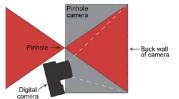
Cameras and Images

Pinhole Camera



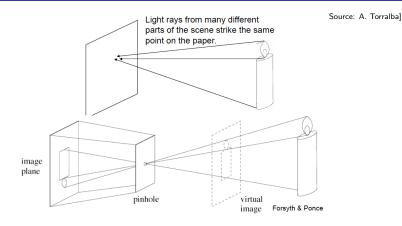


[Source: A. Torralba]



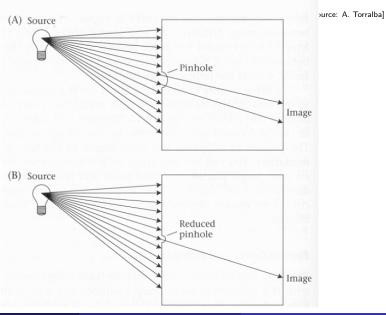
- Make your own camera
- http://www.foundphotography.com/PhotoThoughts/archives/2005/04/pinhole_camera_2.html

Pinhole Camera – How It Works



 The pinhole camera only allows rays from one point in the scene to strike each point of the paper.

Pinhole Camera - How It Works



Pinhole Camera – Example

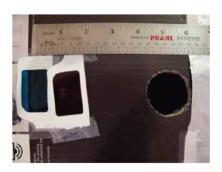
[Source: A. Torralba]





Pinhole Camera

[Source: A. Torralba]





You can make it stereo

Pinhole Camera – Stereo Example

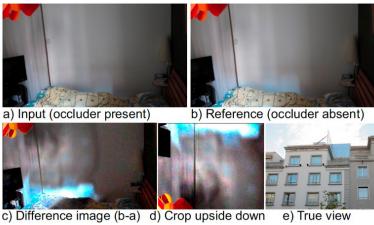
[Source: A. Torralba]



Try it with 3D glasses!

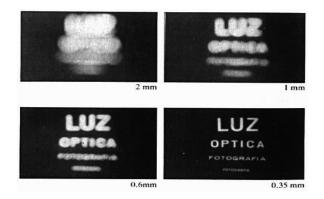
Pinhole Camera

[Source: A. Torralba]



- Remember this example?
- In this case the window acts as a pinhole camera into the room

Shrinking the Aperture

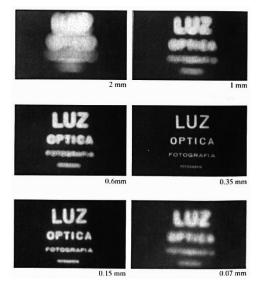


Why not make the aperture as small as possible?

- Less light gets through
- Diffraction effects...

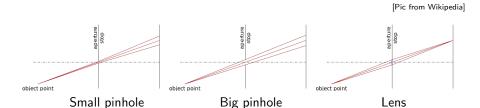
[Source: N. Snavely]

Shrinking the Aperture



[Source: N. Snavely]

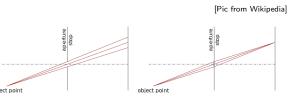
Adding a Lens



- A lens focuses light onto the film
- There is a specific distance at which objects are in focus

Adding a Lens

object point



Lens

• A lens focuses light onto the film

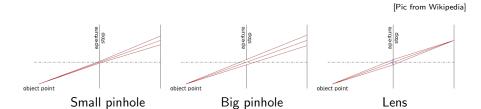
Small pinhole

- There is a specific distance at which objects are in focus
- Changing the shape of the lens changes this distance

[Source: N. Snavely]

Big pinhole

Adding a Lens



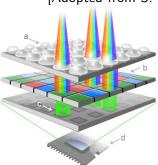
- A lens focuses light onto the film
- There is a specific distance at which objects are in focus
- Changing the shape of the lens changes this distance

[Source: N. Snavely]

