Depth from Stereo

All points on the projective line to P map to p

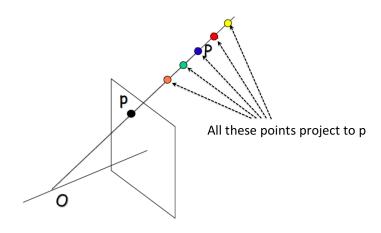
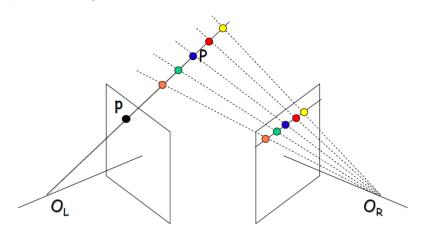


Figure: One camera

 All points on projective line to P in left camera map to a line in the image plane of the right camera



If I search this line to find correspondences...

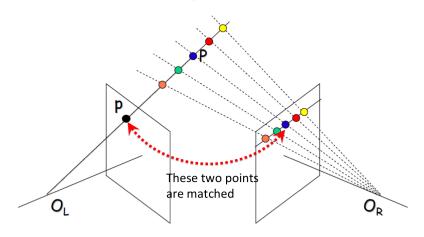


Figure: If I am able to find corresponding points in two images...

I can get 3D!

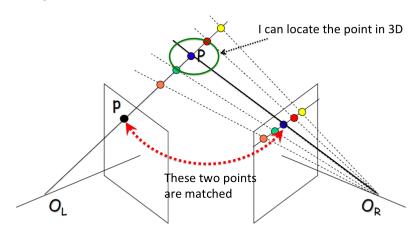


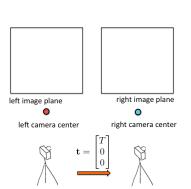
Figure: I can get a point in 3D by triangulation!

Stereo

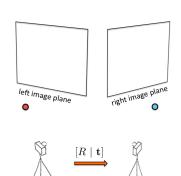
Epipolar geometry

- Case with two cameras with parallel optical axes
- General case

Parallel stereo cameras:



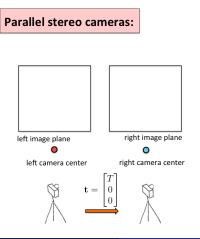
General stereo cameras:



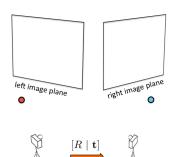
Stereo

Epipolar geometry

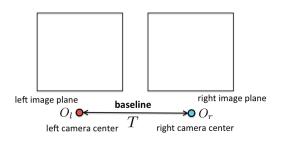
- Case with two cameras with parallel optical axes ← First this
- General case

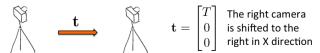


General stereo cameras:

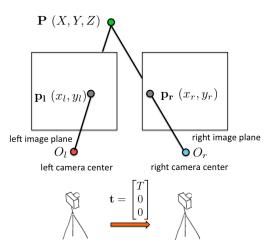


 We assume that the two calibrated cameras (we know intrinsics and extrinsics) are parallel, i.e. the right camera is just some distance to the right of left camera. We assume we know this distance. We call it the baseline.

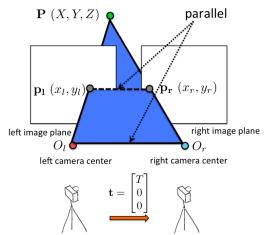




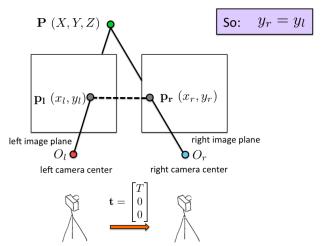
• Pick a point P in the world



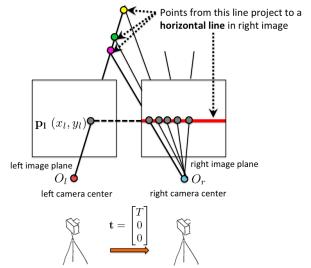
• Points O_I , O_r and P (and p_I and p_r) lie on a plane. Since two image planes lie on the same plane (distance f from each camera), the lines O_IO_r and p_Ip_r are parallel.



