## Camera Models

## Textbook

- If you are interested, this book has it all:


## A. Zisserman and R. Hartley Multiview Geometry

Cambridge University Press, 2003

## Camera

- Camera is structurally similar to the eye

[Source: L.W. Kheng]


## Camera

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## Camera

- Remember the pinhole camera from Lecture 2?

[Source: A. Torralba]


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## Camera

- Remember the pinhole camera from Lecture 2?
- Size of the pinhole is called aperture

[Source: A. Torralba]


## Pinhole Camera



## Shrinking the Aperture



Why not make the aperture as small as possible?

- Less light gets through
- Diffraction effects...
[Source: N. Snavely]


## Shrinking the Aperture


[Source: N. Snavely]

## Adding a Lens

[Pic from Wikipedia]


- A lens focuses light onto the film
- There is a specific distance at which objects are in focus


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- A lens focuses light onto the film
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[Source: N. Snavely]


## Some "Cameras" Have Bigger Lenses than Others


http://www.use.com/images/s_2/thick_glasses_13b6941623c255ff400a_1.jpg?

## Imaging

- Images are 2D projections of real world scene
- Images capture two kinds of information:
- Geometric: positions, points, lines, curves, etc.
- Photometric: intensity, color
- Complex 3D-2D relationships
- Camera models approximate these relationships

[Source: L.W. Kheng]

## Projection


[Source: N. Snavely]

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## 3D to 2D Projection

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- We can do this using a linear 3D to 2D projection matrix


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- Orthographic projection
- Scaled orthographic projection
- Paraperspective projection
[source: R. Urtasun]


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## 3D to 2D Projection

- How are 3D primitives projected onto the image plane?
- We can do this using a linear 3D to 2D projection matrix
- Different types, most common:
- Perspective projection
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## Modeling Projection

[Pics from: A. Torralba, Forsyth \& Ponce]

- We will use the pinhole model as an approximation



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same distance from camera we call it: focal length


## Focal Length

- Can be thought of as zoom
- Related to the field of view


Figure: Image from N. Snavely
[Source: N. Snavelv, slide credit: R. Urtasun]

## Modeling Projection

[Pics from: A. Torralba, Forsyth \& Ponce]

- We will use the pinhole model as an approximation

- Since it's easier to think in a non-upsidedown world, we will work with the virtual image plane, and just call it the image plane.
- How do points in 3D project to image plane? If I know a point in 3D, can I compute to which pixel it projects?


## Modeling Projection



- First some notation which will help us derive the math
- To start with, we need a coordinate system


## Modeling Projection

## camera coordinate system in 3D



- We place a coordinate system relative to camera: optical center or camera center $\mathbf{C}$ is thus at origin $(0,0,0)$.


## Modeling Projection

## camera coordinate system in 3D



- The $Z$ axis is called the optical or principal axis. It is orthogonal to the image plane. Axes $X$ and $Y$ are parallel to the image axes.


## Modeling Projection

## camera coordinate system in 3D

Right Handed Coordinates


- We will use a right handed coordinate system


## Modeling Projection

## camera coordinate system in 3D



- The optical axis intersects the image plane in a point, $\mathbf{p}$. We call this point a principal point. It's worth to remember the principal point since it will appear again later in the math.


## Modeling Projection

## camera coordinate system in 3D



- The distance from the camera center to the principal point is called focal length, we will denote it with $f$. It's worth to remember the focal length since it will appear again later in the math.


## Modeling Projection

## camera coordinate system in 3D



- We'll denote the image axes with $x$ and $y$. An image we see is of course represented with these axes. We'll call this an image coordinate system.
- The tricky part is how to get from the camera's coordinate system (3D) to the image coordinate system (2D).


## Modeling Projection

## camera coordinate system in 3D



- Let's take some point $\mathbf{Q}$ in 3D. $\mathbf{Q}$ "lives" relative to the camera; its coordinates are assumed to be in camera's coordinate system.


## Modeling Projection

## camera coordinate system in 3D



- We call the line from $\mathbf{Q}$ to camera center a projection line.


## Modeling Projection

## camera coordinate system in 3D



- The projection line intersects the image plane in a point $\mathbf{q}$. This is the point we see in our image.


## Modeling Projection

## camera coordinate system in 3D



- First thing to notice is that all points from Q's projection line project to the same point $\mathbf{q}$ in the image!
- Ambiguity: It's impossible to know how far a 3D point is from the camera along the projection line by looking only at the image (point $\mathbf{q}$ ).


## Modeling projection



From the movie Bone Collector

- Ambiguity: It's impossible to know how far a 3D point is from the camera along the projection line by looking only at the image (point $\mathbf{q}$ ).
- It's impossible to know the real 3D size of objects just from an image
- Why did the detective put a dollar bill next to the footprint?
- How would you compute the shoe's dimensions?