Digital Camera

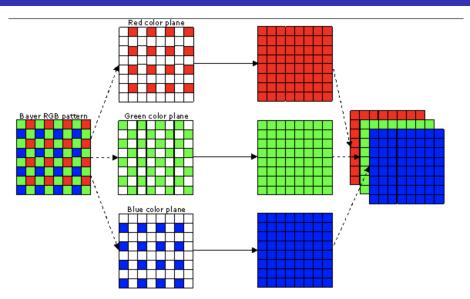


[Adopted from S. Seitz]



- A digital camera replaces film with a sensor array
- Each cell in the array is a light-sensitive diode that converts photons to electrons
- http://electronics.howstuffworks.com/cameras-photography/ digital/digital-camera.htm

Demosaicing



Digital Camera

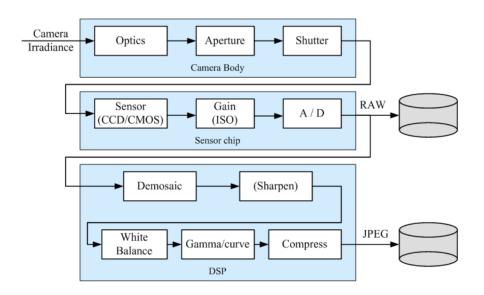


Image Formation

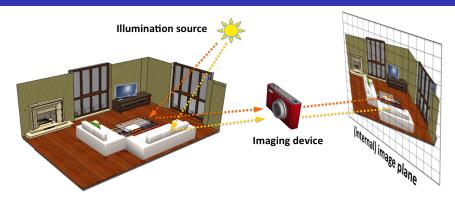


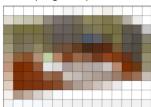
Image formation process producing a particular image depends on:

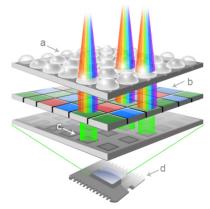
- lighting conditions
- scene geometry
- surface properties
- camera optics

Continuous image projected to sensor array



Sampling and quantization





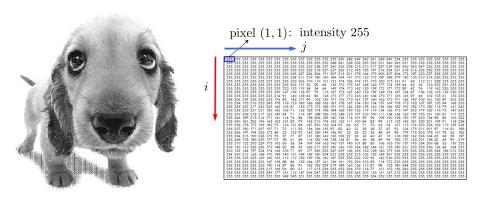
http://pho.to/media/images/digital/digital-sensors.jpg

- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)

- Image is a matrix with integer values
- We will typically denote it with I

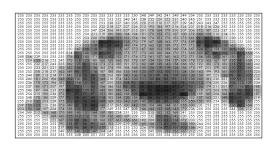


- Image is a matrix with integer values
- We will typically denote it with I
- I(i,j) is called **intensity**



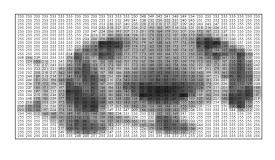
- Image is a matrix with integer values
- We will typically denote it with I
- I(i,j) is called **intensity**
- Matrix I can be $m \times n$ (grayscale)





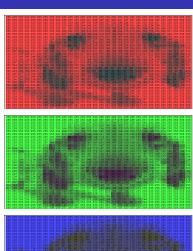
- Image is a matrix with integer values
- We will typically denote it with I
- I(i,j) is called **intensity**
- Matrix I can be $m \times n$ (grayscale)
- or $m \times n \times 3$ (color)

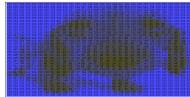




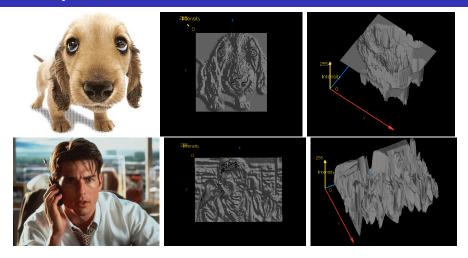
- Image is a matrix with integer values
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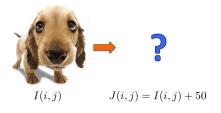


