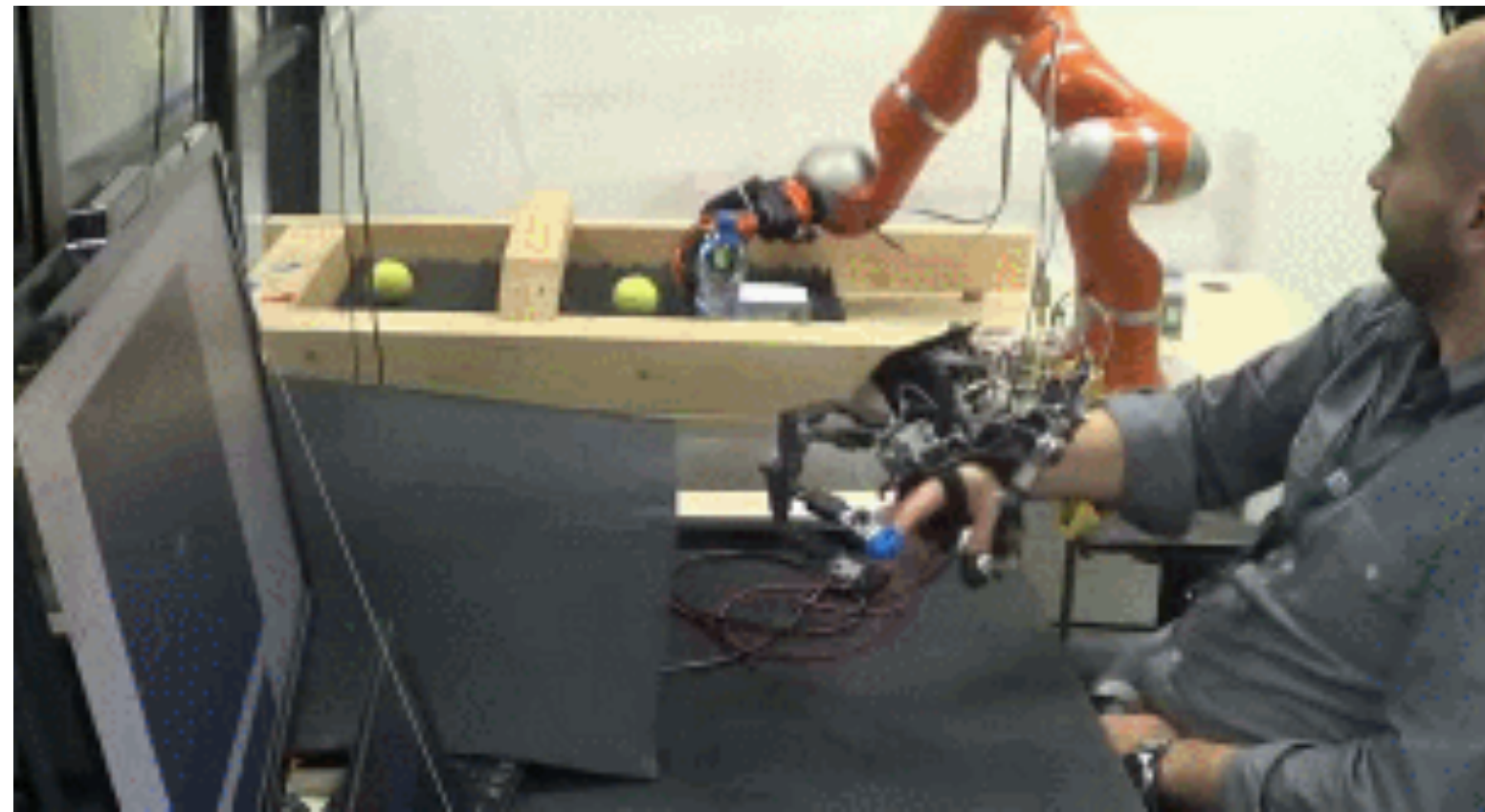


# Shared Autonomy via Hindsight Optimization

Presented by Bin Yang  
22 Feb. 2019



# Teleoperation



**Noisy, insufficient degrees of freedom, tedious**



# Shared Autonomy



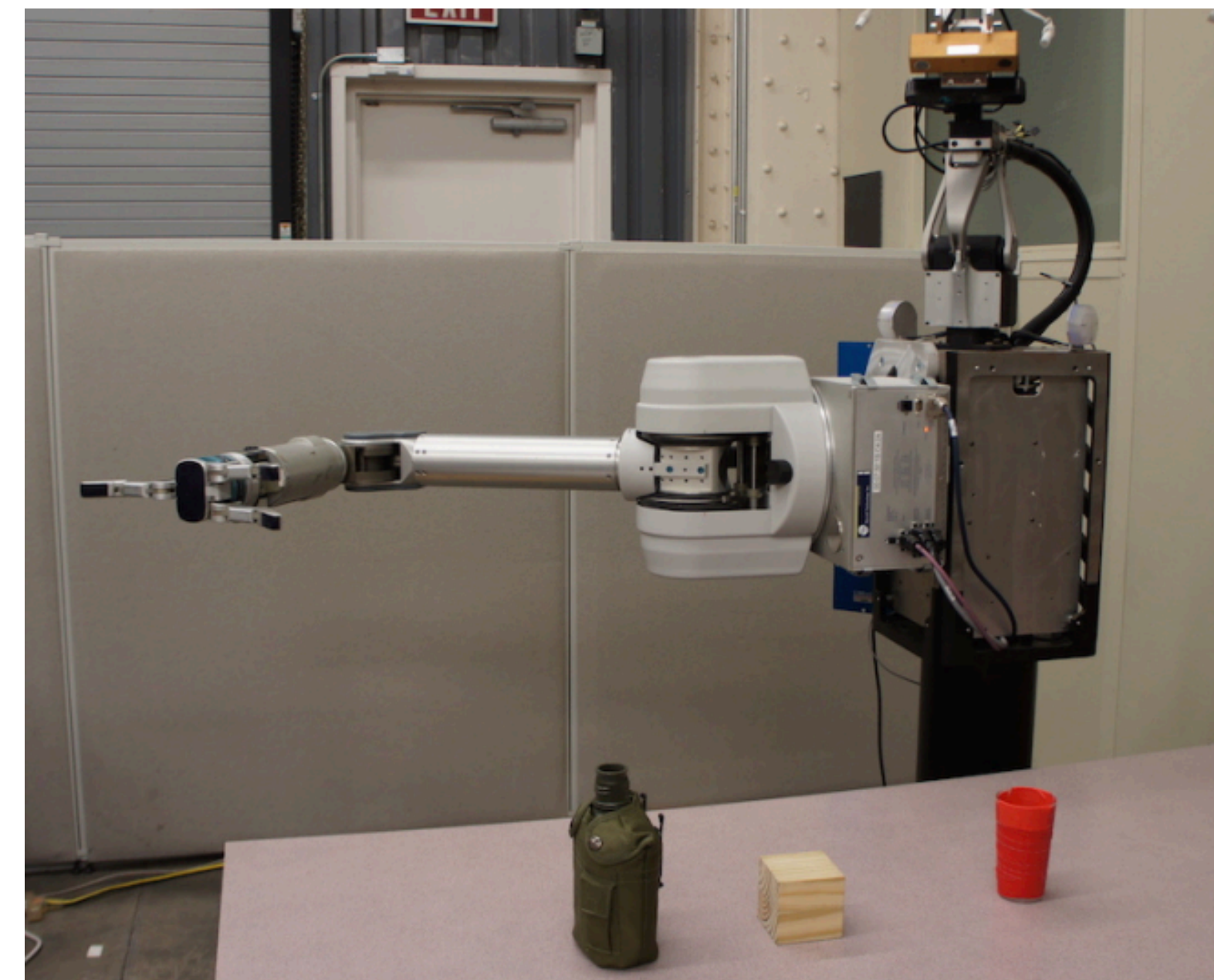
**User Input**

+



**Autonomous Assistance**

=