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## Projection: Ready for Math

[Pic from: Zisserman \& Hartley]


## Projection Equations

- Using similar triangles:

$$
\mathbf{Q}=(X, Y, Z)^{T} \quad \rightarrow \quad\left(\frac{f \cdot X}{Z}, \frac{f \cdot Y}{Z}, f\right)^{T}
$$

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$$

- This is relative to principal point $\mathbf{p}$. To move the origin to $(0,0)$ in image:

$$
\mathbf{q}=(X, Y, Z)^{T} \quad \rightarrow \quad\left(\frac{f \cdot X}{Z}+p_{x}, \frac{f \cdot Y}{Z}+p_{y}, f\right)^{T}
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where $\mathbf{p}=\left(p_{x}, p_{y}\right)$ is the principal point

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- Get the projection by throwing the last coordinate:

$$
\mathbf{Q}=(X, Y, Z)^{T} \quad \rightarrow \quad \mathbf{q}=\left(\frac{f \cdot X}{Z}+p_{x}, \frac{f \cdot Y}{Z}+p_{y}\right)^{T}
$$

- This is NOT a linear transformation as a division by $Z$ is non-linear


## Homogeneous Coordinates!

- We will use homogeneous coordinates, which simply append a 1 to the vector

Homogeneous coordinates to the rescue!

$$
\begin{array}{cc}
(x, y) \Rightarrow\left[\begin{array}{c}
x \\
y \\
1
\end{array}\right] & (x, y, z) \Rightarrow\left[\begin{array}{l}
x \\
y \\
z \\
1
\end{array}\right] \\
\begin{array}{c}
\text { homogeneous image } \\
\text { coordinates }
\end{array} & \text { homogeneous scene } \\
\text { coordinates }
\end{array}
$$

Converting from homogeneous coordinates

$$
\left[\begin{array}{c}
x \\
y \\
w
\end{array}\right] \Rightarrow(x / w, y / w) \quad\left[\begin{array}{l}
x \\
y \\
z \\
w
\end{array}\right] \Rightarrow(x / w, y / w, z / w)
$$

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- In homogeneous coordinates, scaling doesn't affect anything:

$$
\left[\begin{array}{l}
x \\
y \\
1
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w \cdot x \\
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- In Projective Geometry, all points are equal under scaling


## Useful Trivia about Homogeneous Coordinates

- Homogeneous coordinates are quite useful in general. Let's see why
- Let's look at equation of a line in 2D: $a x+b y+c=0$


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- So if I have a line and someone gives me a point ( $x, y$ ), how do I quickly check if the point lies on the line? Homogeneous coordinates, and check if dot product is 0 .


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- Ok, what if I give you two points $\left(x_{1}, y_{1}\right)$ and $\left(x_{2}, y_{2}\right)$ and I ask you to write an equation for the line between them?


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- You can solve a linear system. But it's much easier in homogeneous coordinates: Since both points lie on a line, the homogeneous vectors are both "orthogonal" to the line vector I (dot product 0).


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- You can solve a linear system. But it's much easier in homogeneous coordinates: Since both points lie on a line, the homogeneous vectors are both "orthogonal" to the line vector I (dot product 0).
- We know that a vector orthogonal to two vectors is a cross product between them: $\mathbf{I}=\left(x_{1}, y_{1}, 1\right)^{T} \times\left(x_{2}, y_{2}, 1\right)^{T}$. And this is easy to compute.


## Back to Perspective Projection

- We currently have this (the nasty division by $Z$ ):

$$
\mathbf{Q}=(X, Y, Z)^{T} \quad \rightarrow \quad \mathbf{q}=\left[\begin{array}{l}
\frac{f \cdot X}{f}+p_{x} \\
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- Write this with homogeneous coordinates:

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\frac{f \cdot X}{Z}+p_{x} \\
\frac{f \cdot Y}{Z}+p_{y} \\
1
\end{array}\right] \sim\left[\begin{array}{c}
f \cdot X+Z \cdot p_{x} \\
f \cdot Y+Z \cdot p_{y} \\
Z
\end{array}\right]
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Z
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$$

- We can now write this as matrix multiplication:

$$
\mathbf{Q}=\left[\begin{array}{l}
X \\
Y \\
Z
\end{array}\right] \rightarrow\left[\begin{array}{c}
f \cdot X+Z \cdot p_{x} \\
f \cdot Y+Z \cdot p_{y} \\
Z
\end{array}\right]=\left[\begin{array}{ccc}
f & 0 & p_{x} \\
0 & f & p_{y} \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
X \\
Y \\
Z
\end{array}\right]
$$

## Camera Intrinsics

- From previous slide:

$$
\mathbf{Q}=\left[\begin{array}{l}
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\end{array}\right]\left[\begin{array}{c}
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Y \\
Z
\end{array}\right]
$$

- Write:

$$
K=\left[\begin{array}{llc}
f & 0 & p_{x} \\
0 & f & p_{y} \\
0 & 0 & 1
\end{array}\right]
$$

This is called a camera calibration matrix or intrinsic parameter matrix. The parameters in $K$ are called internal camera parameters.