Intensity



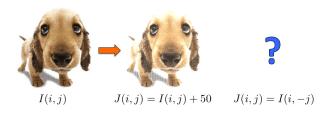
- We can think of a (grayscale) image as a function $f: \mathbb{R}^2 \to \mathbb{R}$ giving the intensity at position (i,j)
- Intensity 0 is black and 255 is white

As with any function, we can apply operators to an image, e.g.:



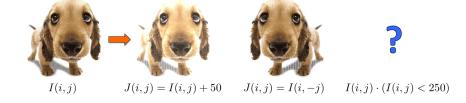
 We'll talk about special kinds of operators, correlation and convolution (linear filtering)

As with any function, we can apply operators to an image, e.g.:



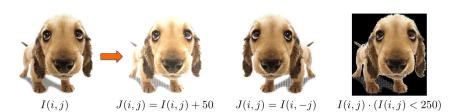
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• As with any function, we can apply operators to an image, e.g.:



 We'll talk about special kinds of operators, correlation and convolution (linear filtering)

Linear Filters

Reading: Szeliski book, Chapter 3.2

Motivation: Finding Waldo

• How can we find Waldo?





[Source: R. Urtasun]

Answer

- Slide and compare!
- In formal language: filtering

Motivation: Noise reduction

• Given a camera and a still scene, how can you reduce noise?



[Source: S. Seitz]

Image Filtering

- Modify the pixels in an image based on some function of a local neighborhood of each pixel
- In other words... Filtering

10	5	3
4	5	1
1	1	7

Local image data



a

7

Modified image data

[Source: L. Zhang]

Applications of Filtering

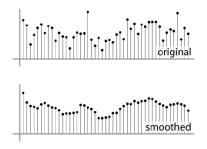
- Enhance an image, e.g., denoise.
- Detect patterns, e.g., template matching.
- Extract information, e.g., texture, edges.
- Filtering is used in Convolutional Neural Networks

Applications of Filtering

- Enhance an image, e.g., denoise. Let's talk about this first
- Detect patterns, e.g., template matching.
- Extract information, e.g., **texture**, **edges**.

Noise reduction

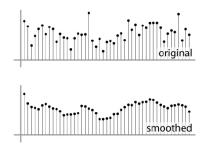
- Simplest thing: replace each pixel by the average of its neighbors.
- This assumes that neighboring pixels are similar, and the noise to be independent from pixel to pixel.



[Source: S. Marschner]

Noise reduction

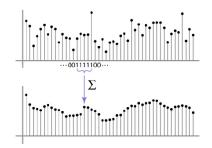
- Simplest thing: replace each pixel by the average of its neighbors.
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[Source: S. Marschner]

Noise reduction

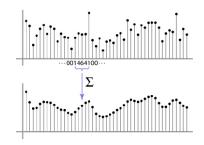
- Simplest thing: replace each pixel by the average of its neighbors
- This assumes that neighboring pixels are similar, and the noise to be independent from pixel to pixel.
- Moving average in 1D: [1, 1, 1, 1, 1]/5



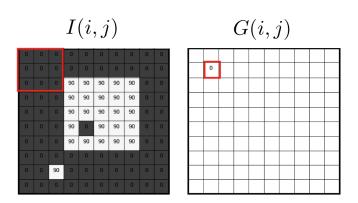
[Source: S. Marschner]

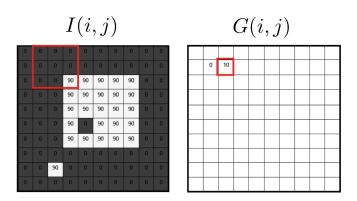
Noise reduction

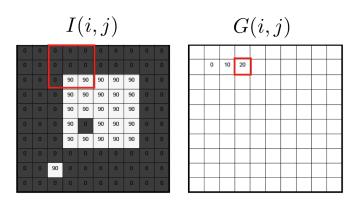
- Simplest thing: replace each pixel by the average of its neighbors
- This assumes that neighboring pixels are similar, and the noise to be independent from pixel to pixel.
- Non-uniform weights [1, 4, 6, 4, 1] / 16

