

Normal Forms and Normalization

- A *normal form* is a property of a database schema.
- When a database schema is un-normalized (that is, does not satisfy the normal form), it allows redundancies of various types which can lead to anomalies and inconsistencies.
- Normal forms can serve as basis for evaluating the quality of a database schema and constitutes a useful tool for database design.
- Normalization is a procedure that transforms an unnormalized schema into a normalized one.

Examples of Redundancy

Employee	Salary	Project	Budget	Function
Brown	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55)	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

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Anomalies

- The value of the salary of an employee is repeated in every tuple where the employee is mentioned, leading to a *redundancy*. Redundancies lead to anomalies:
- If salary of an employee changes, we have to modify the value in all corresponding tuples (update anomaly)
- If an employee ceases to work in projects, but stays with company, all corresponding tuples are deleted, leading to loss of information (*deletion anomaly*)

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A new employee cannot be inserted in the relation until the employee is assigned to a project (*insertion anomaly*)

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What's Wrong???

- We are using a single relation to represent data of very different types.
- In particular, we are using a single relation to store the following types of entities, relationships and attributes:
 - Employees and their salaries;
 - Projects and their budgets;
 - Participation of employees in projects, along with their functions.
- To set the problem on a formal footing, we introduce the notion of *functional dependency (FD)*.

Functional Dependencies (FDs) in the Example

Each employee has a unique salary. We represent this dependency as

$\texttt{Employee} \rightarrow \texttt{Salary}$

and say "Salary *functionally depends* on Employee".

Meaning: if two tuples have the same Employee attribute value, they must also have the same salary attribute value

Likewise,

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- $\texttt{Project} \rightarrow \texttt{Budget}$
 - i.e., each project has a unique budget

Functional Dependencies

- Given schema R(X) and non-empty subsets Y and Z of the attributes X, we say that there is a *functional dependency* between Y and Z (Y→Z), iff for every relation instance r of R(X) and every pair of tuples t₁, t₂ of r, if t₁.Y = t₂.Y, then t₁.Z = t₂.Z.
- A functional dependency is a statement about all allowable relations for a given schema.
- Functional dependencies have to be identified by understanding the semantics of the application.
- Given a particular relation r₀ of R(x), we can tell if a dependency holds or not; but just because it holds for r₀, doesn't mean that it also holds for R(x)!

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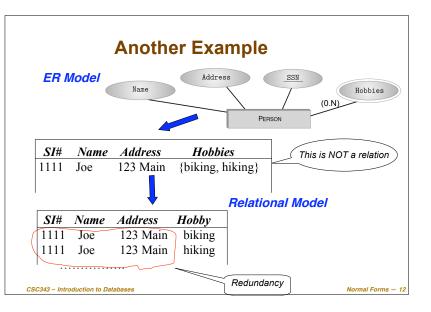
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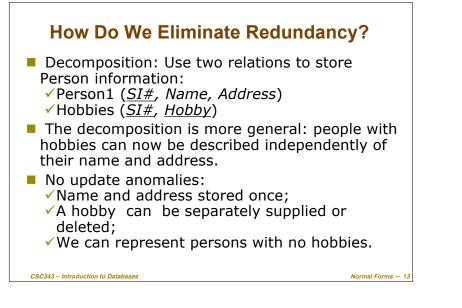
Looking for FDs	 Non-Trivial Dependencies A functional dependency x→z is non-trivial if no attribute in z appears among attributes of x, e.g.,
EmployeeSalaryProjectBudgetFunctionBrown20Mars2technicianGreen35Jupiter15designerGreen35Venus15designerHoskins55Venus15managerHoskins55Jupiter15consultantHoskins55Mars2consultantMoore48Mars2managerMoore48Venus15designerKemp48Venus15designerKemp48Jupiter15manager	 ✓ Employee → Salary is non-trivial; ✓ Employee, Project → Project is trivial. ■ Anomalies arise precisely for the attributes which are involved in (non-trivial) functional dependencies: ✓ Employee → Salary; ✓ Project → Budget. ■ Moreover, note that our example includes another functional dependency: ✓ Employee, Project → Function.
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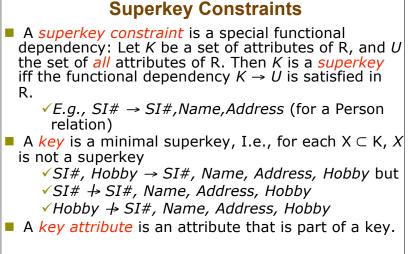
Dependencies Cause Anomalies, ...Sometimes!

