

Database Design Database Redundancies and Anomalies Functional Dependencies Entailment, Closure and Equivalence Lossless Decompositions The Third Normal Form (3NF) The Boyce-Codd Normal Form (BCNF) Normal Forms and Database Design

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Normal Forms -



- We have seen how to design a relational schema by first designing an ER schema and then transforming it into a relational one.
- Now we focus on how to transform the generated relational schema into a "better" one.
- Goodness of relational schemas is defined in terms of the notion of *normal form*.

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Normal Forms and Normalization

- A *normal form* is a property of a database schema.
- When a database schema is un-normalized (that is, does not satisfy the normal form), it allows redundancies of various types which can lead to anomalies and inconsistencies.
- Normal forms can serve as basis for evaluating the quality of a database schema and constitutes a useful tool for database design.
- Normalization is a procedure that transforms an unnormalized schema into a normalized one.

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Normal Forms - 3

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Examples of Redundancy

Brown20Mars2technicGreen35Jupiter15designGreen35Venus15designHoskins55Venus15manage	cian ner
Green35Jupiter15designGreen35Venus15designHoskins55Venus15manage	ner
Green 35 Venus 15 design Hoskins 55 Venus 15 manag	
Hoskins 55 Venus 15 manag	ner
	ger
Hoskins 55 Jupiter 15 consul	tant
Hoskins 55 Mars 2 consul	tant
Moore 48 Mars 2 manag	ger
Moore 48 Venus 15 design	ner
Kemp 48 Venus 15 design	ner
Kemp 48 Jupiter 15 manag	ger

Anomalies

- The value of the salary of an employee is repeated in every tuple where the employee is mentioned, leading to a *redundancy*. Redundancies lead to anomalies:
- If salary of an employee changes, we have to modify the value in all corresponding tuples (update anomaly)
- If an employee ceases to work in projects, but stays with company, all corresponding tuples are deleted, leading to loss of information (*deletion anomaly*)
- A new employee cannot be inserted in the relation until the employee is assigned to a project (*insertion anomaly*)

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Normal Forms — 5

What's Wrong???

- We are using a single relation to represent data of very different types.
- In particular, we are using a single relation to store the following types of entities, relationships and attributes:
 - Employees and their salaries;
 - Projects and their budgets;

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- Participation of employees in projects, along with their functions.
- To set the problem on a formal footing, we introduce the notion of *functional dependency (FD)*.

Functional Dependencies (FDs) in the Example

- Each employee has a unique salary. We represent this dependency as
- Employee → Salary
 and say "Salary functionally depends on
 Employee".
- Meaning: if two tuples have the same Employee attribute value, they must also have the same Salary attribute value
- Likewise,
- $\texttt{Project} \rightarrow \texttt{Budget}$
 - i.e., each project has a unique budget

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Normal Forms —

Functional Dependencies

- Given schema R(X) and non-empty subsets Y and Z of the attributes X, we say that there is a *functional dependency* between Y and Z (Y→Z), iff for every relation instance r of R(X) and every pair of tuples t₁, t₂ of r, if t₁.Y = t₂.Y, then t₁.Z = t₂.Z.
- A functional dependency is a statement about all allowable relations for a given schema.
- Functional dependencies have to be identified by understanding the semantics of the application.

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Given a particular relation r₀ of R(X), we can tell if a dependency holds or not; but just because it holds for r₀, doesn't mean that it also holds for R(X)!

	Look	ing for	FDs	
Employee	Salary	Project	Budget	Function
Brown	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55)	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager
. <u> </u>	•	·	•	
Introduction to Database	25			N





The third dependency, however, does not cause redundancies because {Employee, Project} constitutes a key of the relation (...and a relation cannot contain two tuples with the same values for the key attributes.)

Dependencies on keys are OK, other dependencies are not!

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Superkey Constraints

A superkey constraint is a special functional dependency: Let K be a set of attributes of R, and U the set of all attributes of R. Then K is a superkey iff the functional dependency K → U is satisfied in R.

✓ E.g., $SI\# \rightarrow SI\#$, Name, Address (for a Person relation)

- A *key* is a minimal superkey, I.e., for each $X \subset K$, *X* is not a superkey
 - ✓SI#, Hobby → SI#, Name, Address, Hobby but ✓SI# → SI#, Name, Address, Hobby
 - ✓Hobby → SI#, Name, Address, Hobby
- A *key attribute* is an attribute that is part of a key.

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- Sometimes functional dependencies (FDs) seem to be saying the same thing, e.g., Addr → PostalCode, Str# vs Addr → PostalCode, Addr → Str#
 Another example Addr → PostalCode, PostalCode → Province vs Addr → PostalCode, PostalCode → Province vs Addr → Province
 When are two sets of FDs equivalent? How do
- When are two sets of FDs equivalent? How do we "infer" new FDs from given FDs?