**Achieve Goal**



# Shared Autonomy



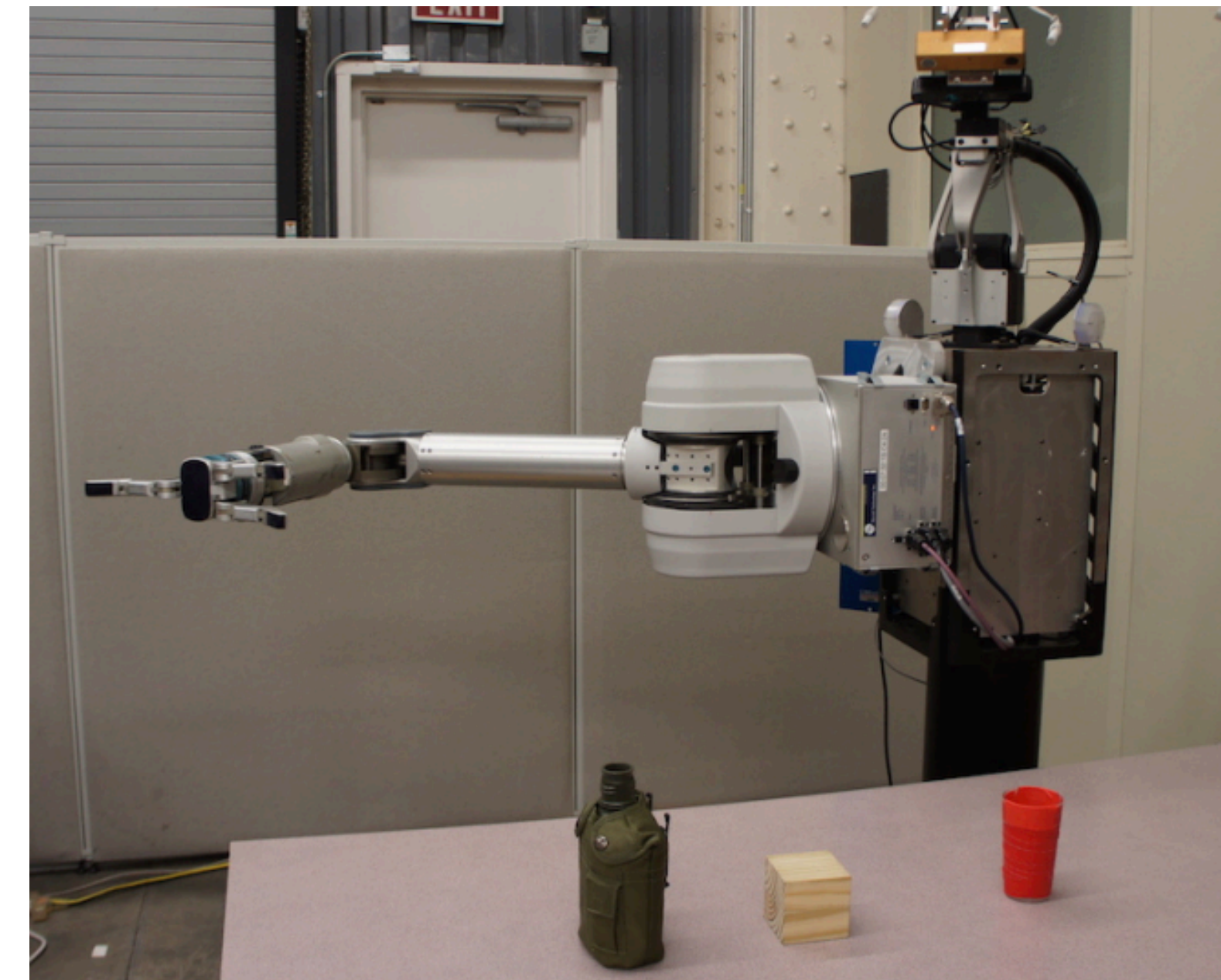
**User Input**

Which goal?

+



=



**Achieve Goal**

**Autonomous Assistance**



# Shared Autonomy

**Predict goal**  
**Assist for single goal**

[Dragan and Srinivasa 13]

[Kofman et al. 05]

[Kragic et al. 05]

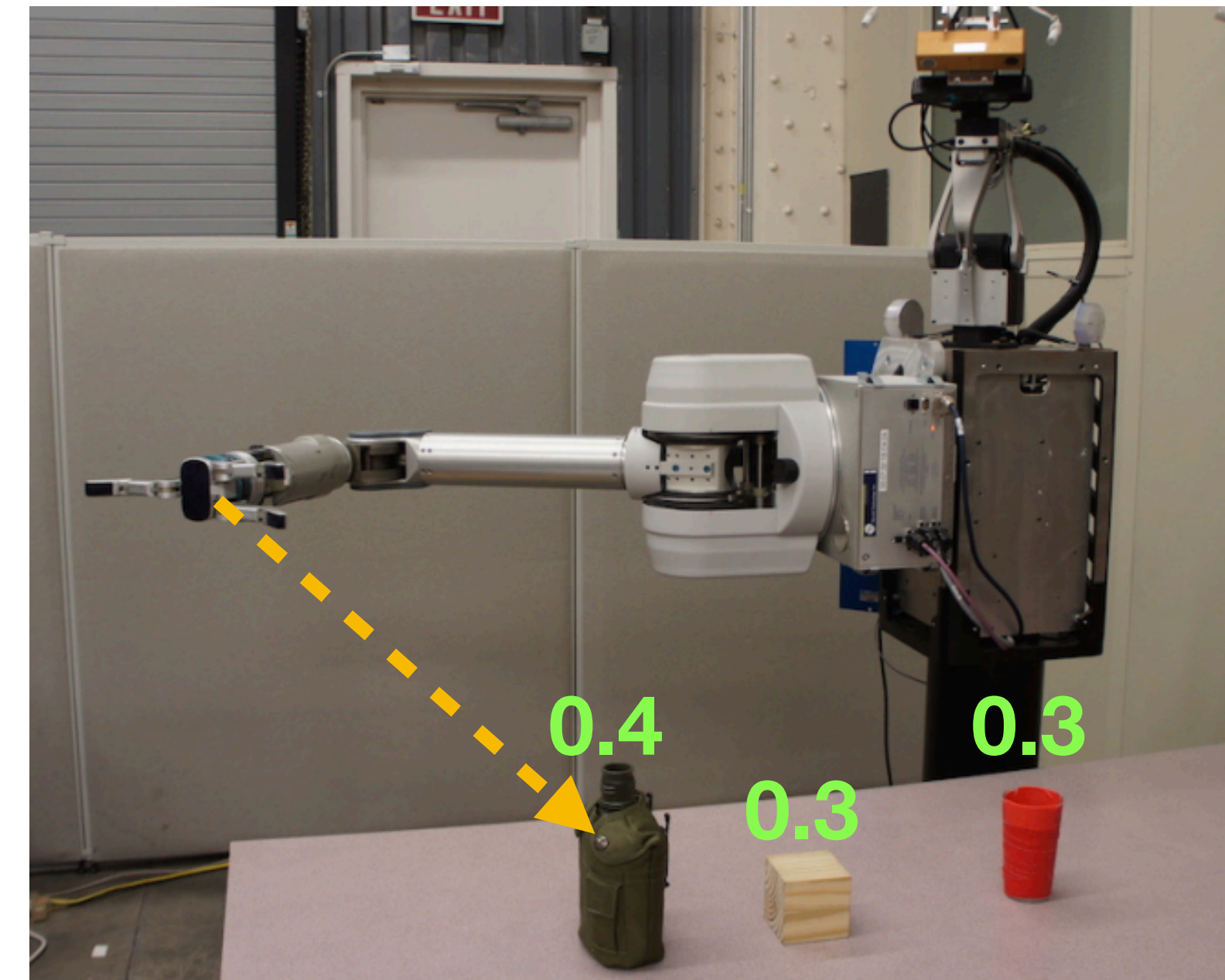
[Yu et al. 05]