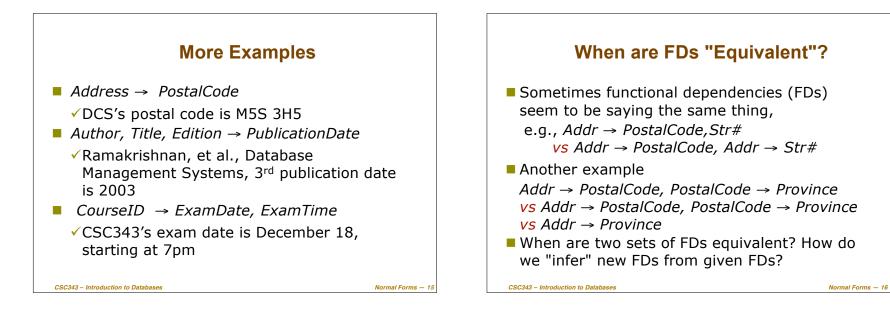
- The first two dependencies cause undesirable redundancies and anomalies.
- The third dependency, however, does not cause redundancies because {Employee, Project} constitutes a key of the relation (...and a relation cannot contain two tuples with the same values for the key attributes.)

Dependencies on keys are OK, other dependencies are not!

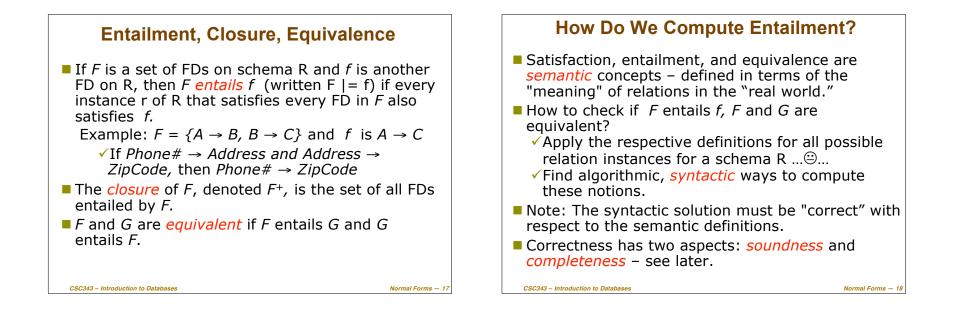








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Armstrong's Axioms for FDs

■ This is the syntactic way of computing/testing semantic properties of FDs \checkmark *Reflexivity*: $Y \subseteq X \mid -X \rightarrow Y$ (trivial FD) *e.g.*, \mid - *Name*, *Address* \rightarrow *Name* \checkmark *Augmentation*: $X \rightarrow Y \mid -XZ \rightarrow YZ$ *e.g.*, *Address* \rightarrow *ZipCode* \mid - *Address*, *Name* \rightarrow *ZipCode*, *Name* \checkmark *Transitivity*: $X \rightarrow Y$, $Y \rightarrow Z \mid -X \rightarrow Z$ *e.g.*, *Phone#* \rightarrow *Address*, *Address* \rightarrow *ZipCode* \mid - *Phone#* \rightarrow *ZipCode*

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Soundness

- Theorem: F |- f implies F |= f
- In words: If FD $f: X \rightarrow Y$ can be derived from a set of FDs *F* using the axioms, then *f* holds in every relation that satisfies every FD in *F*.
- **Example:** Given $X \rightarrow Y$ and $X \rightarrow Z$ then

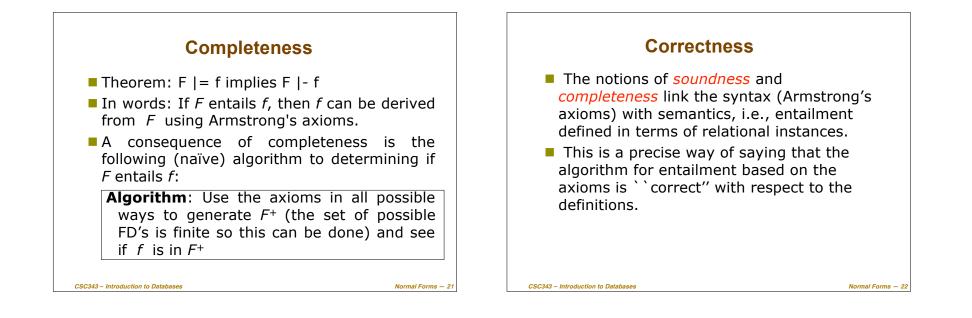
 $X \rightarrow XY$ Augmentation by X $YX \rightarrow YZ$ Augmentation by Y $X \rightarrow YZ$ Transitivity