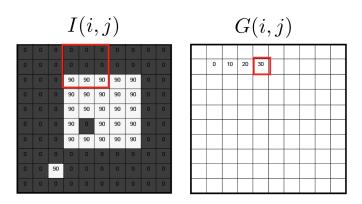


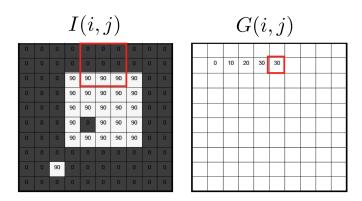
[Source: S. Marschner]

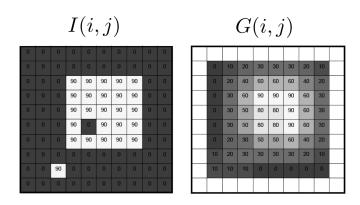












Involves weighted combinations of pixels in small neighborhoods:

$$G(i,j) = \frac{1}{(2k+1)^2} \sum_{u=-k}^{k} \sum_{v=-k}^{k} I(i+u,j+v)$$

 The output pixel's value is determined as a weighted sum of input pixel values

$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

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- This operator is the correlation operator

$$G = F \otimes I$$

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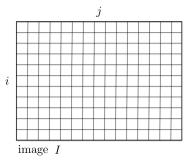
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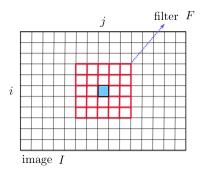
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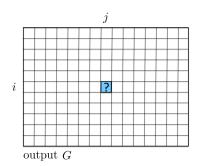
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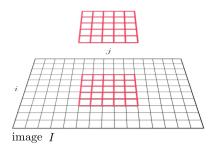
$$G = F \otimes I$$

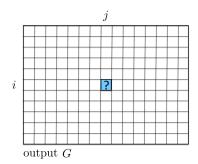


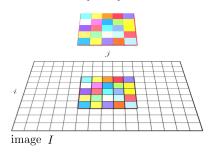


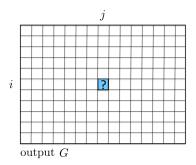








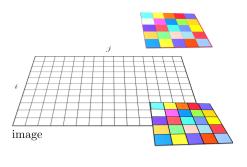


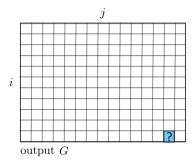


$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

$$G(i,j) = F(\square) \cdot I(\square) + F(\square) \cdot I(\square) + F(\square) \cdot I(\square) + \dots + F(\square) \cdot I(\square)$$

• What happens along the borders of the image?





$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

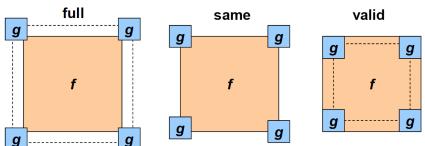
$$G(i,j) = F() \cdot I() + F() \cdot I() + F() \cdot I() + \dots + F() \cdot I()$$

Boundary Effects

- What happens at the border of the image? What's the size of the output matrix?
- MATLAB: FILTER2(G, F, SHAPE)
 Python: SCIPY.NDIMAGE.CONVOLVE
- shape = "full" output size is sum of sizes of f and g
- shape = "same": output size is same as f
- shape = "valid": output size is difference of sizes of f and g

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- shape = "valid": output size is difference of sizes of f and g



• What's the result?



0	0	0
0	1	0
0	0	0

?

Original

• What's the result?



Original





Filtered (no change)

• What's the result?



I	0	0	0
	0	0	1
	0	0	0

?

Original

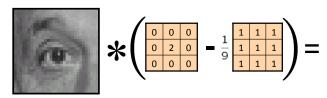
• What's the result?



0	0	0
0	0	1
0	0	0

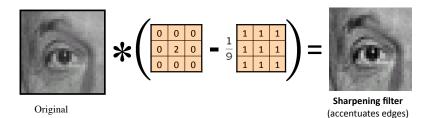


• What's the result?