[McMullen et al. 14]

...



**Autonomous Assistance**



**Achieve Goal**

# Shared Autonomy

## Predict goal Assist for single goal

[Dragan and Srinivasa 13]  
[Kofman et al. 05]  
[Kragic et al. 05]  
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[McMullen et al. 14]

...

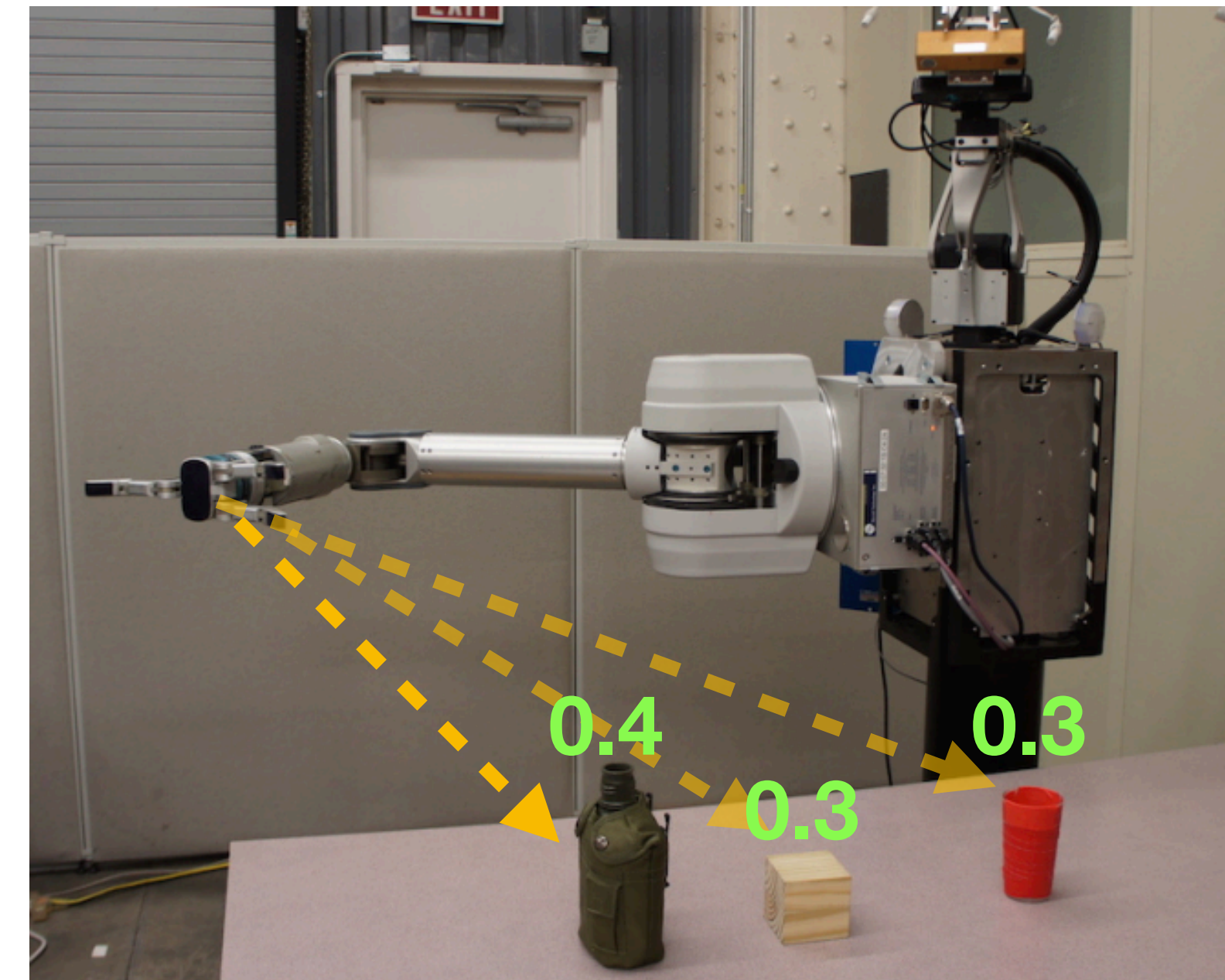
## Predict goal distribution Assist for distribution

[Hauser 13]  
**This work!**

Which goal?