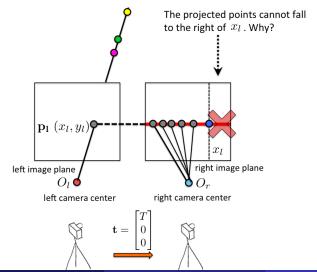
• Since lines O_1O_r and p_lp_r are parallel, and O_l and O_r have the same y, then also p_l and p_r have the same y: $y_r = y_l$!



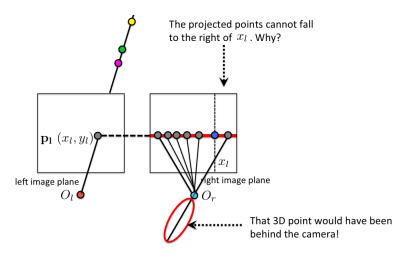
• So all points on the projective line O_1p_1 project to a horizontal line with $y = y_1$ on the right image. This is nice, let's remember this.



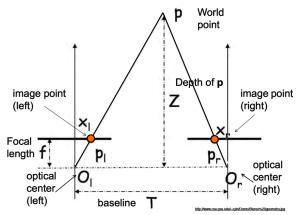
• Another observation: No point from O_lp_l can project to the right of x_l in the right image. Why?



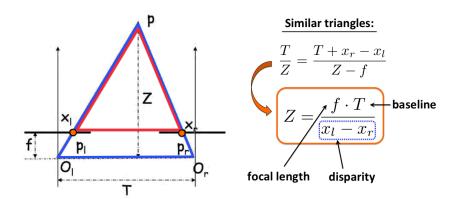
Because that would mean our image can see behind the camera...



• Since our points $\mathbf{p_l}$ and $\mathbf{p_r}$ lie on a horizontal line, we can forget about y_l for a moment (it doesn't seem important). Let's look at the camera situation from the birdseye perspective instead. Let's see if we can find a connection between x_l , x_r and Z (because Z is what we want).

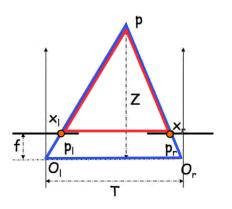


ullet We can then use similar triangles to compute the depth of the point P



[Adopted from: J. Hays]

• We can then use similar triangles to compute the depth of the point P



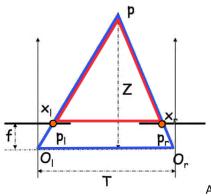
Similar triangles:

$$\frac{T}{Z} = \frac{T + x_l - x_r}{Z - f}$$

$$Z = \frac{f \cdot T}{x_r - x_l}$$

So if I know $\,x_l\,$ and $\,x_r\,$, then I can compute Z!

• We can then use similar triangles to compute the depth of the point P



Similar triangles:

$$\frac{T}{Z} = \frac{T + x_l - x_r}{Z - f}$$

$$Z = \frac{f \cdot T}{x_r - x_l}$$

$$x = \frac{f \cdot X}{Z} + p_x$$

And if I know Z, I can compute X and Y, which gives me the point in 3D

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$?





left image

right image

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching on line $y_r = y_l$.





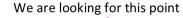
left image

right image

the match will be on this line (same y)

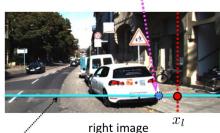
(CAREFUL: this is only true for parallel cameras. Generally, line not horizontal)

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching on line $y_r = y_l$.





left image



the match will be **on the left** of x_l how do I find it?

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

We call this line a scanline





left image

right image

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

How similar?





left image

right image

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

How similar?





left image

right image

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

Most similar. A match!





left image

right image

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .





left image



At each point on the scanline: Compute a matching cost

Matching cost: SSD or normalized correlation

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

$$SSD(\text{patch}_l, \text{patch}_r) = \sum_{x} \sum_{y} (I_{\text{patch}_l}(x, y) - I_{\text{patch}_r}(x, y))^2$$





SSD

left image

Compute a matching cost

Matching cost: SSD (look for minima)



disparity

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .

$$NC(\text{patch}_l, \text{patch}_r) = \frac{\sum_x \sum_y (I_{\text{patch}_l}(x, y) \cdot I_{\text{patch}_r}(x, y))}{||I_{\text{patch}_l}|| \cdot ||I_{\text{patch}_r}||}$$





left image

Norm Corr.