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- Finally: $\left[\begin{array}{c}w \cdot x \\ w \cdot y \\ w\end{array}\right]=K\left[\begin{array}{l}X \\ Y \\ Z\end{array}\right] \rightarrow \mathbf{q}=\left[\begin{array}{l}x \\ y\end{array}\right]$
[Source: Zisserman \& Hartley]


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- It can be a little more complicated. Pixels may not be square:

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K=\left[\begin{array}{ccc}
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f_{x} & 0 & p_{x} \\
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$$

- And there might be a skew angle $\theta$ between $x$ and $y$ image axis:

$$
K=\left[\begin{array}{ccc}
f_{x} & -f_{x} \cot \theta & p_{x} \\
0 & f_{y} / \sin \theta & p_{y} \\
0 & 0 & 1
\end{array}\right]
$$

[Source: Zisserman \& Hartley]

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[Source: Zisserman \& Hartley]

## Perspective Projection


[Source: N. Snavely]

## Dimensionality Reduction Machine (3D to 2D)



Point of observation


## What have we lost?

- Angles
- Distances (lengths)


## Projection properties

- Many-to-one: any points along same ray map to same point in image


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- Points $\rightarrow$ points


## Projection properties

- Many-to-one: any points along same ray map to same point in image
- Points $\rightarrow$ points
- Lines $\rightarrow$ lines. Why?



## Projection properties



Figure: Proof by drawing

## Projection properties



Figure: Proof by drawing

## Projection properties

- Many-to-one: any points along same ray map to same point in image
- Points $\rightarrow$ points
- Lines $\rightarrow$ lines
- But line through principal point projects to a point. Why?


Figure: Can you tell where is the principal point?

## Projection properties

- Many-to-one: any points along same ray map to same point in image
- Points $\rightarrow$ points
- Lines $\rightarrow$ lines
- But line through principal point projects to a point. Why?
- Planes $\rightarrow$ planes



## Projection properties

- Many-to-one: any points along same ray map to same point in image
- Points $\rightarrow$ points
- Lines $\rightarrow$ lines
- But line through principal point projects to a point. Why?
- Planes $\rightarrow$ planes
- But plane through principal point which is orthogonal to image plane projects to line. Why?



## Projection Properties: Cool Facts

Parallel lines converge at a vanishing point

- Each different direction in the world has its own vanishing point

[Adopted from: N. Snavely, R. Urtasun]


## Projection Properties: Cool Facts

Parallel lines converge at a vanishing point

- Each different direction in the world has its own vanishing point
- All lines with the same 3D direction intersect at the same vanishing point

[Pic: R. Szeliski]


## Projection Properties: Vanishing Point

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- Line that passes through $\mathbf{V}$ with direction $\mathbf{D}: \mathbf{X}=\mathbf{V}+t \mathbf{D}$.


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- All lines with the same 3D direction intersect at the same vanishing point. Why?
- Line that passes through $\mathbf{V}$ with direction $\mathbf{D}: \mathbf{X}=\mathbf{V}+t \mathbf{D}$.
- Project it:

$$
\left[\begin{array}{c}
w x \\
w y \\
w
\end{array}\right]=K \mathbf{X}=\left[\begin{array}{ccc}
f & 0 & p_{x} \\
0 & f & p_{y} \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
V_{x}+t D_{x} \\
V_{y}+t D_{y} \\
V_{z}+t D_{z}
\end{array}\right]=\left[\begin{array}{c}
f V_{x}+f t D_{x}+p_{x} V_{z}+t p_{x} D_{z} \\
f V_{y}+f t D_{y}+p_{y} V_{z}+t p_{y} D_{z} \\
V_{z}+t D_{z}
\end{array}\right]
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V_{z}+t D_{z}
\end{array}\right]
$$

- Send $t \rightarrow \infty$ and compute $x$ and $y$ :

$$
\begin{aligned}
& x=\lim _{t \rightarrow \infty} \frac{f V_{x}+f t D_{x}+p_{x} V_{z}+t p_{x} D_{z}}{V_{z}+t D_{z}}=\frac{f D_{x}+p_{x} D_{z}}{D_{z}} \\
& y=\lim _{t \rightarrow \infty} \frac{f V_{y}+f t D_{y}+p_{y} V_{z}+t p_{y} D_{z}}{V_{z}+t D_{z}}=\frac{f D_{y}+p_{y} D_{z}}{D_{z}}
\end{aligned}
$$