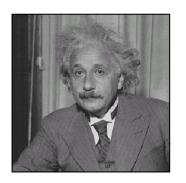


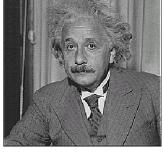
Original

• What's the result?



Sharpening





before

after

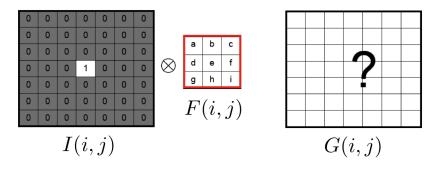
Sharpening



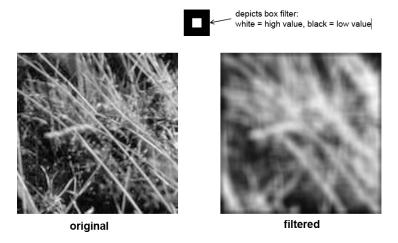
[Source: N. Snavely]

Example of Correlation

• What is the result of filtering the impulse signal (image) I with the arbitrary filter F?



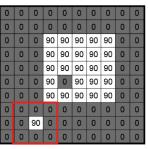
Smoothing by averaging



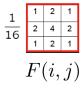
• What if the filter size was 5×5 instead of 3×3 ?

Gaussian filter

- What if we want nearest neighboring pixels to have the most influence on the output?
- Removes high-frequency components from the image ("low-pass filter").

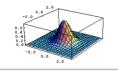


$$\overline{I(i,j)}$$

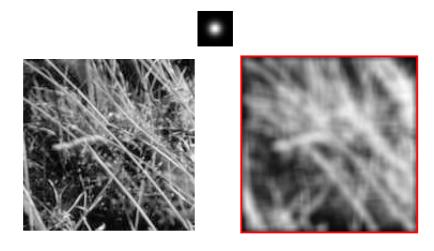


This kernel is an approximation of a 2d Gaussian function:

$$h(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2 + v^2}{2\sigma^2}}$$

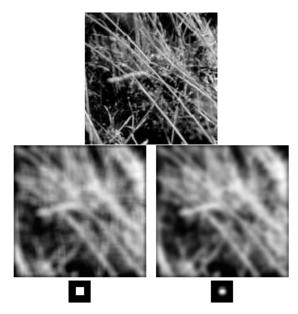


Smoothing with a Gaussian



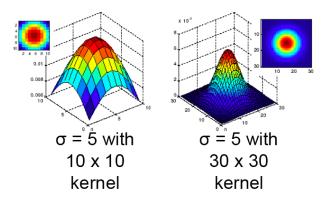
[Source: K. Grauman]

Mean vs Gaussian



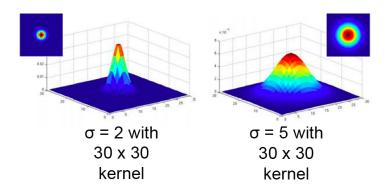
Gaussian filter: Parameters

• Size of filter or mask: Gaussian function has infinite support, but discrete filters use finite kernels.

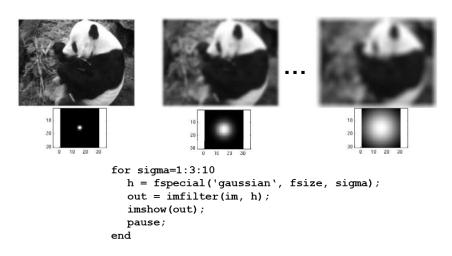


Gaussian filter: Parameters

• Variance of the Gaussian: determines extent of smoothing.



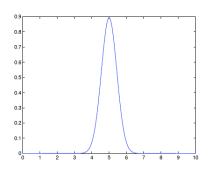
Gaussian filter: Parameters

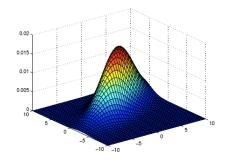


Is this the most general Gaussian?

ullet No, the most general form for $\mathbf{x} \in \Re^d$

$$\mathcal{N}\left(\mathbf{x};\,\mu,\Sigma\right) = \frac{1}{(2\pi)^{d/2}|\Sigma|^{1/2}}\exp\left(-\frac{1}{2}(\mathbf{x}-\mu)^T\Sigma^{-1}(\mathbf{x}-\mu)\right)$$





• We typically use isotropic filters (i.e., circularly symmetric)

- All values are positive.
- They all sum to 1.