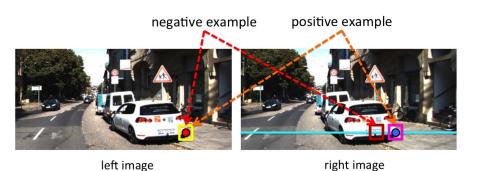
Compute a matching cost

Matching cost: Normalized Corr. (look for maxima)

disparity

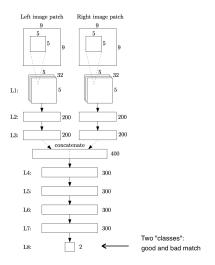
• Version'2015: Can I do this task even better?

• Version'2015: Train a classifier! How can I get ground-truth?



Training examples: get positive and negative matches

Version'2015: Train a Neural Network classifier!



 $[J.\ Zbontar\ and\ Y.\ LeCun:\ Computing\ the\ Stereo\ Matching\ Cost\ with\ a\ Convolutional\ Neural$

- Version'2015: Train a Neural Network classifier!
- To get the most amazing performance

	Method	Setting	Code	Out-Noc	Out-All	Avg-Noc	Avg-All	Density	Runtime	Environment	Compare
1	MC-CNN-acrt		<u>code</u>	2.43 %	3.63 %	0.7 px	0.9 px	100.00 %	67 s	Nvidia GTX Titan X (CUDA, Lua/Torch7)	
Zb	ontar and Y. LeCun	Stereo Mat	ching by	Training a Co	nvolutional	Neural Netwo	ork to Comp	are Image Pat	ches. Submitted	I to JMLR .	
2	<u>Displets</u>		<u>code</u>	2.47 %	3.27 %	0.7 px	0.9 px	100.00 %	265 s	>8 cores @ 3.0 Ghz (Matlab + C/C++)	
Gu	uney and A. Geiger:	Displets: Re	solving S	tereo Ambigu	ities using C	bject Knowle	dge. Confer	ence on Com	puter Vision and	Pattern Recognition (CVPR) 2015.	
3	MC-CNN			2.61 %	3.84 %	0.8 px	1.0 px	100.00 %	100 s	Nvidia GTX Titan (CUDA, Lua/Torch7)	
Zb	ontar and Y. LeCun	Computing	the Ster	eo Matching (Cost with a	Convolutional	Neural Net	work. Confere	nce on Compute	er Vision and Pattern Recognition (CVPR) 2015.	
4	PRSM	±₽	<u>code</u>	2.78 %	3.00 %	0.7 px	0.7 px	100.00 %	300 s	1 core @ 2.5 Ghz (C/C++)	
Vo	ogel, K. Schindler an	d S. Roth: <u>3</u>	D Scene I	Flow Estimat	ion with a P	iecewise Rigio	Scene Mod	<u>el</u> . ijcv 2015.	L		
5	SPS-StFl	⇒Ж		2.83 %	3.64 %	0.8 px	0.9 px	100.00 %	35 s	1 core @ 3.5 Ghz (C/C++)	
Ya	amaguchi, D. McAlle	ster and R. I	Jrtasun:	Efficient Join	t Segmenta	tion, Occlusio	n Labeling,	Stereo and Flo	ow Estimation.	ECCV 2014.	
5	VC-SF	⇒₽		3.05 %	3.31 %	0.8 px	0.8 px	100.00 %	300 s	1 core @ 2.5 Ghz (C/C++)	
	and C Dath and K	Schindler: V	C	istant 3D Sca	ne Flow Est	imation over	Multiple Fra	mes. Proceed	lings of Europea	n Conference on Computer Vision. Lecture Notes in, Com	nuter Science 2
Vo	get, 5. Roth and K.	scilliater. v	iew-cons	indicente de dece							iputer science zi
	Deep Embed	Julinder. <u>v</u>	iew-cons	3.10 %	4.24 %	0.9 px	1.1 px	100.00 %	3 s	1 core @ 2.5 Ghz (C/C++)	puter science zi
7				3.10 %	4.24 %	p	p				
7	Deep Embed			3.10 %	4.24 %	p	p				
7 . Ch	Deep Embed nen, X. Sun, Y. Yu, L			3.10 % : <u>A Deep Vis</u>	4.24 % ual Correspo	ndence Embe	dding Mode	for Stereo Mi	atching Costs. I	CCV 2015.	
7 . Ch	Deep Embed nen, X. Sun, Y. Yu, L JSOSM			3.10 % : <u>A Deep Vis</u>	4.24 % ual Correspo	ndence Embe	dding Mode	for Stereo Mi	atching Costs. I	CCV 2015.	
7 Ch B non	Deep Embed nen, X. Sun, Y. Yu, L JSOSM nymous submission	. Wang and	C. Huang	3.10 % : <u>A Deep Visu</u> 3.15 % 3.28 %	4.24 % yal Correspo 3.94 % 4.07 %	0.8 px	0.9 px	100.00 % 99.98 %	105 s 50 min	8 cores @ 2.5 Ghz (C/C++) 1 core @ 3.0 Ghz (Matlab + C/C++)	

Figure: Performance on KITTI (metrics is error, so lower is better)

• For each point $\mathbf{p_l} = (x_l, y_l)$, how do I get $\mathbf{p_r} = (x_r, y_r)$? By matching. Patch around (x_r, y_r)) should look similar to the patch around (x_l, y_l) .