## Projection Properties: Vanishing Point

- All lines with the same 3D direction intersect at the same vanishing point. Why?
- Line that passes through $\mathbf{V}$ with direction $\mathbf{D}: \mathbf{X}=\mathbf{V}+t \mathbf{D}$.
- Project it:

$$
\left[\begin{array}{c}
w x \\
w y \\
w
\end{array}\right]=K \mathbf{X}=\left[\begin{array}{ccc}
f & 0 & p_{x} \\
0 & f & p_{y} \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
V_{x}+t D_{x} \\
V_{y}+t D_{y} \\
V_{z}+t D_{z}
\end{array}\right]=\left[\begin{array}{c}
f V_{x}+f t D_{x}+p_{x} V_{z}+t p_{x} D_{z} \\
f V_{y}+f t D_{y}+p_{y} V_{z}+t p_{y} D_{z} \\
V_{z}+t D_{z}
\end{array}\right]
$$

- Send $t \rightarrow \infty$ and compute $x$ and $y$ :

$$
\begin{aligned}
& x=\lim _{t \rightarrow \infty} \frac{f V_{x}+f t D_{x}+p_{x} V_{z}+t p_{x} D_{z}}{V_{z}+t D_{z}}=\frac{f D_{x}+p_{x} D_{z}}{D_{z}} \\
& y=\lim _{t \rightarrow \infty} \frac{f V_{y}+f t D_{y}+p_{y} V_{z}+t p_{y} D_{z}}{V_{z}+t D_{z}}=\frac{f D_{y}+p_{y} D_{z}}{D_{z}}
\end{aligned}
$$

- This doesn't depend on $\mathbf{V}$ ! So all lines with direction $\mathbf{D}$ go to this point!


## Projection Properties: Vanishing Point

- All lines with the same 3D direction intersect at the same vanishing point.


## Projection Properties: Vanishing Point

- All lines with the same 3D direction intersect at the same vanishing point.
- The easiest way to find this point: Translate line with direction $\mathbf{D}$ to the camera center. This line intersects the image plane in the vanishing point corresponding to direction D! Why?



## Projection Properties: Cool Facts

## Parallel lines converge at a vanishing point

- Each different direction in the world has its own vanishing point
- Lines parallel to image plane are also parallel in the image (we say that they intersect at infinity). Why?


In 3D: parailiel to image plane In 2D: parallel (no VP)

## Projection Properties: Cool Facts

- Lines parallel to image plane are also parallel in the image. We say that they intersect at infinity.
doesn't intersect image plane! So no vanishing point!



## Projection Properties: Cool Facts

- Lines parallel to image plane are also parallel in the image. We say that they intersect at infinity.
doesn't intersect image plane! So no vanishing point!

parallel lines in the world, parallel to image plane


## Projection Properties: Cool Tricks

- This picture has been recorded from a car with a camera on top. We know the camera intrinsic matrix $K$.
- Can we tell the incline of the hill we are driving on?
- How?



## Projection Properties: Cool Tricks

- Can we tell the incline of the hill we are driving on?


Figure: This is the 3D world behind the picture.

## Projection Properties: Cool Tricks

- Can we tell the incline of the hill we are driving on?


Figure: If we compute the 3D direction of the house's vertical lines relative to camera, we have the incline! How can we do that?

## Projection Properties: Cool Tricks

- Can we tell the incline of the hill we are driving on?
meet at a vanishing point


Figure: Extract "vertical" lines and compute vanishing point. How can we compute direction in 3D from vanishing point (if we have $K$ )?

## Projection Properties: Cool Tricks

- Can we tell the incline of the hill we are driving on?


Figure: This picture should help.

## Projection Properties: Cool Tricks

- Can we tell the incline of the hill we are driving on?

- We have:

$$
\left[\begin{array}{c}
w \cdot v p_{x} \\
w \cdot v p_{y} \\
w
\end{array}\right]=K \mathbf{D} \quad \rightarrow \quad \mathbf{D}=w K^{-1}\left[\begin{array}{c}
v p_{x} \\
v p_{y} \\
1
\end{array}\right] \quad \rightarrow \quad \text { normalize } \mathbf{D} \text { to norm } 1
$$

## Vanishing Points Can be Deceiving

- Parallel lines converge at a vanishing point.
- But intersecting lines in 2D are not necessary parallel in 3D.

[Source: A. Jepson]


## Projection Properties: Cool Facts

## Parallel lines converge at a vanishing point

- Each different direction in the world has its own vanishing point
- For lines on the same 3D plane, the vanishing points lie on a line. We call it a vanishing line. Vanishing line for the ground plane is a horizon line.