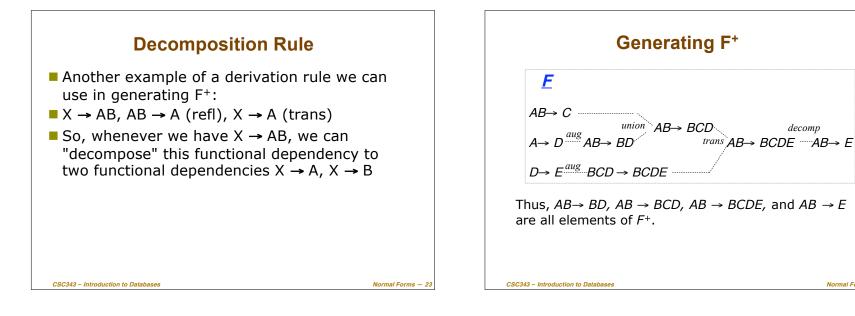
Thus, $X \rightarrow YZ$ is satisfied in every relation where both $X \rightarrow Y$ and $X \rightarrow Z$ are satisfied. We have derived the *union rule* for FDs.

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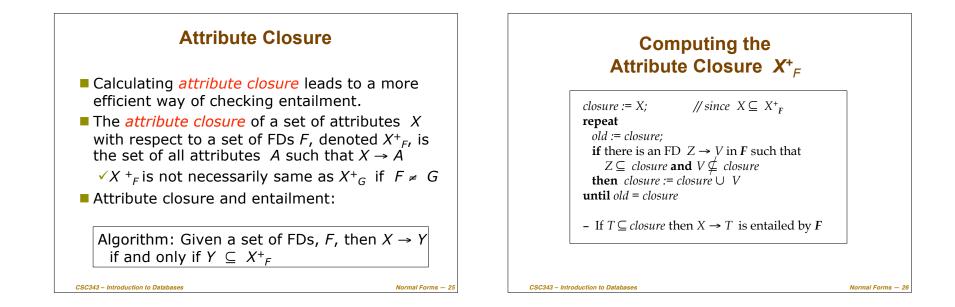
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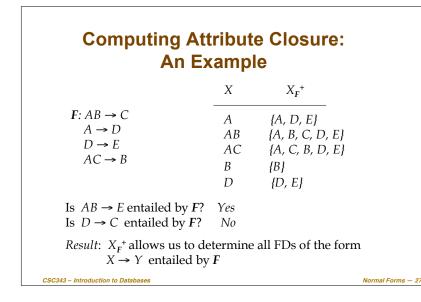
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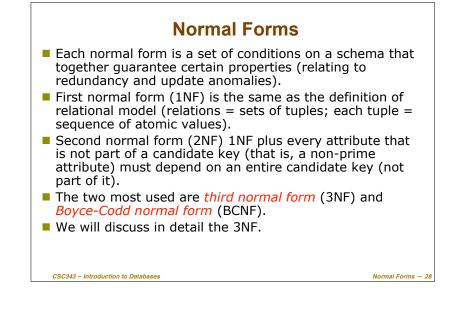


