

# Embedding Invisible Information in Color Images \*

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## Abstract

We describe a method for embedding information in color images. A model of human color vision is used to ensure that the embedded signal is invisible. Sinusoidal signals are embedded so that they can be detected (decoded) without use of the original image. The sinusoids act as a grid, providing a coordinate frame on the image. We use the grid to automatically scale and align (deskew) images that have been printed and then scanned.

## Introduction

This paper concerns the embedding of information in images. The goal is to perturb images in ways that are invisible to humans but not to computers. Applications include watermarking [1, 5, 6], the embedding of image calibration information, or high-bandwidth digital messages [2]. Although these applications have differing requirements, in each case there is a trade-off between the amplitude of the embedded signal and its perceptibility. As the power of the embedded signal increases there is greater image degradation, but the decoding becomes easier.

This paper describes the embedding of amplitude-modulated sinusoidal signals in color images. The embedded information is sufficiently robust that it can be reliably extracted after being printed and scanned on commonplace equipment. To control the perceptibility of the embedded signal, or to ensure that it is below threshold, we use a quantitative model of human visual discriminability.

The sinusoids act as a grid, providing an image coordinate frame. Once the decoder has extracted the frequencies of the embedded sinusoids it computes the mapping from the original image to the scanned image. It then automatically aligns and scales the scanned image with the original. As a result, one does not have to align the image perfectly on the scanner,

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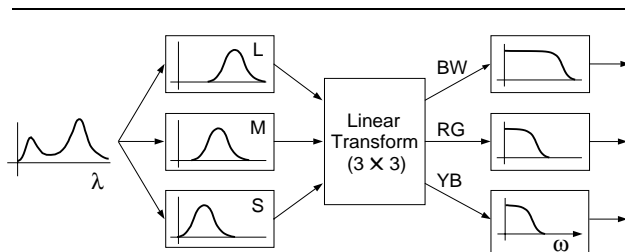


Figure 1: In human color processing, the input is encoded as 3 cone responses at each image position. These are transformed into an opponent-color representation with 3 bands, namely, black-white (BW), red-green (RG), and yellow-blue (YB). They are low-pass filtered with different frequency cutoffs.

nor scale/rotate the page after scanning. The frequencies could also act as landmarks with respect to which other embedded information could be located.

## Human Color Processing: S-CIELAB

CIELAB is a well-known standard for measuring color reproduction errors. It was based on psychophysical studies of color discriminability with large uniform color patches [7, 8]. More recent studies have shown that color appearance also depends on the local structure of the image. Measurements of color appearance with fine-scale patterns (eg. color square-wave gratings of different spatial frequencies) differ from those with large uniform color patches. To explain these results, Poirson and Wandell [3, 4] proposed a pattern-color separable model for early human color processing (see Fig. 1). In this model the initial color signals (the cone absorptions) are first transformed into an opponent-color representation with three bands (spatial images), referred to as luminance, red-green (RG), and yellow-blue (YB). Each band is then smoothed with a lowpass filter, where the RG and YB bands have lower frequency cutoffs.

S-CIELAB is an extension of CIELAB to account for the dependence of color appearance on spatial

structure. To measure color differences between two images, S-CIELAB transforms each image into an opponent-color representation and applies lowpass filters to each of the 3 bands. The results are then transformed into CIE XYZ-tristimulus coordinates, from which the conventional CIELAB formula is used to measure the color difference at each pixel [7, 8]. These color differences are denoted by  $\Delta E$ , where values greater than 1 imply that the color differences are detectable by humans. Values less than 1 imply that they are not discriminable.

S-CIELAB requires some calibration parameters. It requires the mapping between the digital representation of the color image and the spectral reflectance of the image when printed or displayed. Thus, we need a detailed model of the printer or display device and the spectral distribution of the illuminant. At present, our model simply assumes that the image is displayed on a CRT monitor with a conventional set of RGB phosphors. S-CIELAB also requires that we specify a *white point*. For images printed on white paper this would normally be the reflectance of the paper alone, under a standard illuminant. With digital images, we define the white point to be the highest luminance in the image (the pixel with the largest Y component in CIE XYZ-tristimulus coordinates).

In practice, color differences with  $\Delta E < 3$  are not readily apparent. However, with incomplete knowledge of the proper calibration parameters, it is important to keep the  $\Delta E$  values small (e.g.  $\leq 1$ ) to be conservative. The user could, however, change this threshold to accept more or less degradation.

## Signal Embedding

In our application we embed a sum of sinusoidal signals,  $S(x, y)$ , into the yellow-blue (YB) color band of the opponent-color representation (see Fig. 1). We choose high frequencies where human sensitivity is low and most images contain relatively little power. The signal,  $S(x, y)$ , is embedded in an iterative manner as shown in Fig. 2. S-CIELAB is used in each iteration to attenuate the signal amplitude wherever the difference between the original image and the test image (the original plus the embedded signal) is significant, ie where  $\Delta E(x, y) > 1$ .