## Projection Properties: Cool Facts

## Parallel lines converge at a vanishing point

- For lines on the same 3D plane, the vanishing points lie on a line. We call it a vanishing line. Vanishing line for the ground plane is a horizon line.
- Some horizon lines are nicer than others ;)


Punta Cana

## Projection Properties: Cool Facts

## Parallel lines converge at a vanishing point

- For lines on the same 3D plane, the vanishing points lie on a line. We call it a vanishing line or a horizon line.
- Parallel planes in 3D have the same horizon line in the image.



## Projection Properties: Cool Facts

- Can I tell how much above ground this picture was taken?



## Projection Properties: Cool Facts

- Can I tell how much above ground this picture was taken?



## Projection Properties: Cool Facts

- Same distance as where the horizon intersects a building



## Projection Properties: Cool Facts

- Same distance as where the horizon intersects a building: 50 floors up



## Projection Properties: Cool Facts

- This is only true when the camera (image plane) is orthogonal to the ground plane. And the ground plane is flat.
- A very nice explanation of this phenomena can be find by Derek Hoiem here: https://courses.engr.illinois.edu/cs543/sp2011/materials/3dscene_ book_svg.pdf



## Orthographic Projection



## Orthographic Projection


[Source: R. Urtasun]

- Requires no division and simply drops the $Z$ coordinate.


## Orthographic Projection


[Source: R. Urtasun]

- Requires no division and simply drops the $Z$ coordinate.
- Orthographic projection:

$$
\mathbf{Q}=\left[\begin{array}{l}
X \\
Y \\
Z \\
1
\end{array}\right] \rightarrow\left[\begin{array}{l}
X \\
Y \\
1
\end{array}\right]=\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
X \\
Y \\
Z \\
1
\end{array}\right]
$$

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1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
X \\
Y \\
Z \\
1
\end{array}\right]
$$

- Special case of perspective projection where the distance from the camera center to the image plane is infinity


## Orthographic Projection


[Source: N. Snavely]

## Orthographic Projection



Perspective projection


Parallel (orthographic) projection

- For perspective projection lines parallel in 3D are not parallel in the image.
- For orthographic projection lines parallel in 3D are parallel in the image.
[Source: A. Torralba]


## Camera Parameters

We are not yet done with projection. To fully specify projection, we need to:

- Describe its internal parameters (we know this, this is our K)


## Camera Parameters

We are not yet done with projection. To fully specify projection, we need to:

- Describe its internal parameters (we know this, this is our K)
- Describe its pose in the world. Two important coordinate systems:
- World coordinate system
- Camera coordinate system

[Source: N. Snavely, slide credit: R. Urtasun]


## Camera Parameters

- Why two coordinate systems?


Figure: Imagine this is your room.

## Camera Parameters

- Why two coordinate systems?


Figure: When you were furnishing you measured everything in detail.

## Camera Parameters

- Why two coordinate systems?


I measured everything in my room relative to this point
Figure: Thus you know all coordinates relative to a special point (origin) and coordinate system in the room. This is your room's (world) coordinate system.

## Camera Parameters

- Why two coordinate systems?


But to project my room to camera, I need to have the room in the camera coordinate system!

Figure: Now you take a picture and you wonder how points project to camera. In order to project, you need all points in camera's coordinate system.

## Camera Parameters

- Why two coordinate systems?

Gives 3D point cloud


Camera (RGB)

Figure: For e.g. self-driving cars, 3D points are typically measured with Velodyne.

## Camera Parameters

- Why two coordinate systems?


Figure: We want to be able to project the 3D points in Velodyne's coordinate svstem onto an image captured by a camera

## Camera Parameters

- Why two coordinate systems?


Figure: We want to be able to project the 3D points in Velodyne's coordinate system onto an image captured by a camera.

## Projection

To project a point $(X, Y, Z)$ in world coordinates on the image plane, we need to:

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## Projection

To project a point $(X, Y, Z)$ in world coordinates on the image plane, we need to:

- Transform $(X, Y, Z)$ into camera coordinates. We thus need:
- Camera position (in world coordinates)
- Camera orientation (in world coordinates)


## Projection

To project a point $(X, Y, Z)$ in world coordinates on the image plane, we need to:

- Transform $(X, Y, Z)$ into camera coordinates. We thus need:
- Camera position (in world coordinates)
- Camera orientation (in world coordinates)
- To project into the image plane
- Need to know camera intrinsics


## Projection

To project a point $(X, Y, Z)$ in world coordinates on the image plane, we need to:

- Transform $(X, Y, Z)$ into camera coordinates. We thus need:
- Camera position (in world coordinates)
- Camera orientation (in world coordinates)
- To project into the image plane
- Need to know camera intrinsics
- These can all be described with matrices!
[Source: N. Snavely, slide credit: R. Urtasun]


## Camera Extrinsics



Figure: We first need our camera position and orientation in the room's world.