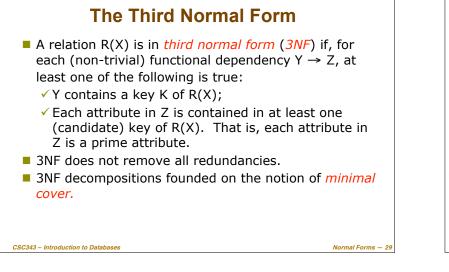


decomp





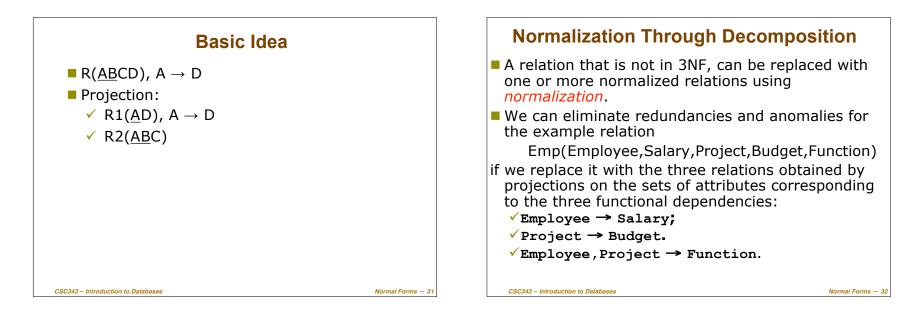




Decomposition into 3NF: Basic Idea

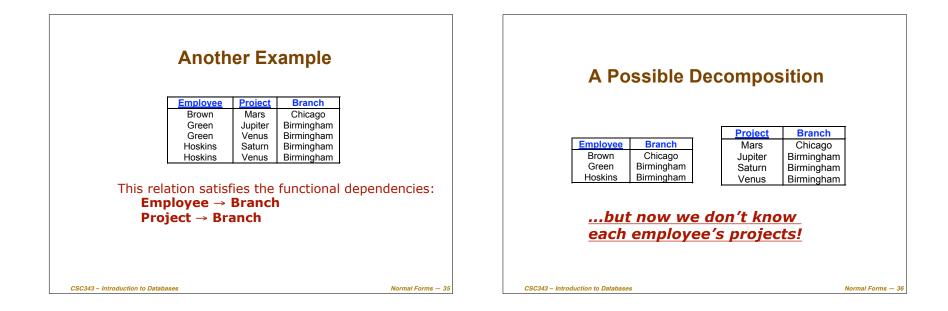
- Decomposition into 3NF can proceed as follows.
 - ✓ For each functional dependency of the form $Y \rightarrow Z$, where Y contains a subset of a key K of R(X), create a projection on all the attributes Y, Z (2NF).
 - ✓ For each dependency of the form $Y \rightarrow Z$, where Y, doesn't contain any key, and not all attributes of Z are key attributes, create a projection on all the attributes Y, Z (3NF).
- The new relations only include dependencies Y → Z, where Y contains a key K of R(X), or Z contains only key attributes.

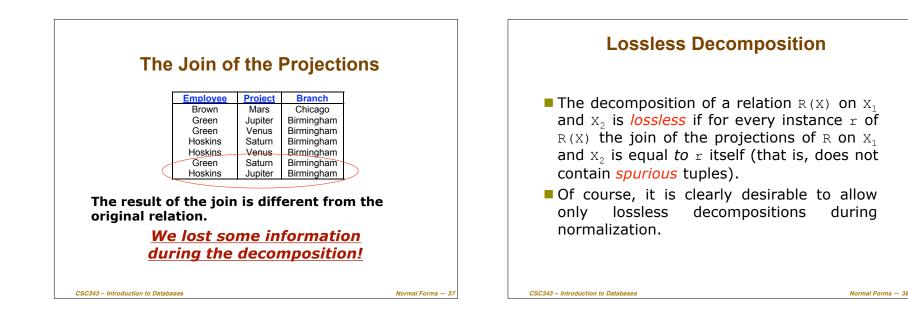
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Employee Brown	Salary	Project		
Brown	00	_	Budget	Function
0	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

Result of				No	ormaliza	tion	
	Em	ployee	Salary	Ī			
	B	Brown	20	1	Project	Budget	T
	-	Green	35		Mars	2	1
		oskins	55		Jupiter	15	
		loore	48		Venus	15	
	ŀ	Kemp	48	ļ			-
Employ	vee	Project	Funct	ion			
Brow	n	Mars	techni	cian	The key	rs of nei	w relations
Gree	n	Jupiter	desig	ner	are lefthand si functional dependent ant satisfaction of therefore guaran		sides of
Gree	n	Venus	desig	ner			
Hoski	ns	Venus	mana	ger			
Hoski	ns	Jupiter	consul	tant			f 3NF is
Hoski	ns	Mars	consul	tant			anteed for
Moor	е	Mars	mana	ger			
Moor	е	Venus	designer		the new relations.		ations.
Kem	р	Venus	desig	ner			
Kem	n	Jupiter	mana	aer			





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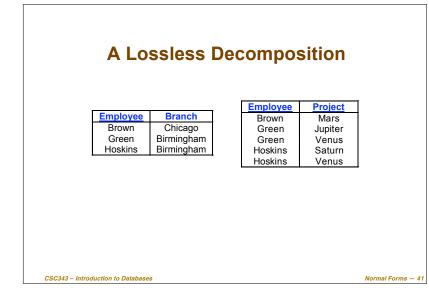
A Condition for Lossless Decomposition

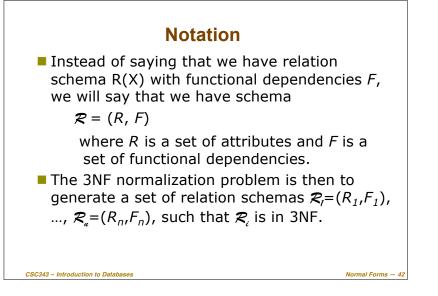
- Let R(X) be a relation schema and let X_1 and X_2 be two subsets of X such that $X_1 \cup X_2 = X$. Also, let $X_0 = X_1 \cap X_2$.
- If R(X) satisfies the functional dependency $X_0 \rightarrow X_1$ or $X_0 \rightarrow X_2$, then the decomposition of R(X) on X_1 and X_2 is lossless.
- In other words, R(X) has a lossless decomposition on two relations if the set of attributes common to the relations is a superkey for at least one of the decomposed relations.