Entailment, Closure, Equivalence

- If F is a set of FDs on schema R and f is another FD on R, then F entails f (written F |= f) if every instance r of R that satisfies every FD in F also satisfies f.
 - Example: $F = \{A \rightarrow B, B \rightarrow C\}$ and f is $A \rightarrow C$
 - ✓ If Phone# → Address and Address → ZipCode, then Phone# → ZipCode
- The closure of F, denoted F⁺, is the set of all FDs entailed by F.
- F and G are equivalent if F entails G and G entails F.

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Normal Forms – 17

How Do We Compute Entailment?

- Satisfaction, entailment, and equivalence are semantic concepts – defined in terms of the "meaning" of relations in the "real world."
- How to check if F entails f, F and G are equivalent?
 - ✓Apply the respective definitions for all possible relation instances for a schema R …☺…
 - Find algorithmic, syntactic ways to compute these notions.
- Note: The syntactic solution must be "correct" with respect to the semantic definitions.
- Correctness has two aspects: soundness and completeness see later.

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Armstrong's Axioms for FDs

■ This is the syntactic way of computing/testing semantic properties of FDs </pr

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Normal Forms — 19

Soundness

■ Theorem: F |- f implies F |= f

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- In words: If FD $f: X \rightarrow Y$ can be derived from a set of FDs *F* using the axioms, then *f* holds in every relation that satisfies every FD in *F*.
- **Example:** Given $X \rightarrow Y$ and $X \rightarrow Z$ then

 $X \rightarrow XY$ Augmentation by X $YX \rightarrow YZ$ Augmentation by Y $X \rightarrow YZ$ Transitivity

Thus, $X \rightarrow YZ$ is satisfied in every relation where both $X \rightarrow Y$ and $X \rightarrow Z$ are satisfied. We have derived the *union rule* for FDs.



- Theorem: F |= f implies F |- f
- In words: If F entails f, then f can be derived from F using Armstrong's axioms.
- A consequence of completeness is the following (naïve) algorithm to determining if F entails f:

Algorithm: Use the axioms in all possible ways to generate F^+ (the set of possible FD's is finite so this can be done) and see if f is in F^+

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Normal Forms - 21

Correctness

- The notions of soundness and completeness link the syntax (Armstrong's axioms) with semantics, i.e., entailment defined in terms of relational instances.
- This is a precise way of saying that the algorithm for entailment based on the axioms is ``correct" with respect to the definitions.

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Computing Att An Ex	ampl	e Closure: le	
	X	X_{F}^{+}	
$F: AB \to C$ $A \to D$ $D \to E$ $AC \to B$	A AB AC B D	{A, D, E} {A, B, C, D, E} {A, C, B, D, E} {B} {D, E}	
Is $AB \rightarrow E$ entailed by F ? Is $D \rightarrow C$ entailed by F ?	Yes No		
Result: X_F^+ allows us to de $X \rightarrow Y$ entailed by	etermine F	all FDs of the for	m

Each normal form is a set of conditions o	n a schema that
together guarantee certain properties (re redundancy and update anomalies).	lating to
First normal form (1NF) is the same as the relational model (relations = sets of tuple sequence of atomic values).	ne definition of es; each tuple =
Second normal form (2NF) 1NF plus ever is not part of a candidate key (that is, a attribute) must depend on an entire cand part of it).	y attribute that non-prime lidate key (not
The two most used are third normal form Boyce-Codd normal form (BCNF).	(3NF) and
We will discuss in detail the 3NF.	



- A relation R(X) is in *third normal form* (*3NF*) if, for each (non-trivial) functional dependency Y → Z, at least one of the following is true:
 - ✓ Y contains a key K of R(X);
 - ✓ Each attribute in Z is contained in at least one (candidate) key of R(X). That is, each attribute in Z is a prime attribute.
- 3NF does not remove all redundancies.
- 3NF decompositions founded on the notion of *minimal* cover.

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Normal Forms – 29

Decomposition into 3NF: Basic Idea

- Decomposition into 3NF can proceed as follows.
 - ✓ For each functional dependency of the form $Y \rightarrow Z$, where Y contains a subset of a key K of R(X), create a projection on all the attributes Y, Z (2NF).
 - ✓ For each dependency of the form $Y \rightarrow Z$, where Y, doesn't contain any key, and not all attributes of Z are key attributes, create a projection on all the attributes Y, Z (3NF).
- The new relations only include dependencies Y → Z, where Y contains a key K of R(X), or Z contains only key attributes.