## Camera Extrinsics


c ... camera position in room coordinate system
$\mathbf{u}, \mathbf{v}, \mathbf{w} . . .3$ orthogonal directions of camera in room coordinate system

## Camera Extrinsics

## What is Q in camera's coordinate system??



Q - c ... makes position relative to camera
c ... camera position in room coordinate system
$\mathbf{u}, \mathbf{v}, \mathbf{w} \ldots 3$ orthogonal directions of camera in room coordinate system

## Camera Extrinsics

## What is Q in camera's coordinate system??



$$
\begin{array}{lll}
\mathbf{Q}-\mathbf{c} & \ldots & \text { makes position relative to camera } \\
R\left[\begin{array}{lll}
\mathbf{u} & \mathbf{v} & \mathbf{w}
\end{array}\right]=I & \text { (looking for rotation } \\
\text { to canonical orientation) }
\end{array}
$$

C ... camera position in room coordinate system
$\mathbf{u}, \mathbf{v}, \mathbf{w}$... 3 orthogonal directions of camera in room coordinate system

## Camera Extrinsics



## What is Q in camera's coordinate system??

Q - c ... makes position relative to camera

$$
R\left[\begin{array}{lll}
\mathbf{u} & \mathbf{v} & \mathbf{w}
\end{array}\right]=I \quad \begin{aligned}
& \quad \begin{array}{l}
\text { (looking for rotation } \\
\text { to canonical orientation) }
\end{array}
\end{aligned}
$$

$R \cdot R^{T}=I \quad$ (since orientation is orthogonal matrix)
c ... camera position in room coordinate system
$\mathbf{u}, \mathbf{v}, \mathbf{w} \ldots 3$ orthogonal directions of camera in room coordinate system

## Camera Extrinsics



C ... camera position in room coordinate system
$\mathbf{u}, \mathbf{v}, \mathbf{w} . . .3$ orthogonal directions of camera in room coordinate system

## Camera Extrinsics



Figure: Final Transformation

## Projection Equations

- Projection matrix $P$ models the cumulative effect of all intrinsic and extrinsic parameters. We use homogeneous coordinates for 2D and 3D:

$$
\mathbf{q}=\left[\begin{array}{c}
a x \\
a y \\
a
\end{array}\right]=\mathbf{P}\left[\begin{array}{c}
X \\
Y \\
Z \\
1
\end{array}\right]
$$

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X \\
Y \\
Z \\
1
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$$

- It can be computed as

$$
\mathbf{P}=\underbrace{\left[\begin{array}{lll}
f & 0 & p_{x} \\
0 & f & p_{y} \\
0 & 0 & 1
\end{array}\right]}_{\text {intrinsics } K} \underbrace{\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0
\end{array}\right]}_{\text {projection }} \underbrace{\left[\begin{array}{cc}
\mathbf{R}_{3 \times 3} & 0_{3 \times 1} \\
0_{1 \times 3} & 1
\end{array}\right]}_{\text {rotation }} \underbrace{\left[\begin{array}{cc}
\mathbf{I}_{3 \times 3} & \mathbf{T}_{3 \times 1} \\
0_{1 \times 3} & 1
\end{array}\right]}_{\text {translation }}
$$

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- Projection matrix $P$ models the cumulative effect of all intrinsic and extrinsic parameters. We use homogeneous coordinates for 2D and 3D:

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\mathbf{I}_{3 \times 3} & \mathbf{T}_{3 \times 1} \\
0_{1 \times 3} & 1
\end{array}\right]}_{\text {translation }}
$$

- To get a point $\mathbf{q}$ in the image plane, I need to compute $\mathbf{P}(X, Y, Z, 1)^{T}$, where $\mathbf{P}$ is a $3 \times 4$ matrix. This gives me a $3 \times 1$ vector. Now I divide all coordinates with the third coordinate (making the third coordinate equal to $1)$, and then drop the last coordinate. As simple as that.


## The Projection Matrix

- The projection matrix is defined as

$$
\mathbf{P}=\underbrace{\mathbf{K}}_{\text {intrinsics }} \underbrace{\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0
\end{array}\right]}_{\text {projection }} \underbrace{\left[\begin{array}{lll}
\mathbf{R}_{3 \times 3} & 0_{3 \times 1} \\
0_{1 \times 3} & 1
\end{array}\right]}_{\text {rotation }} \underbrace{\left[\begin{array}{cc}
\mathbf{I}_{3 \times 3} & \mathbf{T}_{3 \times 3} \\
0_{1 \times 3} & 1
\end{array}\right]}_{\text {translation }}
$$

- More compactly

$$
\mathbf{P}=\mathbf{K}\left[\begin{array}{ll}
\mathbf{R} & \mathbf{t}
\end{array}\right]
$$

- Sometimes you will see notation:

$$
\mathbf{P}=\mathbf{K}[\mathbf{R} \mid \mathbf{t}]
$$

It's the same thing.