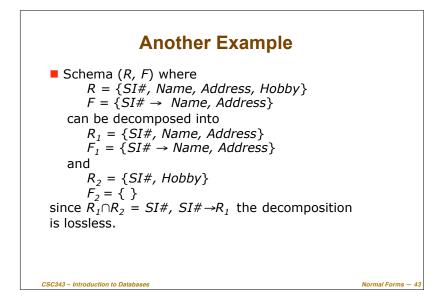
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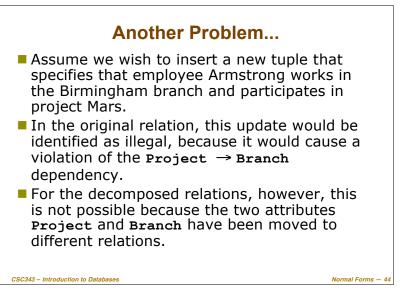
Intuition Behind the Test for Losslessness

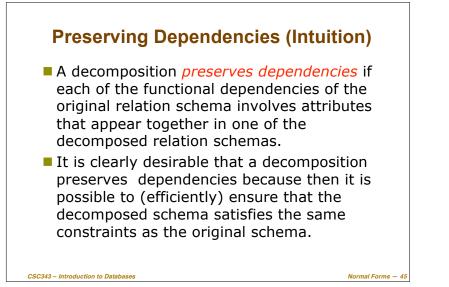
Suppose $R_1 \cap R_2 \rightarrow R_2$. Then a row of r_1 can combine with *exactly* one row of r_2 in the natural join (since in r_2 a particular set of values for the attributes in $R_1 \cap R_2$ defines a unique row) $R_1 \cap R_2 \xrightarrow{R_1 \cap R_2}$ $r_1 \xrightarrow{r_2}$



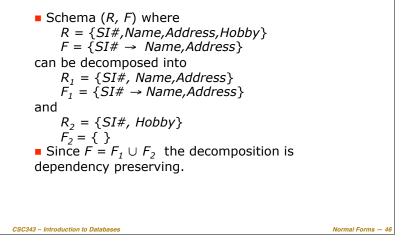


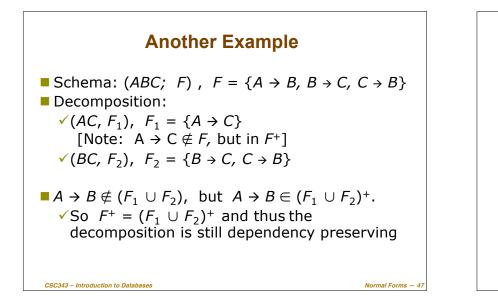


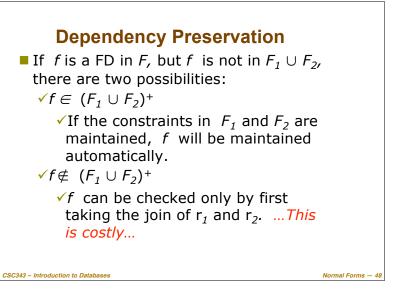




Example







Desirable Qualities for Decompositions

Decompositions should always satisfy the properties of lossless decomposition and dependency preservation:

- Lossless decomposition ensures that the information in the original relation can be accurately reconstructed based on the information represented in the decomposed relations.
- Dependency preservation ensures that the decomposed relations have the same capacity to represent the integrity constraints as the original relations and therefore to reveal illegal updates.

Minimal Cover

- A minimal cover for a set of dependencies F is a set of dependencies U such that:
 - ✓ *U* is equivalent to *F* (I.e., $F^+ = U^+$)
 - ✓ All FDs in *U* have the form $X \rightarrow A$ where *A* is a single attribute
 - ✓ It is not possible to make *U* smaller (while preserving equivalence) by
 - ✓Deleting an FD

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- ✓ Deleting an attribute from an FD (its LHS)
- FDs and attributes that can be deleted in this way are called *redundant*.

Computing the Minimal Cover

Example: $F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E\}$

- Step 1: Make RHS of each FD into a single attribute: Use decomposition rule for FDs.
 - ✓ Example: $L \rightarrow AD$ replaced by $L \rightarrow A$, $L \rightarrow D$; $ABH \rightarrow CK$ by $ABH \rightarrow C$, $ABH \rightarrow K$
- Step 2: Eliminate redundant attributes from LHS: If B is a single attribute and FD $XB \rightarrow A \in F$, $X \rightarrow A$ is entailed by F, then B is unnecessary.

e.g., Can an attribute be deleted from $ABH \rightarrow C$? Compute $AB_{F}^{+}AH_{F}^{+}BH_{F}^{+}$; Since $C \in (BH)_{F}^{+}$, $BH \rightarrow C$ is entailed by F and A is redundant in $ABH \rightarrow C$.