**Autonomous Assistance**

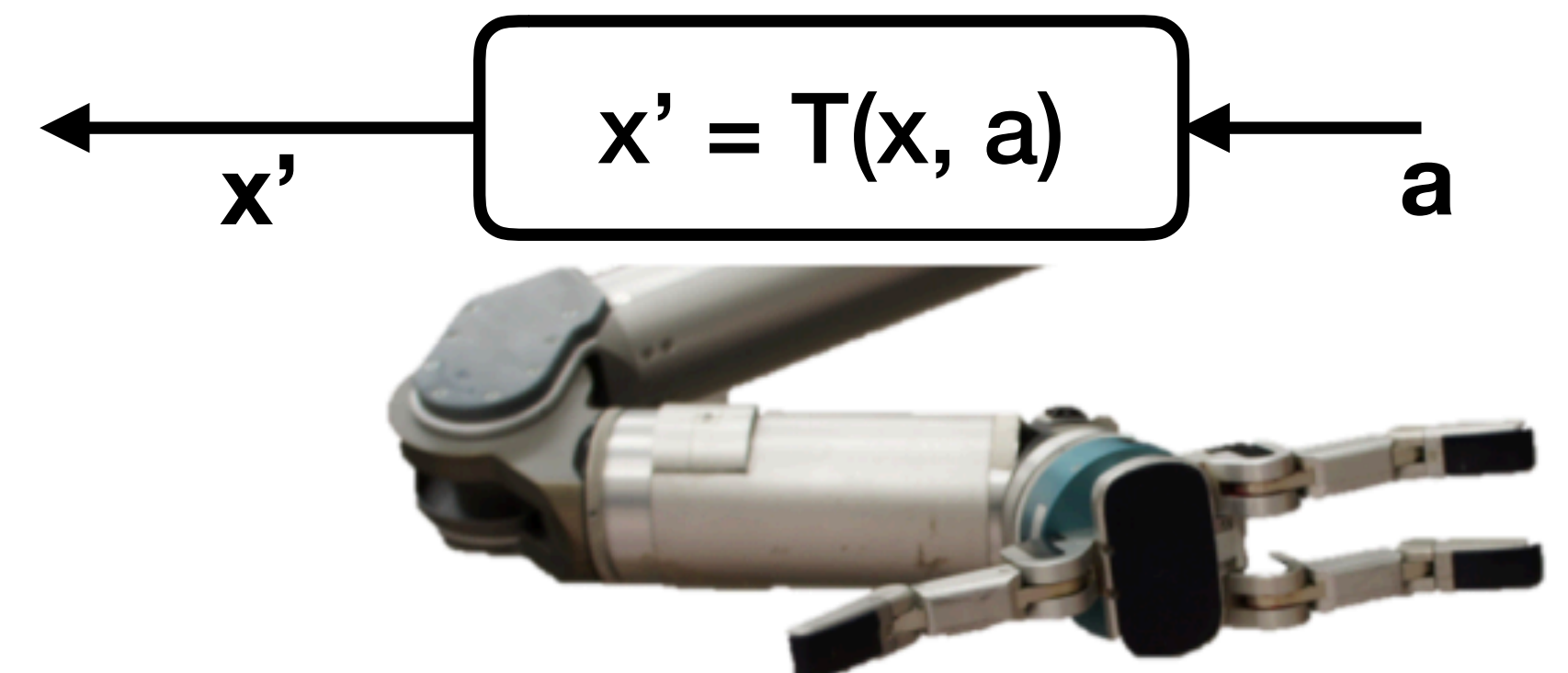


**Achieve Goal**



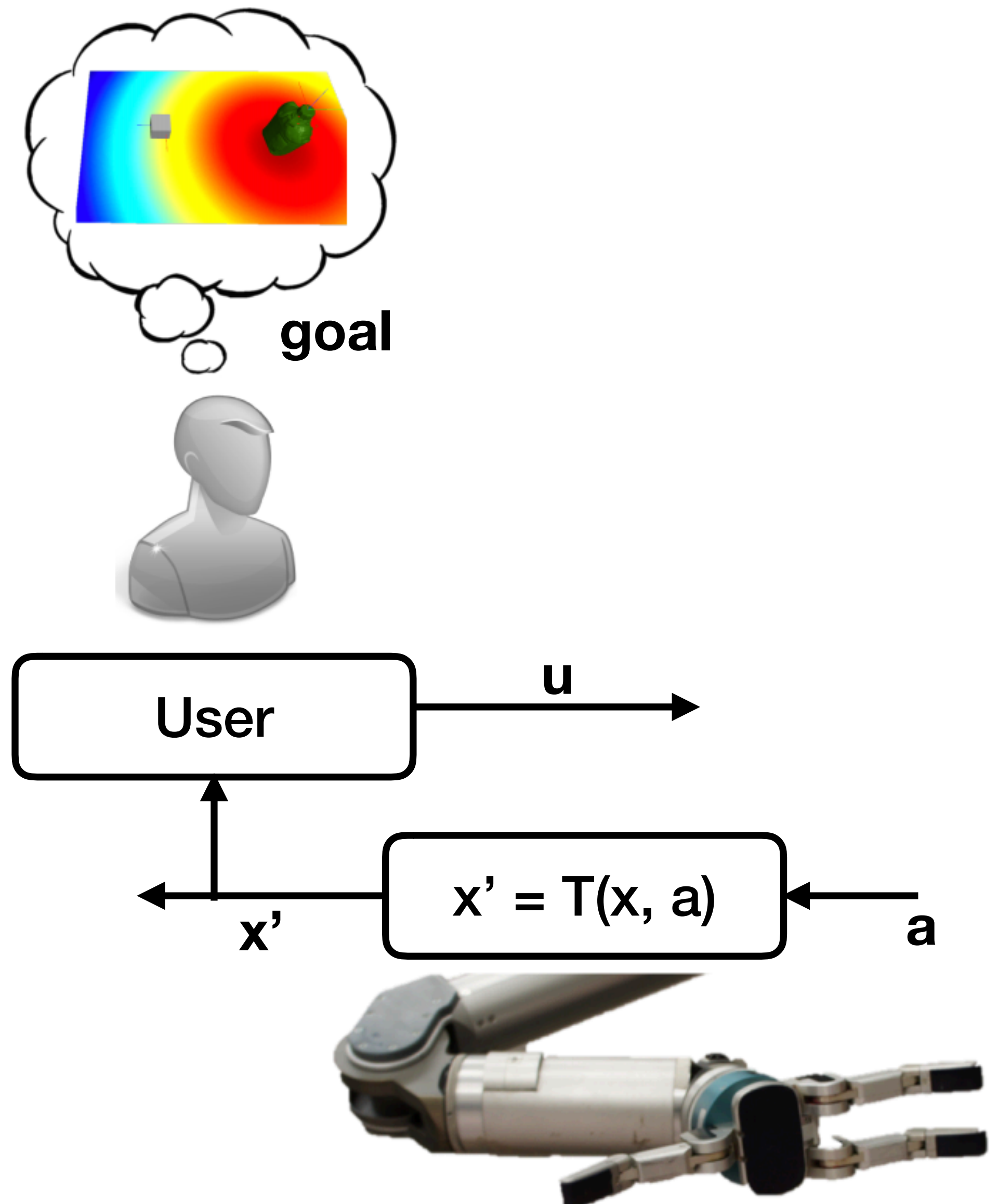
# Method

- System dynamics:  $x' = T(x, a)$



# Method

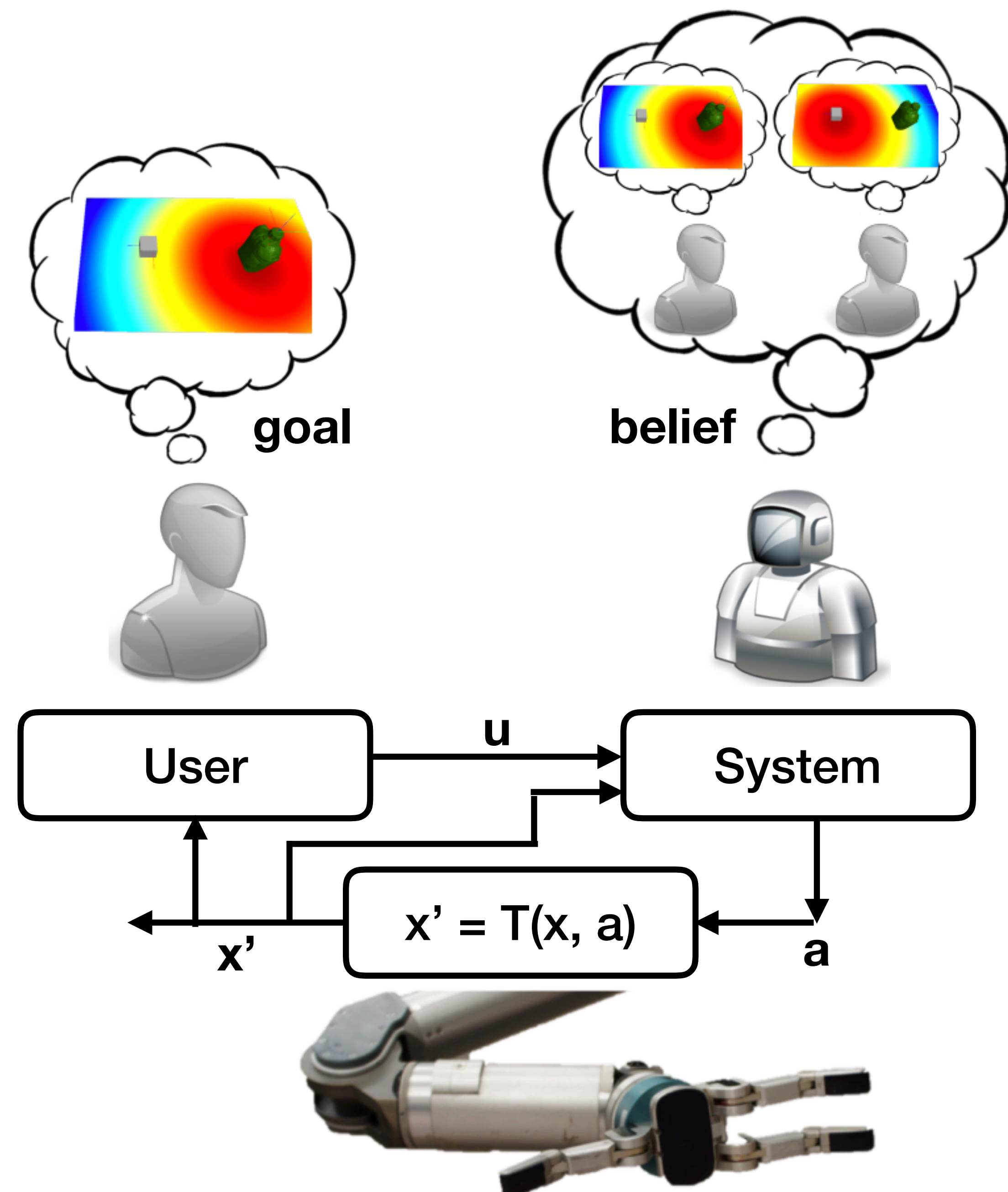
- System dynamics:  $x' = T(x, a)$
- User (MDP) as  $(X, U, T, C_g^{\text{usr}})$ 
  - User policy:  $\pi_g^{\text{usr}}(x) = p(u|x, g)$
  - MaxEnt IOC:  $C_g^{\text{usr}} : X \times U \rightarrow \mathcal{R}$