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Note: This holds for smoothing filters, not general filters

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- They all sum to 1.
- Amount of smoothing proportional to mask size.
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Note: This holds for smoothing filters, not general filters

Template Matching: Finding Waldo





image I

• How can we use what we just learned about filtering to find Waldo?

Template Matching: Finding Waldo





image I

filter F

• Is correlation a good choice?

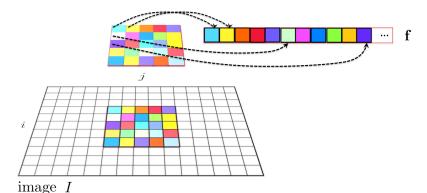
Remember correlation:

$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

Can we write that in a more compact form (with vectors)?

Remember correlation:

$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$



Remember correlation:

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$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

$$G(i,j) = \mathbf{f}^{T} \cdot \mathbf{t}_{ij}$$
image I

Remember correlation:

$$G(i,j) = \sum_{u=-k}^{k} \sum_{v=-k}^{k} F(u,v) \cdot I(i+u,j+v)$$

- Can we write that in a more compact form (with vectors)?
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• **Homework:** Can we write full correlation $G = F \otimes I$ in matrix form?

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- Normalized cross-correlation:

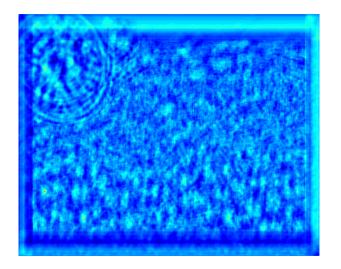
$$G(i,j) = \frac{\mathbf{f}^T \cdot \mathbf{t}_{ij}}{||\mathbf{f}|| \cdot ||\mathbf{t}_{ij}||}$$



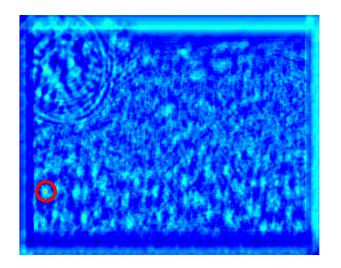




filter F



Result of normalized cross-correlation



• Find the highest peak



And put a bounding box (rectangle the size of the template) at the point!



• Homework: Do it yourself! Code on class webpage. Don't cheat!

Convolution

Convolution operator

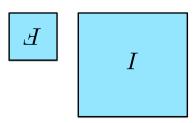
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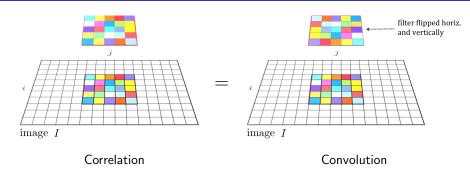
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 Equivalent to flipping the filter in both dimensions (bottom to top, right to left) and apply correlation.





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• If the input is an impulse signal, how will the outputs differ? $\delta * I$ and $\delta \otimes I$?

"Optical" Convolution

Camera Shake



Figure: Fergus, et al., SIGGRAPH 2006

• Blur in out-of-focus regions of an image.



Figure: Bokeh: http://lullaby.homepage.dk/diy-camera/bokeh.html Click for more info

[Source: N. Snavely]

Properties of Convolution

Commutative : f * g = g * f

Associative : f * (g * h) = (f * g) * h

Distributive : f * (g + h) = f * g + f * h

Assoc. with scalar multiplier : $\lambda \cdot (f * g) = (\lambda \cdot f) * h$

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- **Homework:** Why is this good news?
- Hint: Think of complexity of convolution and Fourier Transform
- Homework: Do above properties also hold for correlation?
- Both correlation and convolution are linear shift-invariant (LSI)
 operators: the effect of the operator is the same everywhere.