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\mathbf{R} & \mathbf{t}
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- Sometimes you will see notation:

$$
\mathbf{P}=\mathbf{K}[\mathbf{R} \mid \mathbf{t}]
$$

It's the same thing.

- This might look complicated. Truth is, in most cases you don't have $\mathbf{P}$ at all, so you can't really compute any projections. When you have a calibrated camera, then someone typically gives you $\mathbf{P}$. And then projection is easy.


## A Short Note on Camera Calibration



Detect corners in image and figure out which corner corresponds to which point in the 3D pattern.


You measured all distances for this pattern.

The general procedure:

- Place a 3D pattern (for which you know all distances) in front of camera.
- Take a picture. Detect corners in image and find correspondences with the points in the pattern.
- Go to the internet and check out the math that tells you how to compute $K$ from these 2D-3D correspondences. ;) We won't cover in class.
[Pic from: R. Duraiswami]


## Camera Calibration: Interesting Fact

- Let's say you have an image but you don't know anything about the camera (for example, image downloaded from the web).
- For images where you see lines corresponding to 3 orthogonal directions, like cubes or rooms, you can compute the camera matrix $K$ as well as $R$ and $t$ !

- How to do this is explained in the Zisserman \& Hartley book.


## Projection Properties: Cool Facts

- As a consequence, for scenes with lots of lines (e.g. man-made scenes) one can reconstruct the scene in 3D from a single image!



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## Projection Properties: Cool Facts

- As a consequence, for scenes with lots of lines (e.g. man-made scenes) one can reconstruct the scene in 3D from a single image!
- For those interested, check out the math here:


## A. Criminisi, I. Reid, and A. Zisserman

## Single View Metrology

International Journal of Computer Vision, vol 40, num 2, 2000
http://www.cs.cmu.edu/ ph/869/papers/Criminisi99.pdf

## Inserting Objects


link to video

## Camera Calibration: Another Interesting Fact



- From a longer video in which the sun travels across the sky you can compute the camera intrinsic matrix, as well as extrinsic, i.e., the GPS location where you are! Well, up to a 100 km accuracy...


## Camera Calibration: Another Interesting Fact

> J.-F. Lalonde, S. G. Narasimhan, and A. A. Efros

> What Do the Sun and Sky Tell Us About the Camera?
> International Journal on Computer Vision, 88(1), May 2010
> Paper: http://vision.gel.ulaval.ca/~jflalonde/projects/ sky/index.html
> Code: https://github.com/jflalonde/webcamCalibration

- From a longer video in which the sun travels across the sky you can compute the camera intrinsic matrix, as well as extrinsic, i.e., the GPS location where you are! Well, up to a 100 km accuracy...
- Is this useful? Maybe, to catch terrorists that record their videos outside.


## Exercise (Not Very Easy, But Fun)

- We want to render (project) a 3D CAD model of a car to this image in a realistic way
- How?



## Exercise

- First get a CAD model. There are tones of them, e.g. 3D Warehouse (free)
- https://3dwarehouse.sketchup.com/search.html?q=car\&backendClass=entity



## Exercise

- We downloaded this model. Now what?


Figure: A CAD model is a collection of 3D vertices and faces that connect the vertices. Each face represents a small triangle. It typically has color.

## Exercise

- Our image was collected with a car on the road:
- A camera was on top of the car, approximately 1.7 m above ground
- Image plane is orthogonal to the ground
- We have the internal parameters of the camera, $\mathbf{K}$.



## Exercise

- Our image was collected with a car on the road:
- A camera was on top of the car, approximately 1.7 m above ground
- Image plane is orthogonal to the ground
- We have the internal parameters of the camera, $\mathbf{K}$.
- With a little bit of math, we can compute the ground plane in 3D, relative to camera. We a bit more math we can compute which point on the ground plane projects to an image point $(x, y)$.


## How?

- We can now "place" our CAD model to this point (compute $R$ and $\mathbf{t}$ )


## Exercise

- Our image was collected with a car on the road:
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- We have the internal parameters of the camera, $\mathbf{K}$.
- With a little bit of math, we can compute the ground plane in 3D, relative to camera. We a bit more math we can compute which point on the ground plane projects to an image point $(x, y)$.


## How?

- We can now "place" our CAD model to this point (compute $R$ and $\mathbf{t}$ )
- Rendering:

Compute $[a x, a y, a]^{T}=K[R \mid \mathbf{t}][X, Y, Z, 1]^{T}$ for each CAD vertex $[X, Y, Z]^{T}$. Divide $[a x, a y, a]^{T}$ with third coord and drop it.

## Exercise

- That's it. Make a video for more fun



## Exercise

- That's it. Make a video for more fun



## Exercise

- That's it. Make a video for more fun



## Can we Turn Fun into Useful?

- Can we use this in some more practical (useful) application?