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Computing the Minimal Cover (cont'd)

Step 3: Delete redundant FDs from *F*: If $F - \{f\}$ entails *f*, then *f* is redundant; if *f* is $X \rightarrow A$ then check if $A \in X^+_{F^- \{f\}}$

e.g., $BGH \rightarrow L$ is entailed by $E \rightarrow L$, $BH \rightarrow E$, so it is redundant

Note: The order of steps 2, 3 can't be interchanged!! See textbook for a counterexample.

$$\begin{split} F_{1} &= \{ABH \rightarrow C, \, ABH \rightarrow K, \, A \rightarrow D, \, C \rightarrow E, \, BGH \rightarrow L, \, L \rightarrow A, \, L \rightarrow D, \, E \rightarrow L, \, BH \rightarrow E \} \\ F_{2} &= \{BH \rightarrow C, \, BH \rightarrow K, \, A \rightarrow D, \, C \rightarrow E, \, BH \rightarrow L, \, L \rightarrow A, \, L \rightarrow D, \, E \rightarrow L, \, BH \rightarrow E \} \\ F_{3} &= \{BH \rightarrow C, \, BH \rightarrow K, \, A \rightarrow D, \, C \rightarrow E, \, L \rightarrow A, \, E \rightarrow L \} \end{split}$$

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Starting with a schema R = (R, F): Step 1: Compute minimal cover U of F. The decomposition is based on U, but since $U^+ = F^+$ the same functional dependencies will hold. A minimal cover for $F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E\}$ is $U = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, L \rightarrow A, E \rightarrow L\}$



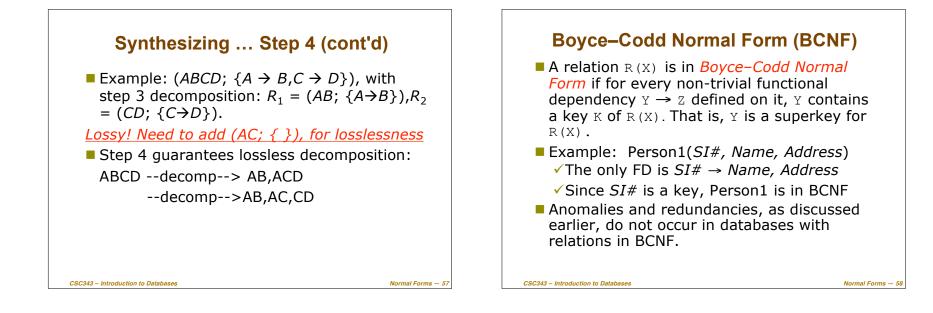
Step 2: Partition U into sets U_1 , U_2 , ... U_n such that the LHS of all elements of U_i are the same:

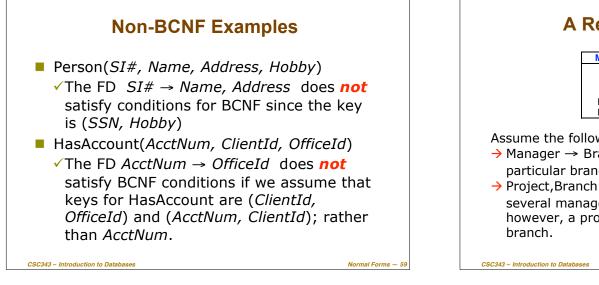
$$\checkmark U_1 = \{BH \rightarrow C, BH \rightarrow K\}, U_2 = \{A \rightarrow D\}, \\ U_2 = \{C \rightarrow E\}, U_4 = \{L \rightarrow A\}, U_5 = \{E \rightarrow L\}$$

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Step 3: For each U_i form schema R_i = (R_i, U_i), where R_i is the set of all attributes mentioned in U_i
Each FD of U will be in some R_i. Hence the decomposition is *dependency preserving*:
R₁ = (BHCK; BH→C, BH→K),
R₂ = (AD; A→D),
R₃ = (CE; C → E),
R₄ = (AL; L→A),
R₅ = (EL; E → L)

Step 4: If no R_i is a superkey of R, add schema R₀ = (R₀, {}) where R₀ is a key of R. R₀ = (BGH, {}); R₀ might be needed when not all attributes are contained in R₁∪R₂ ...∪R_n; A missing attribute A must be part of all keys (since it's not in any FD of U, deriving a key constraint from U involves the augmentation axiom); R₀ might be needed even if all attributes are accounted for in R₁∪R₂ ...∪R_n