# Method

- System dynamics:  $x' = T(x, a)$
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    - User policy:  $\pi_g^{\text{usr}}(x) = p(u|x, g)$
    - MaxEnt IOC:  $C_g^{\text{usr}} : X \times U \rightarrow \mathcal{R}$
  - System (POMDP) as  $(S, A, T, C^{\text{rob}}, U, \Omega)$ 
    - Uncertainty over user's goal
    - System state:  $S = X \times G$
    - Observation: user inputs  $U$
    - Observation model  $\Omega$
- $$p(g|\xi^{0 \rightarrow t}) = \frac{p(\xi^{0 \rightarrow t}|g)p(g)}{\sum_{g'} p(\xi^{0 \rightarrow t}|g')p(g')}$$
- Cost function  $C^{\text{rob}} : S \times A \times U \rightarrow \mathcal{R}$





# Hindsight Optimization

- MDP solution:

$$V^{\pi^r}(s) = \mathbb{E} \left[ \sum_t C^r(s_t, u_t, a_t) \mid s_0 = s \right]$$

$$V^*(s) = \min_{\pi^r} V^{\pi^r}(s)$$



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$$\begin{aligned} V^{\text{HS}}(b) &= \mathbb{E}_b \left[ \min_{\pi^r} V^{\pi^r}(s) \right] \\ &= \mathbb{E}_g[V_g(x)] \end{aligned}$$



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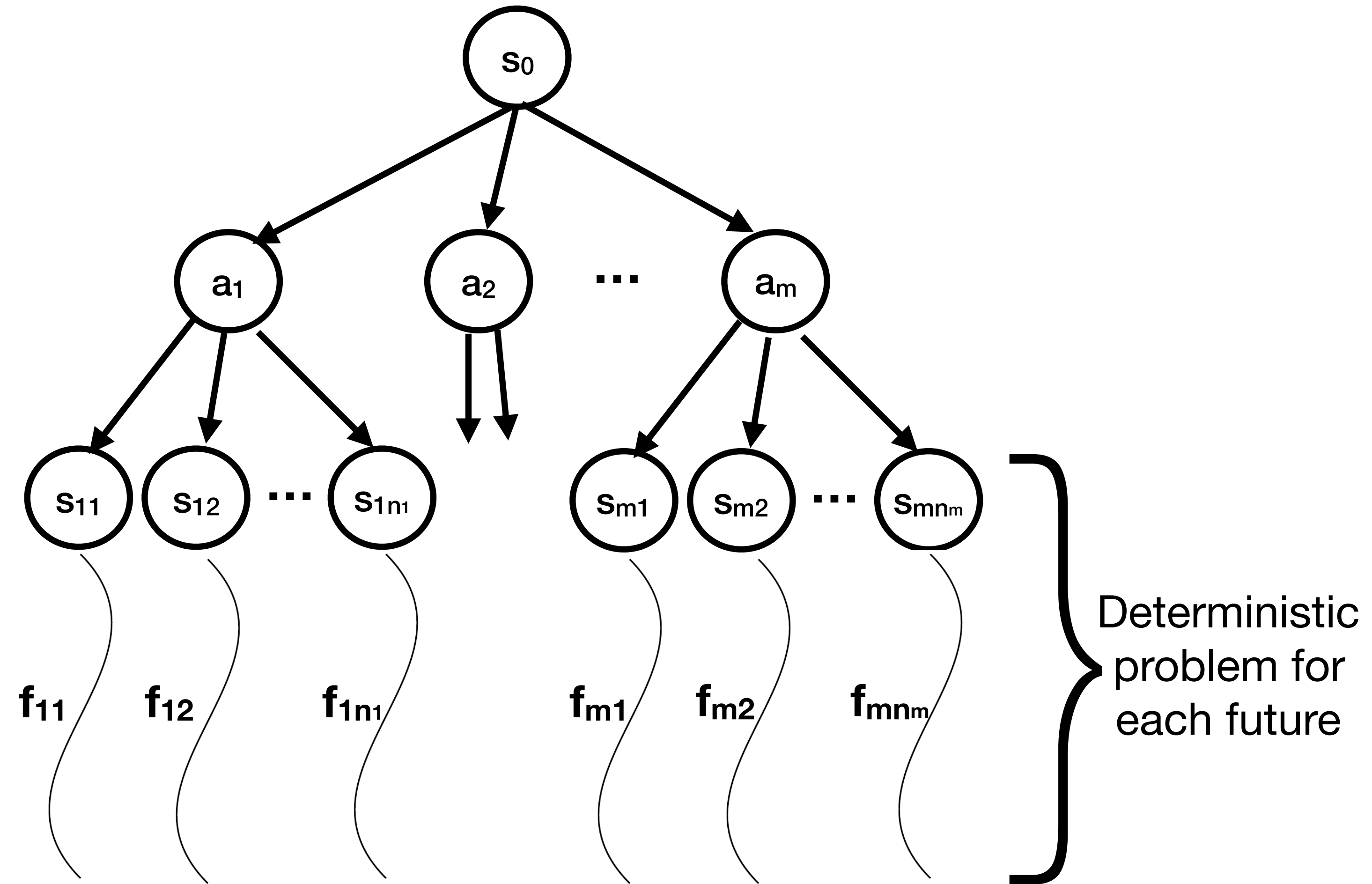
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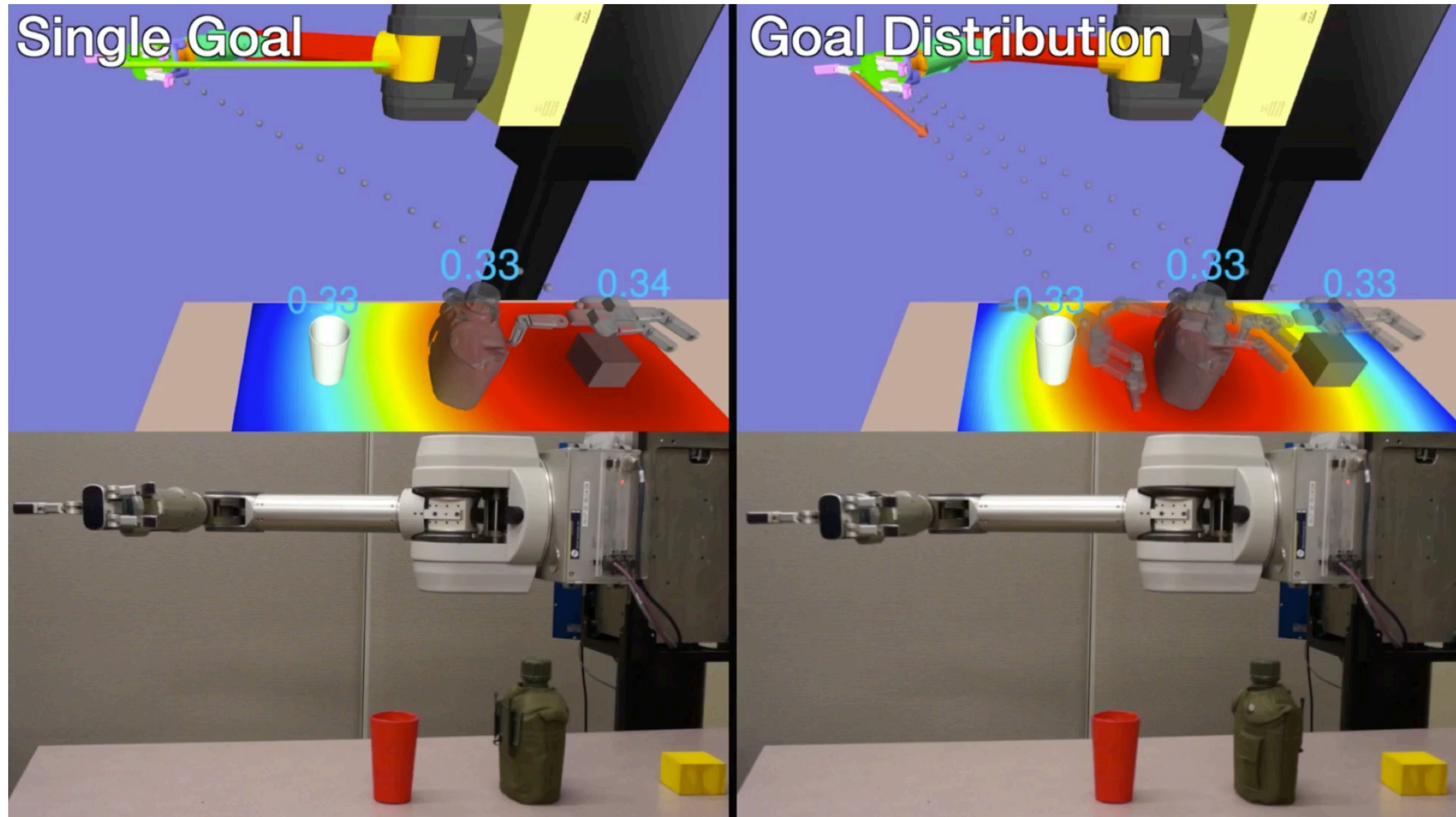
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# Results (video)