At each iteration, if there are a sufficient number of image locations where  $\Delta E(x, y) > 1$ , then  $\Delta E(x, y)$  is converted into an image of attenuation factors  $a(x, y)$ :

$$a(x, y) = (2 / (2 + \max[0, \Delta E(x, y) - 1]))^2 \quad (1)$$

The image of attenuation factors,  $a(x, y)$ , is blurred and then multiplied with the signal that was embedded in the previous iteration, yielding the embedded

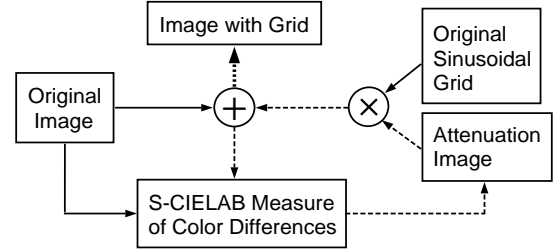


Figure 2: In each iteration of the embedding process (dashed arrows), a signal is added, after which S-CIELAB is used to indicate where color differences are detectable. At these locations the embedded signal is attenuated before being added again.

signal for the next iteration. This process runs until 99.5% of the pixels have  $\Delta E(x, y) \leq 1$ , which usually takes 3 to 5 iterations. The final embedded signal is

$$G(x, y) = \left( \prod_{i=1}^n a_i(x, y) \right) S(x, y) \quad (2)$$

where  $n$  is the number of iterations,  $S(x, y)$  is the sum of sinusoids, and  $a_i(x, y)$  is the blurred attenuation image at iteration  $i$ . The amplitude of the embedded signal can only decrease at each iteration, which ensures convergence so that  $\Delta E(x, y) \leq 1$  almost everywhere. Equation (1), which converts  $\Delta E$  values into attenuation factors, was chosen empirically to obtain a reasonable rate of convergence.

The blurring of  $a(x, y)$  is important because S-CIELAB measures color differences in local neighborhoods, due to the spatial blurring in each opponent-color band. We blur  $a(x, y)$  using the same lowpass filter that S-CIELAB uses for the YB band. The blurring also keeps the bandwidth of the embedded signal relatively small. This keeps its frequency content away from low frequencies to which humans are very sensitive. Smaller bandwidths also keep the power of the sinusoids more concentrated and easier to detect.

To demonstrate the method we embedded 4 sinusoids into the image shown in Fig.4 (left). Figure 3 shows the amplitude-modulated grid and the YB band with the embedded signal after iterations 1 and 2. The sinusoids had orientations of  $\pm 45^\circ$  and wavelengths of 3.8 and 2.7 pixels. Figure 4 shows the original and the resultant images. We calibrated S-CIELAB so that the embedded signal would be invisible when viewed from 10 inches (at which the frequencies are 7 and 10 cycles/degree). In fact, the process is sufficiently robust that the embedded signal remains invisible even when viewed more closely.

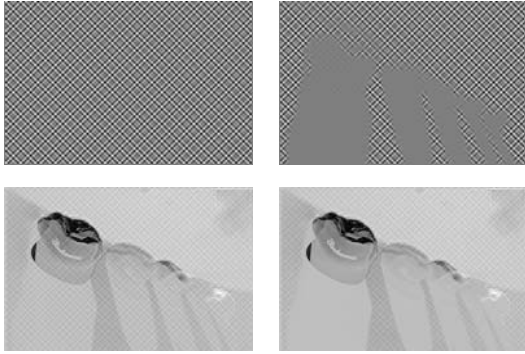


Figure 3: Results of embedding after iterations 1 and 2. (top) Amplitude-modulated grid. (bottom) YB band with embedded signal.



Figure 4: Original hats image (left) and a version with the embedded sinusoids (right). The grid should be invisible when viewed from 10in or more. See CD-ROM proceedings for color images.

## Signal Decoding

The decoder extracts the frequencies that correspond to the embedded sinusoids. To do this without the original image relies on several factors: First, the sinusoids have high frequencies where most images have little power in the YB band. Second, there are geometric relations between the frequencies that will not likely occur by chance. We assume that geometric distortions caused by printing/scanning are nearly conformal (rotation and uniform scaling), and can be modeled well as a linear mapping. This allows us to use our knowledge of the geometric relations among the embedded sinusoids to facilitate their detection.

Following Fig. 5, the scanned image is transformed into the opponent-color space, and the amplitude spectrum of the YB band,  $A(\omega_x, \omega_y)$ , is computed. Figure 6(top-left) shows the log spectrum of the YB band of Fig. 4 (right). Notice the peak power concentrations of the four embedded sinusoids. To enhance the peaks, we divide  $A(\omega_x, \omega_y)$  by a blurred version of itself. Fig. 6 (top-right) shows the detected peaks.