Gaussian Filter

• Convolving twice with Gaussian kernel of width σ is the same as convolving once with kernel of width $\sigma\sqrt{2}$



We don't need to filter twice, just once with a bigger kernel

[Source: K. Grauman]

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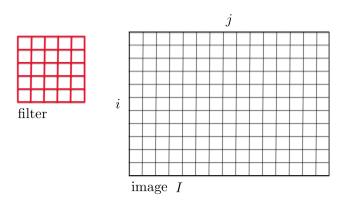
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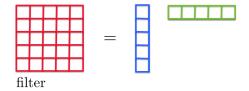
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- And it is the outer product of two filters:

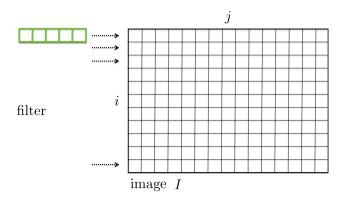
$$\mathbf{F} = \mathbf{v} \, \mathbf{h}^T$$

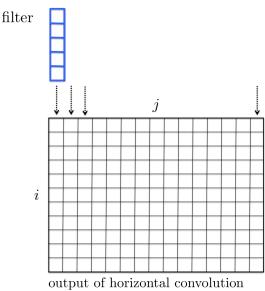
 Homework: Think why in the case of separable filters 2D convolution is the same as two 1D convolutions

[Source: R. Urtasun]





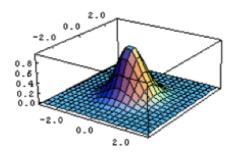




Separable Filters: Gaussian filters

• One famous separable filter we already know:

Gaussian :
$$f(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{\sigma^2}}$$

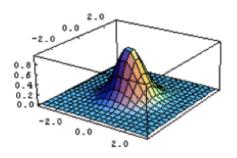


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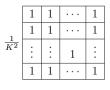
= $\left(\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{x^2}{\sigma^2}}\right) \cdot \left(\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{y^2}{\sigma^2}}\right)$



Is this separable? If yes, what's the separable version?

$\frac{1}{K^2}$	1	1		1
	1	1		1
	:	:	1	:
	1	1		1

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$$\frac{1}{K}$$
 1 1 \cdots 1

What does this filter do?

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$$\begin{array}{c|cccc}
 & 1 & 2 & 1 \\
\hline
 & 2 & 4 & 2 \\
\hline
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\end{array}$$

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$$\begin{array}{c|cccc}
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$$\frac{1}{4}$$
 $\begin{bmatrix} 1 & 2 & 1 \end{bmatrix}$

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- Matlab: [U,S,V] = SVD(F);
- $\sqrt{\sigma_1}\mathbf{u}_1$ and $\sqrt{\sigma_1}\mathbf{v}_1^T$ are the vertical and horizontal filter.

Summary – Stuff You Should Know

- Correlation: Slide a filter across image and compare (via dot product)
- Convolution: Flip the filter to the right and down and do correlation
- ullet Smooth image with a Gaussian kernel: bigger σ means more blurring
- **Some** filters (like Gaussian) are **separable**: you can filter faster. First apply 1D convolution to each row, followed by another 1D conv. to each column
- Applying first a Gaussian filter with σ_1 and then another Gaussian with σ_2 is the same as applying one Gaussian filter with $\sigma = \sqrt{\sigma_1^2 + \sigma_2^2}$

Functions

Python functions:

- SCIPY.NDIMAGE.CORRELATE: correlation
- SCIPY.NDIMAGE.CONVOLVE: convolution
- Many filters available: https://docs.scipy.org/doc/scipy-0.15.1/ reference/ndimage.html#module-scipy.ndimage.filters

Matlab functions:

- IMFILTER: can do both correlation and convolution
- CORR2, FILTER2: correlation, NORMXCORR2 normalized correlation
- CONV2: does convolution
- FSPECIAL: creates special filters including a Gaussian

Edges

• What does blurring take away?



[Source: S. Lazebnik]

Next time:

Edge Detection