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Employee	Salary	Project	Budget	Function
Brown	20	Mars	2	technician
Green	35	Juniter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

Result of Normalization

	En E H H	nployee Brown Green oskins Moore Kemp	Salary 20 35 55 48 48		Project Mars Jupiter Venus	Budget 2 15 15	I
	Employee Brown Green Hoskins Hoskins Hoskins Moore Moore Kemp Kemp	Project Mars Jupiter Venus Jupiter Mars Venus Venus Jupiter	Functi technic design design manag consult consult manag design design manag	on an er er er ant ant er er er er	The key are le functio satisfo therefo the	s of new athand nal depe action of re guard new rela	v relations sides of endencies; f 3NF is anteed for ations.
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Another Example	A Possible Decomposition
Employee Project Branch Brown Mars Chicago Green Jupiter Birmingham Green Venus Birmingham Hoskins Saturn Birmingham Hoskins Venus Birmingham Birmingham Birmingham Birmingham Birmingham Birmingham Birmingham Hoskins Venus Birmingham Birmingham Birmingham Birmingham Birmingham Birmingham <th>EmployeeBranchBrownChicagoGreenBirminghamHoskinsBirminghamSaturnBirminghamVenusBirminghamSirminghamSaturnBirminghamBirmingham</th>	EmployeeBranchBrownChicagoGreenBirminghamHoskinsBirminghamSaturnBirminghamVenusBirminghamSirminghamSaturnBirminghamBirmingham
CSC343 – Introduction to Databases Normal Forms – 35	CSC343 – Introduction to Databases Normal Forms – 3





Of course, it is clearly desirable to allow only lossless decompositions during normalization.

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A Condition for Lossless Decomposition

- Let R(X) be a relation schema and let X_1 and X_2 be two subsets of X such that $X_1 \cup X_2 = X$. Also, let $X_0 = X_1 \cap X_2$.
- If R(X) satisfies the functional dependency $X_0 \rightarrow X_1$ or $X_0 \rightarrow X_2$, then the decomposition of R(X) on X_1 and X_2 is lossless.
- In other words, R(X) has a lossless decomposition on two relations if the set of attributes common to the relations is a superkey for at least one of the decomposed relations.

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Normal Forms – 39

Intuition Behind the Test for Losslessness





Another Example

■ Schema (*R*, *F*) where $R = \{SI\#, Name, Address, Hobby\}$ $F = \{SI\# \rightarrow Name, Address\}$ can be decomposed into $R_1 = \{SI\#, Name, Address\}$ $F_1 = \{SI\# \rightarrow Name, Address\}$ and $R_2 = \{SI\#, Hobby\}$ $F_2 = \{\}$ since $R_1 \cap R_2 = SI\#$, $SI\# \rightarrow R_1$ the decomposition is lossless.

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- A decomposition preserves dependencies if each of the functional dependencies of the original relation schema involves attributes that appear together in one of the decomposed relation schemas.
- It is clearly desirable that a decomposition preserves dependencies because then it is possible to (efficiently) ensure that the decomposed schema satisfies the same constraints as the original schema.

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Normal Forms – 45

Example









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Desirable Qualities for Decompositions

Decompositions should always satisfy the properties of lossless decomposition and dependency preservation:

- Lossless decomposition ensures that the information in the original relation can be accurately reconstructed based on the information represented in the decomposed relations.
- Dependency preservation ensures that the decomposed relations have the same capacity to represent the integrity constraints as the original relations and therefore to reveal illegal updates.

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Computing the Minimal Cover

Example: $F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E,$

 $BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E$

- Step 1: Make RHS of each FD into a single attribute: Use decomposition rule for FDs.
 - ✓ Example: $L \rightarrow AD$ replaced by $L \rightarrow A$, $L \rightarrow D$; $ABH \rightarrow CK$ by $ABH \rightarrow C$, $ABH \rightarrow K$
- Step 2: Eliminate redundant attributes from LHS: If B is a single attribute and FD $XB \rightarrow A \in F$, $X \rightarrow A$ is entailed by F, then B is unnecessary.

e.g., Can an attribute be deleted from $ABH \rightarrow C$? Compute AB_{F}^{+} , AH_{F}^{+} , BH_{F}^{+} ; Since $C \in (BH)_{F}^{+}$, $BH \rightarrow C$ is entailed by F and A is redundant in $ABH \rightarrow C$.

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Normal Forms - 51

Computing the Minimal Cover (cont'd)

Step 3: Delete redundant FDs from *F*: If $F - \{f\}$ entails *f*, then *f* is redundant; if *f* is $X \rightarrow A$ then check if $A \in X^+_{F-\{f\}}$

e.g., $BGH \rightarrow L$ is entailed by $E \rightarrow L$, $BH \rightarrow E$, so it is redundant

Note: The order of steps 2, 3 can't be interchanged!! See textbook for a counterexample.