## Can we Turn Fun into Useful?

- Generate 3D boxes and score (classifier on some image features)

X. Chen, K. Kundu, Y. Zhu, A. Berneshawi, H. Ma, S. Fidler, R. Urtasun. 3D Object Proposals for Accurate Object Class Detection. NIPS'15


## Can we Turn Fun into Useful?

## Car

|  | Method | Setting | Code | Moderate | Easy | Hard | Runtime | Environment | Compare |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | DenseBox2 |  |  | 89.32 \% | 93.94\% | 79.81\% | 5 s | GPU (e) 2.5 Ghz (C/C++) | $\bigcirc$ |
| L. Huang, Y. Yang, Y. Deng and Y. Yu: DenseBox: Unifying Landmark Localization with End to End Obiect Detection. ArXiv e-prints 2015. |  |  |  |  |  |  |  |  |  |
| 2 | DJML |  |  | 88.79 \% | 91.31\% | 77.73 \% | x s | GPU @ 1.5 Ghz (Matlab + C/C++) | 0 |
| 3 | 3DOP | ช0才 |  | 88.64\% | 93.04\% | 79.10\% | 3 s | GPU @ 2.5 Ghz (Matlab + C/C++) | $\square$ |
| X. Chen, K. Kundu, Y. Zhu, A. Berneshawi, H. Ma, S. Fidler and R. Urtasun: 3D Object Proposals for Accurate Object Class Detection. NIPS 2015. |  |  |  |  |  |  |  |  |  |
| 4 | SubCNN |  |  | 88.16\% | 90.89\% | $77.06 \%$ | 2 s | GPU @ 2.5 Ghz (Python + C/C++) | $\bigcirc$ |
| Anonymous submission |  |  |  |  |  |  |  |  |  |
| 5 | Mono3D |  |  | 86.72\% | 90.08\% | 77.88\% | x s | GPU @ 2.5 Ghz (Matlab + C/C++) | 0 |
| Anonymous submission |  |  |  |  |  |  |  |  |  |
| 6 | DenseBoxV2 L |  |  | 84.92 \% | 88.77\% | 70.00\% | 0.04 s | GPU @ 2.0 Ghz (C/C++) | $\square$ |

L. Huang, Y. Yang, Y. Deng and Y. Yu: DenseBox: Unifying Landmark Localization with End to End Object Detection. ArXiv e-prints 2015.

## Cyclist

|  | Method | Setting | Code | Moderate | Easy | Hard | Runtime | Environment | Compare |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3DOP | - |  | 68.94 \% | 78.39\% | 61.37\% | 3 s | GPU @ 2.5 Ghz (Matlab + C/C++) | O |
| X. Chen, K. Kundu, Y. Zhu, A. Berneshawi, H. Ma, S. Fidler and R. Urtasun: 3 D Object Proposals for Accurate Object Class Detection. NIPS 2015. |  |  |  |  |  |  |  |  |  |
| 2 | Mono3D |  |  | $63.17 \%$ | 76.82\% | 55.68\% | X 5 | GPU @ 2.5 Ghz (Matlab + C/C++) | $\square$ |
| Anonymous submission |  |  |  |  |  |  |  |  |  |
| 3 | SDP |  |  | 61.87\% | 73.59\% | 54.29\% | 1 s | GPU @ 2.5 Ghz (C/C++) | $\square$ |
| Anonymous submission |  |  |  |  |  |  |  |  |  |
| 4 | SubCNN |  |  | 59.70\% | 74.15\% | 53.08\% | 2 s | GPU @ 2.5 Ghz (Python + C/C++) | $\square$ |
| Anonymous submission |  |  |  |  |  |  |  |  |  |
| 5 | Regionlets |  |  | 58.72\% | 70.41\% | 51.83\% | 1 s | >8 cores@2.5 Ghz (C/C++) | $\square$ |
| X. Wang, M. Yang, S. Zhu and Y. Lin: Regionlets for Generic Object Detection. International Conference on Computer Vision 2013. <br> C. Long, X. Wang, G. Hua, M. Yang and Y. Lin: Accurate Oblect Detection with Location Relaxation and Regionlets Relocalization. Asian Conference on Computer Vision 2014. |  |  |  |  |  |  |  |  |  |
| 6 | MV-RGBD-RF | -\% |  | 42.61\% | 52.97\% | $37.42 \%$ | 4 s | 4 cores @ 2.5 Ghz (C/C++) | $\square$ |

A. Gonzalez, G. Villalonga, J. Xu, D. Vazquez, J. Amores and A. Lopez: Multiview Random Forest of Local Experts Combining RGB and LIDAR data for Pedestrian Detection. IEEE Intelligent Vehicles

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A Little More on Camera Models