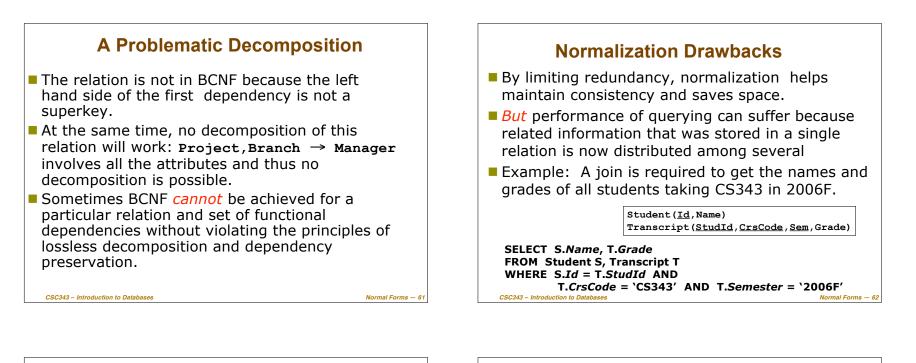


A Relation not in BCNF

Manager	Project	Branch
Brown	Mars	Chicago
Green	Jupiter	Birmingham
Green	Mars	Birmingham
Hoskins	Saturn	Birmingham
Hoskins	Venus	Birmingham

Assume the following dependencies:

- → Manager → Branch each manager works in a particular branch;
- → Project,Branch → Manager each project has several managers, and runs on several branches; however, a project has a unique manager for each branch.



Denormalization

- Tradeoff: Judiciously introduce redundancy to improve performance of certain queries
- Example: Add attribute *Name* to Transcript → Transcript'

SELECT T.*Name*, T.*Grade* FROM Transcript' T WHERE T.*CrsCode* = 'CS305' AND T.*Semester* = 'S2002'

✓ Join is avoided;

 If queries are asked more frequently than Transcript is modified, added redundancy might improve average performance;

✓ But, Transcript' is no longer in BCNF since key is (StudId,CrsCode,Semester) and StudId \rightarrow Name.

for the right hand side, which is part of the {Project,Branch} key.

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BCNF, but it is in 3NF.

The 3NF is less restrictive than the BCNF and for this reason does not offer the same guarantees of quality for a relation; it has the advantage however, of *always* being achievable.

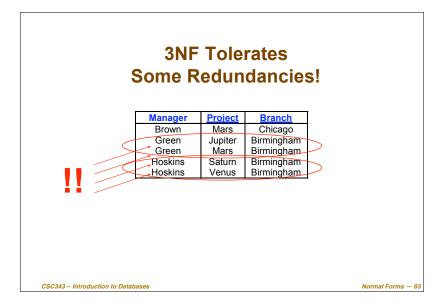
BCNF and 3NF

The Project-Branch-Manager schema is not in

In particular, the Project, Branch → Manager dependency has as its left hand side a key,

while Manager → Branch has a unique attribute

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A Revised Example

Manager	Project	Branch	Division
Brown	Mars	Chicago	1
Green	Jupiter	Birmingham	1
Green	Mars	Birmingham	1
Hoskins	Saturn	Birmingham	2
Hoskins	Venus	Birmingham	2

Functional dependencies:

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- Manager -> Branch, Division -- each manager works at one branch and manages one division;
- Branch, Division Manager -- for each branch and division there is a single manager;
- Project, Branch → Division, Manager -- for each branch, a project is allocated to a single division and has a sole manager responsible.

BCNF Normalization (Partial)

 \rightarrow Given: R = (R; F) where R = ABCDEGHK and $F = \{ABH \rightarrow C, A \rightarrow DE, BGH \rightarrow K, K \rightarrow ADH, BH \rightarrow GE\}$ ✓ Step 1: Find a FD that violates BCNF Note $ABH \rightarrow C$, $(ABH)^+$ includes all attributes (BH is a key) $A \rightarrow DE$ violates BCNF since A is not a superkey ($A^+ = ADE$) ✓ Step 2: Split R into: $R_1 = (ADE; F_1 = \{A \rightarrow DE\})$ Remove DE - A $\mathsf{R}_2 = (ABCGHK; F_1 = \{ABH \rightarrow C, BGH \rightarrow K, K \rightarrow AH, BH \rightarrow G\})$ \rightarrow Note 1: R₁ is in BCNF \rightarrow Note 2: Decomposition is lossless since A is a key of R₁. \rightarrow Note 3: FDs $K \rightarrow D$ and $BH \rightarrow E$ are not in F_1 or F_2 . But both can be derived from $F_1 \cup F_2$ (*E.g.*, $K \rightarrow A$ and $A \rightarrow D$ implies $K \rightarrow D$) Hence, decomposition is dependency preserving. CSC343 – Introduction to Databases Normal Forms - 67