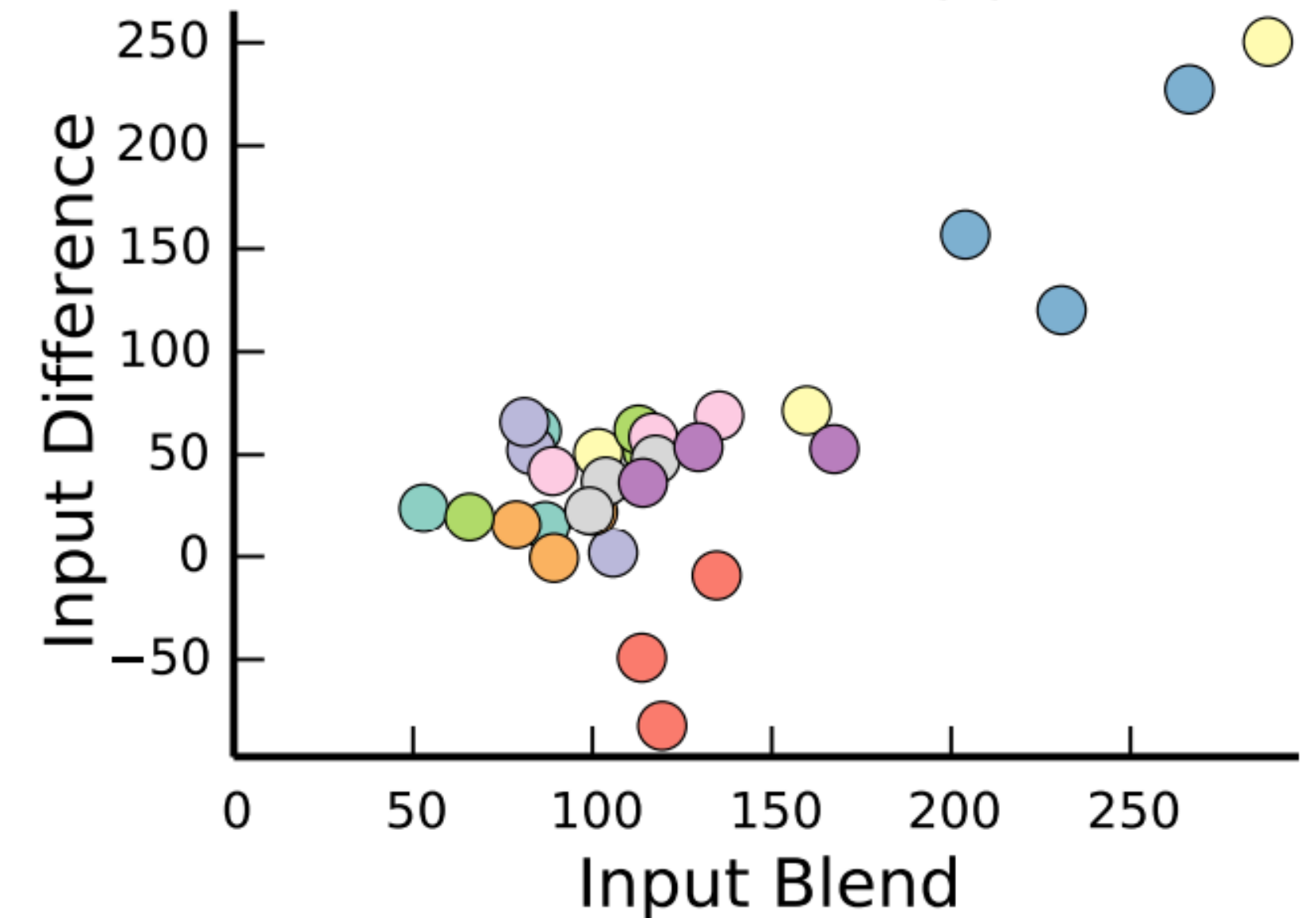
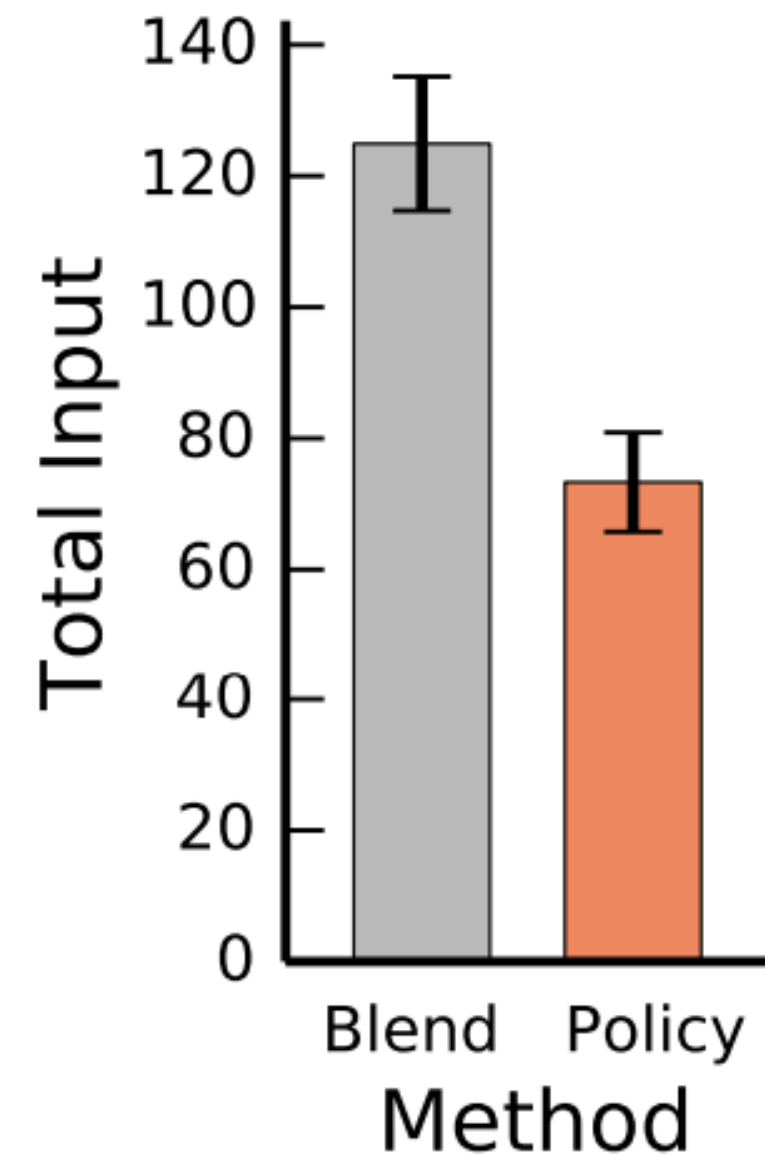