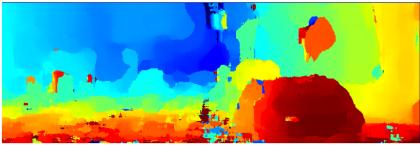
left image

Do this for all the points in the left image!

• We get a disparity map as a result





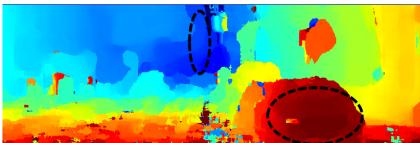


Result: **Disparity map**

• We get a disparity map as a result

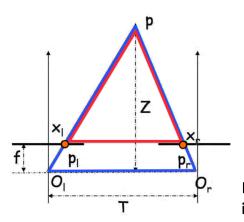






Things that are closer have **larger disparity** than those that are far away from camera. Why?

Depth and disparity are inversely proportional



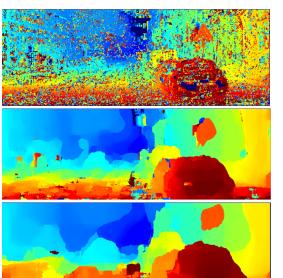
Similar triangles:

$$\frac{T}{Z} = \frac{T + x_l - x_r}{Z - f}$$

$$Z = \underbrace{\frac{f \cdot T}{x_r - x_l}}$$

Depth (Z) and disparity are inversely proportional

• Smaller patches: more detail, but noisy. Bigger: less detail, but smooth



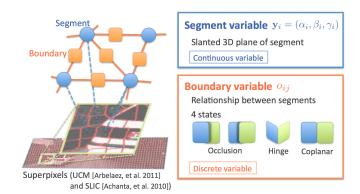
patch size = 5

patch size = 35

patch size = 85

You Can Do It Much Better...

• With Energy Minimization on top, e.g., a Markov Random Field (MRF)

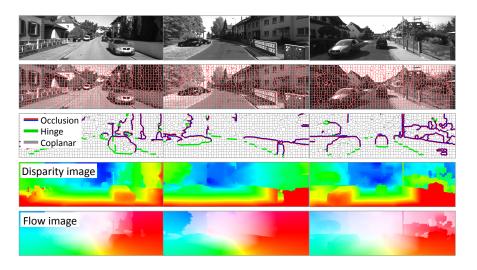


K. Yamaguchi, D. McAllester, R. Urtasun, Efficient Joint Segmentation, Occlusion Labeling, Stereo and Flow Estimation, ECCV 2014

Paper: http://www.cs.toronto.edu/~urtasun/publications/yamaguchi_et_al_eccv14.pdf Code: http://ttic.uchicago.edu/~dmcallester/SPS/index.html

You Can Do It Much Better...

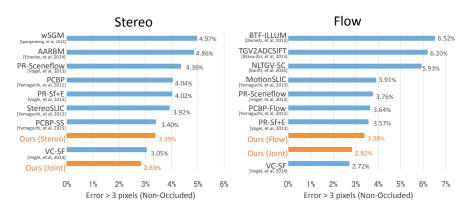
[K. Yamaguchi, D. McAllester and R. Urtasun, ECCV 2014]



Look at State-of-the-art on KITTI

Where "Ours" means: [K. Yamaguchi, D. McAllester and R. Urtasun, ECCV 2014]

• How can we evaluate the performance of a stereo algorithm?



Autonomous driving dataset KITTI: http://www.cvlibs.net/datasets/kitti/

From Disparity We Get...

• Depth: Once you have disparity, you have 3D



Figure: K. Yamaguchi, D. McAllester and R. Urtasun, ECCV 2014

From Disparity We Get...

Money ;)



Stereo

Epipolar geometry

- Case with two cameras with parallel optical axes
- General case ← Next time