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BCNF Decomposition Algorithm

Input: \mathbf{R} = (R; F)

Decomp := \mathbf{R}

while there is \mathbf{S} = (S; F') \in Decomp and \mathbf{S} not in BCNF do

Find X \rightarrow Y \in F' that violates BCNF // X isn't a superkey in \mathbf{S}

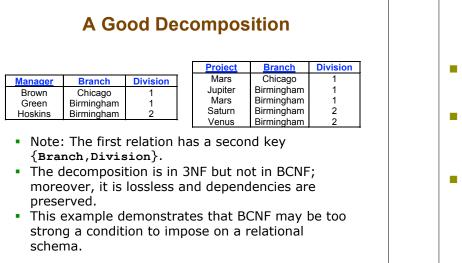
Replace \mathbf{S} in Decomp with \mathbf{S}_1 = (XY; F_1), \mathbf{S}_2 = (S - (Y - X); F_2)

// F_1 = all FDs of F' involving only attributes of XY

// F_2 = all FDs of F' involving only attributes of S - (Y - X)

end

return Decomp
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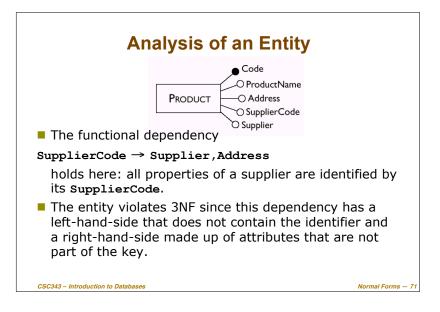
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Database Design and Normalization

- The theory of normalization can be used as a basis for quality control operations on schemas, during both conceptual and logical design.
- Analysis of the relations obtained during the logical design phase can identify places where the conceptual design was inaccurate: such a validation of the design is usually relatively easy.
- Normalization can also be used during conceptual design for quality control of each element of a conceptual schema (entity or relationship).

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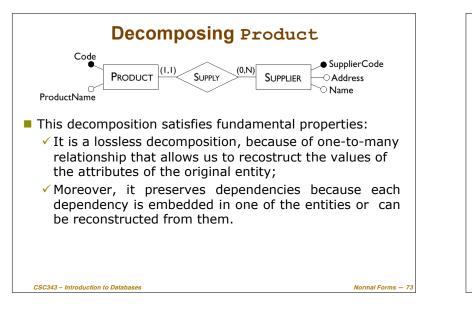


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Decomposing Product

- Supplier is (or should be) an independent entity, with its own attributes (code, surname and address)
- If Product and Supplier are distinct entities, they should be linked through a relationship.
- Since there is a functional dependency from Code to SupplierCode, we are sure that each product has at most one supplier (maximum cardinality 1).
- Since there is no dependency from SupplierCode to Code, we have an unrestricted maximum cardinality (N) for Supplier in the relationship.

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Analysis of a Relationship Now we show how to analyze n-ary relationships for $n \ge 3$, in order to determine whether they should be decomposed. Consider DEPARTMENT (0,N) (0.N)(0,1) PROFESSOR THESIS **S**TUDENT (0,N) Degree PROGRAMME

Some Functional Dependencies

- ✓ Student → DegreeProgramme (each student is enrolled in one degree programme)
- ✓ Student → Professor (each student writes a thesis under the supervision of a single professor)
- ✓ Professor → Department (each professor is associated with a single department and the students under her supervision are students in that department)

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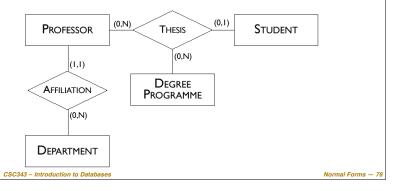
- The (unique) key of the relationship is Student (given a student, the degree programme, the professor and the department are identified uniquely)
- The third FD causes a violation of 3NF.

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Decomposing Thesis

The following is a decomposition of Thesis where the two decomposed relationships are both in 3NF(also in BCNF)

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More Observations...

- The relationship Thesis is in 3NF, because its key is made up of the Student entity, and its dependencies all have this entity on the left hand side.
- However, not all students write theses, therefore not all students have supervisors.
- From a normal form point of view, this is not a problem.
- However, our conceptual schema should reflect the fact that being in a degree programme and having a supervisor are independent facts.

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