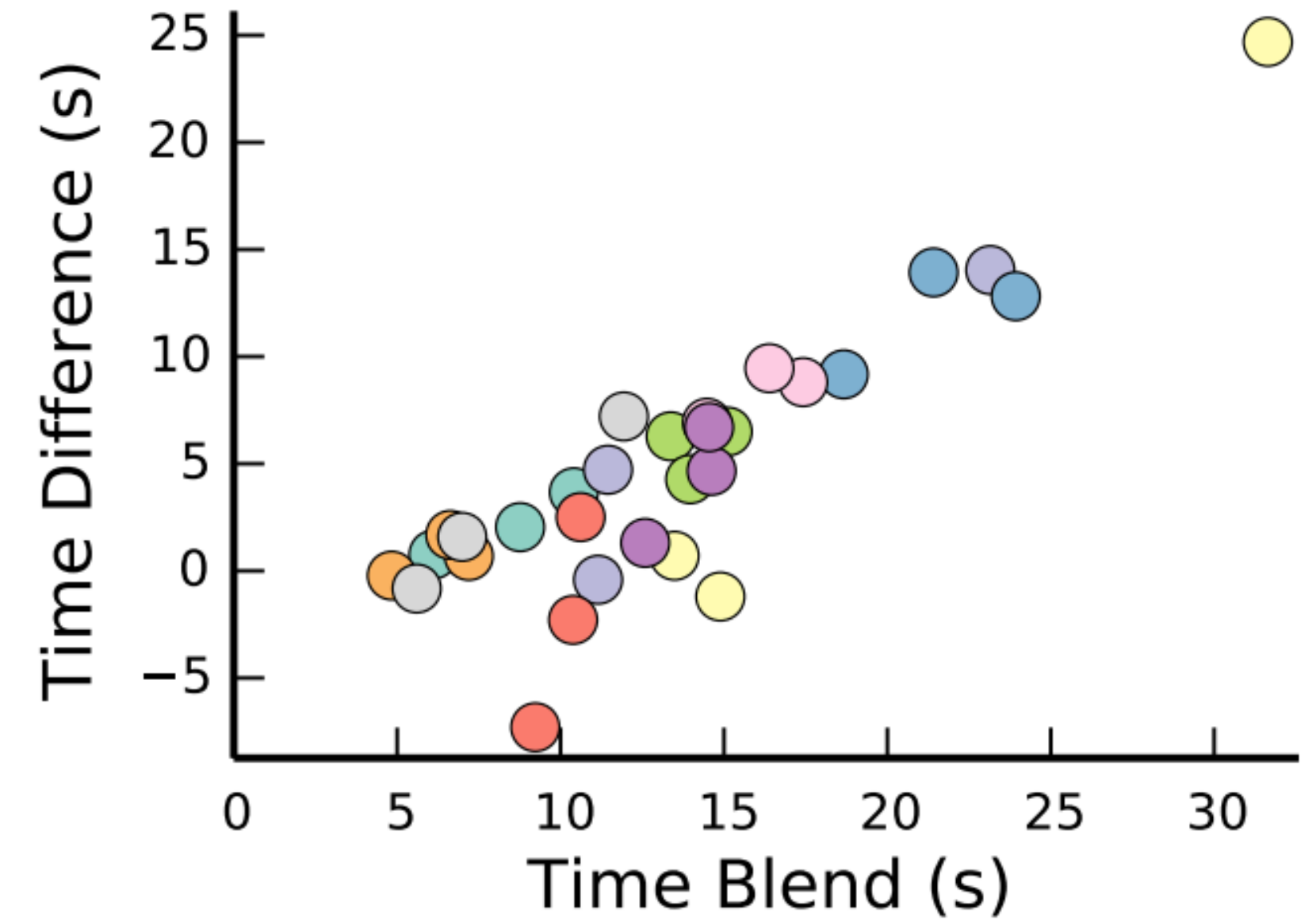
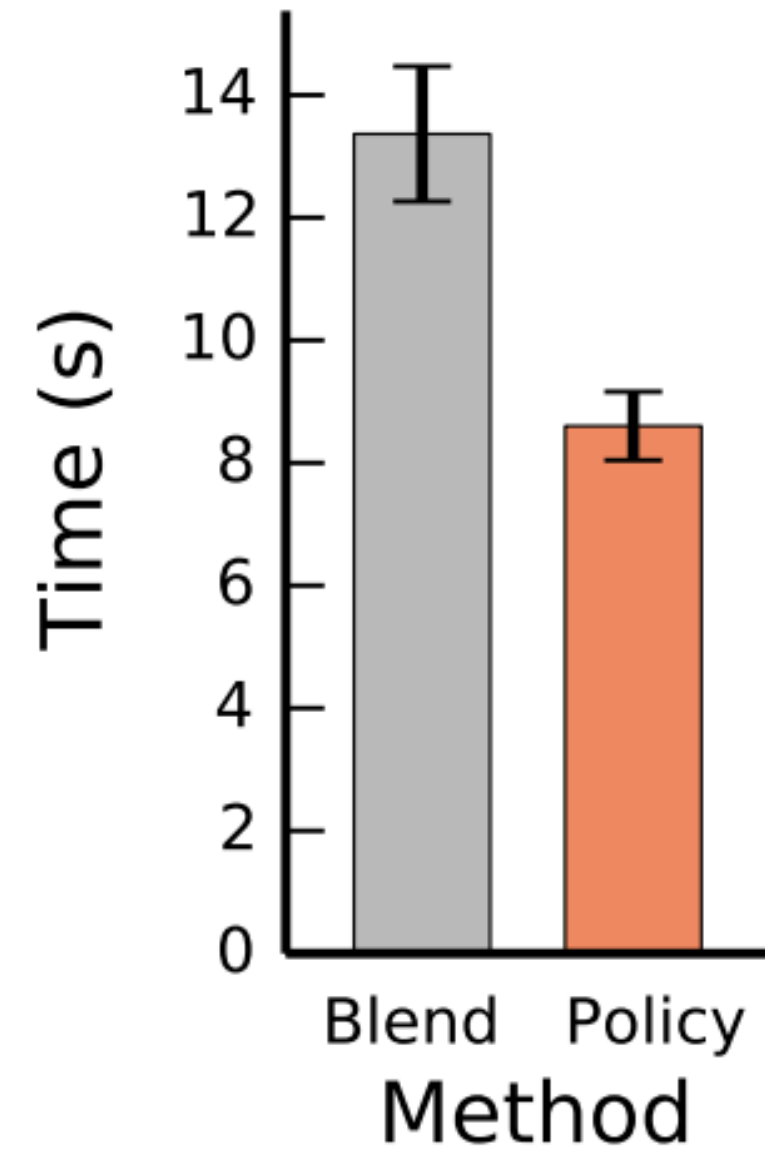