Figure 6 (bottom) shows peaks detected from a scanned version of Fig. 7 (top). This spectrum differs from that in Fig. 6 (top-right). First, the peaks corresponding to the embedded sinusoids occur at different

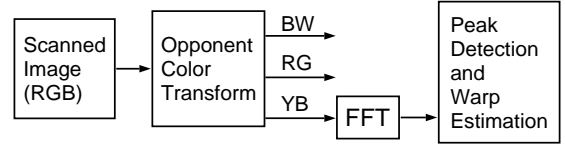


Figure 5: The decoder transforms the image into the opponent-color representation, and computes the amplitude spectrum of the YB band. Its peaks are enhanced and detected, from which the mapping between the scanned image and the original is computed.

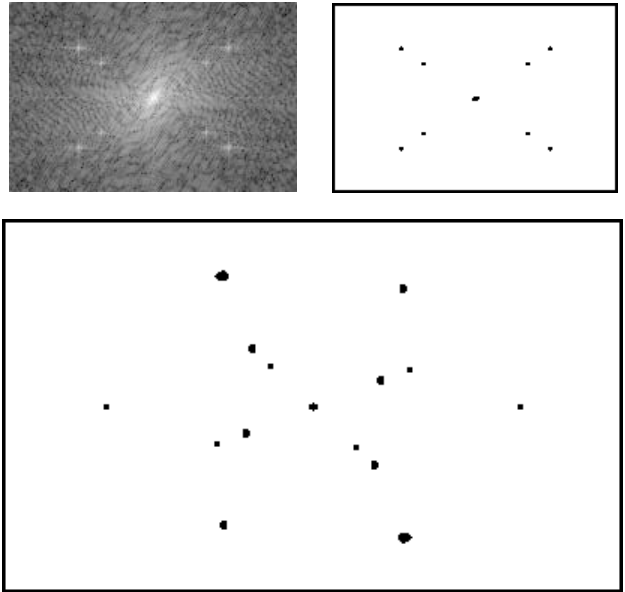


Figure 6: (top-left) Log amplitude spectrum (origin at image center) of the YB band of the image with the grid in Fig. 4. (top-right) Enhanced spectrum, thresholded to show the peaks detected. (bottom) Peaks detected from scanned image in Fig. 8.

frequencies and orientations because the resolutions of the printer and scanner were different and because the page was not oriented perfectly on the scanner. Second, note that new spectral peaks have appeared, caused by scanner/printer artifacts and the oriented boundaries of the scanned image.

The decoder first extracts all energy peaks as candidate frequencies. From the set of candidates we examine all combinations of four, discarding those immediately that violate our *a priori* geometric constraints on the embedded frequencies. This pruning quickly removes the unlikely candidates. Of the sets of four that remain, we find the one that yields the best (least-squares sense) linear mapping between the locations of the scanned peaks and the original peaks.



Figure 7: (top) Fig. 4 (right) was scanned at 300dpi. (bottom) Warped version of the scanned image computed by the decoder. The mapping was roughly conformal with a rotation of  $11^\circ$  and a scale factor of 2. Print resolution was 300dpi. Image size was  $192 \times 128$ .

The decoder outputs the 4 frequencies and the linear mapping between the scanned and original images. Fig. 7 (top) shows a scanned portion of Fig. 4 (right) that contains the embedded grid. It was scanned at 300dpi on an HP ScanJet IIc, and one can see that the image quality is poor. The page orientation was about  $11^\circ$  and the scanned image is a factor of 2 larger because the images in Fig. 4 were originally printed at twice their nominal size. Despite the poor image quality, the decoder extracted the frequencies and the linear mapping. We warped the scanned image using this mapping, the result of which is in Fig. 7 (bottom).

We have tested this process on several images, showing that the amplitude of the embedded signal is sufficient to be detected by desktop scanners. Note

that the embedded sinusoids are well within the frequency range to which humans are normally quite sensitive with luminance (black-white) patterns. However, human sensitivity at these frequencies in color bands is much lower, and this is why we embed the signal in the YB band. One advantage of this is that the embedded signals can be detected at relatively low sampling rates (e.g., in preview mode on the scanner).

## Conclusion

We describe a way to embed sinusoidal signals in color images. We use a model of human color vision to make them invisible, yet they can be detected and extracted by a decoder without using the original image. The sinusoidal signals act as a grid, providing a coordinate frame on the image. We can extract the sinusoids from a scanned version of the image, and thereby compute the mapping from the original image to the scanned image. With this we automatically scale and orient the scanned version with the original.

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