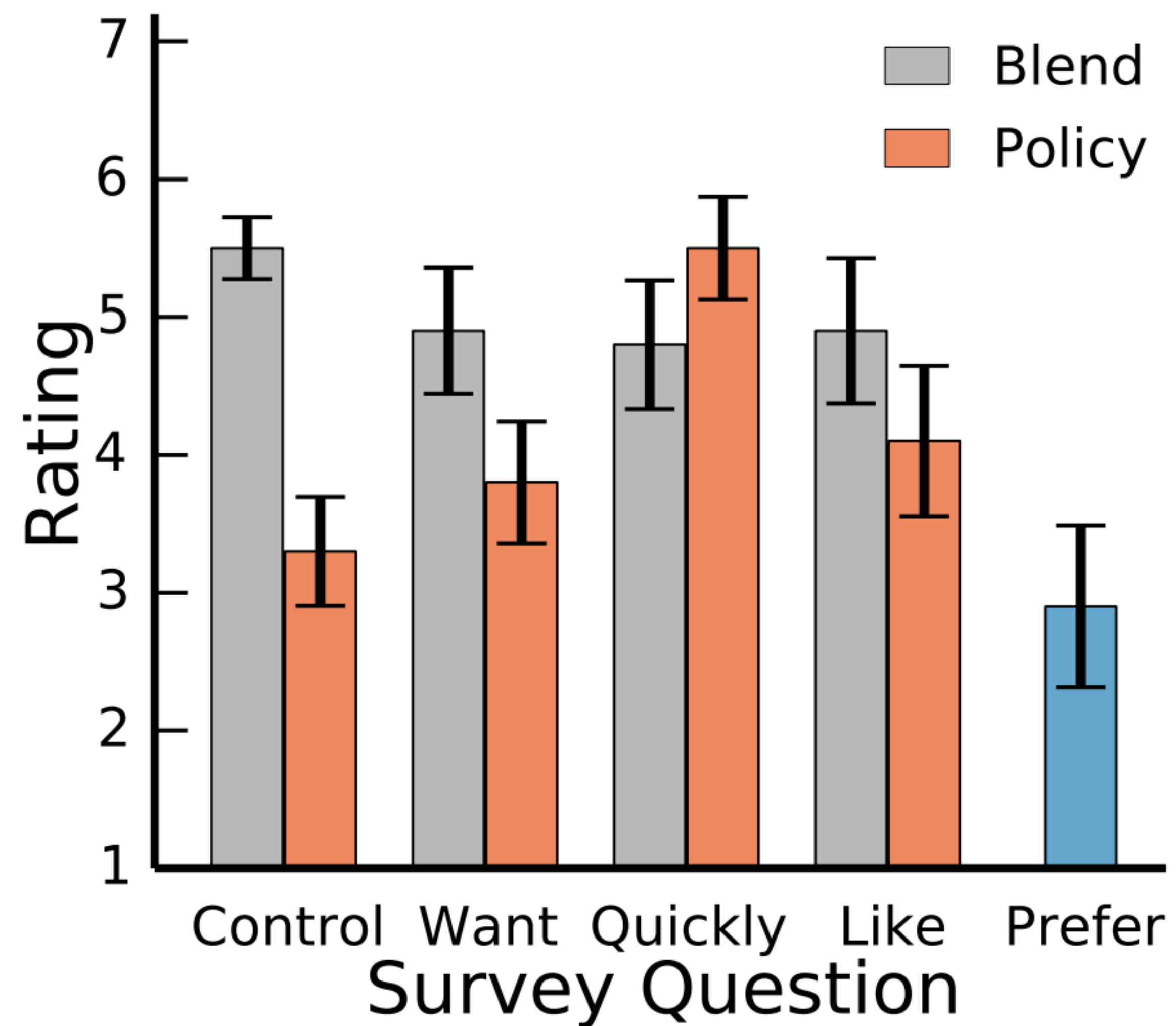
# Results

Compare with method that predicts one goal, the proposed method has:

- Faster execution time
- Fewer user inputs



# User Study





# Limitations

- Requires prior knowledge about the world:
  - a dynamics model that predicts the consequences of taking a given action in a given state of the environment;
  - the set of possible goals for the user;
  - the user's control policy given their goal.
- Suitable in constrained domains where where this knowledge can be directly hard-coded or learned.
- Unsuitable for unstructured environments with ill-defined goals and unpredictable user behavior.

# References

- Javdani, S., Srinivasa, S. S., & Bagnell, J. A. (2015). Shared autonomy via hindsight optimization. *Robotics science and systems: online proceedings, 2015*.
- RSS2015 talk: “Shared autonomy via hindsight optimization”
- Javdani, S., Admoni, H., Pellegrinelli, S., Srinivasa, S. S., & Bagnell, J. A. (2018). Shared autonomy via hindsight optimization for teleoperation and teaming. *The International Journal of Robotics Research*, 37(7), 717-742.
- ICAPS 2015 talk: "Hindsight Optimization for Probabilistic Planning with Factored Actions"