 $\begin{array}{l} F_1 = \{ABH \rightarrow C, \ ABH \rightarrow K, \ A \rightarrow D, \ C \rightarrow E, \ BGH \rightarrow L, \ L \rightarrow A, \ L \rightarrow D, \ E \rightarrow L, \ BH \rightarrow E \} \\ F_2 = \{BH \rightarrow C, \ BH \rightarrow K, \ A \rightarrow D, \ C \rightarrow E, \ BH \rightarrow L, \ L \rightarrow A, \ L \rightarrow D, \ E \rightarrow L, \ BH \rightarrow E \} \\ F_3 = \{BH \rightarrow C, \ BH \rightarrow K, \ A \rightarrow D, \ C \rightarrow E, \ L \rightarrow A, \ E \rightarrow L \} \end{array}$

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Starting with a schema R = (R, F):

Step 1: Compute minimal cover U of F. The decomposition is based on U, but since $U^+ = F^+$ the same functional dependencies will hold.

A minimal cover for

 $F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E\}$

IS

$$U = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, L \rightarrow A, E \rightarrow L\}$$

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- Step 4: If no R_i is a superkey of R, add schema R₀ = (R₀, {}) where R₀ is a key of R.
 ✓ R₀ = (BGH, {}); R₀ might be needed when not all attributes are contained in R₁∪R₂ ...∪ R_n;
 ✓ A missing attribute A must be part of all keys (since it's not in any FD of U, deriving a key constraint from U involves the augmentation axiom);
 - ✓ R_0 might be needed even if all attributes are accounted for in $R_1 \cup R_2 \dots \cup R_n$

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Boyce–Codd Normal Form (BCNF)

- A relation R(X) is in Boyce-Codd Normal Form if for every non-trivial functional dependency Y → Z defined on it, Y contains a key K of R(X). That is, Y is a superkey for R(X).
- - ✓ Since SI# is a key, Person1 is in BCNF
- Anomalies and redundancies, as discussed earlier, do not occur in databases with relations in BCNF.

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- Person(SI#, Name, Address, Hobby)
 ✓The FD SI# → Name, Address does not satisfy conditions for BCNF since the key is (SSN, Hobby)
- HasAccount(AcctNum, ClientId, OfficeId)
 - ✓The FD AcctNum → OfficeId does not satisfy BCNF conditions if we assume that keys for HasAccount are (ClientId, OfficeId) and (AcctNum, ClientId); rather than AcctNum.

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Normal Forms – 59

A Relation not in BCNF

Manager	Project	Branch
Brown	Mars	Chicago
Green	Jupiter	Birmingham
Green	Mars	Birmingham
Hoskins	Saturn	Birmingham
Hoskins	Venus	Birmingham

Assume the following dependencies:

- → Manager → Branch each manager works in a particular branch;
- → Project,Branch → Manager each project has several managers, and runs on several branches; however, a project has a unique manager for each branch.

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A Problematic Decomposition

- The relation is not in BCNF because the left hand side of the first dependency is not a superkey.
- At the same time, no decomposition of this relation will work: Project, Branch → Manager involves all the attributes and thus no decomposition is possible.
- Sometimes BCNF cannot be achieved for a particular relation and set of functional dependencies without violating the principles of lossless decomposition and dependency preservation.

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Normal Forms – 61

Normalization Drawbacks

- By limiting redundancy, normalization helps maintain consistency and saves space.
- But performance of querying can suffer because related information that was stored in a single relation is now distributed among several
- Example: A join is required to get the names and grades of all students taking CS343 in 2006F.

 Student(Id, Name)

 Transcript(StudId, CrsCode, Sem, Grade)

 SELECT S.Name, T.Grade

 FROM Student S, Transcript T

 WHERE S.Id = T.StudId AND

 T.CrsCode = `CS343' AND T.Semester = `2006F'

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Denormalization

- Tradeoff: Judiciously introduce redundancy to improve performance of certain queries
- Example: Add attribute *Name* to Transcript → Transcript'
 - SELECT T.*Name*, T.*Grade* FROM Transcript' T WHERE T.*CrsCode* = 'CS305' AND T.*Semester* = 'S2002' ✓ Join is avoided;
 - If queries are asked more frequently than Transcript is modified, added redundancy might
 - improve average performance;
 - ✓ But, Transcript' is no longer in BCNF since key is (StudId,CrsCode,Semester) and StudId \rightarrow Name.

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Normal Forms - 63

BCNF and **3NF**

- The Project-Branch-Manager schema is not in BCNF, but it <u>is</u> in 3NF.
- In particular, the Project, Branch → Manager dependency has as its left hand side a key, while Manager → Branch has a unique attribute for the right hand side, which is part of the {Project, Branch} key.
- The 3NF is less restrictive than the BCNF and for this reason does not offer the same guarantees of quality for a relation; it has the advantage however, of *always* being achievable.

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A Revised Example

<u>Manager</u>	Project	Branch	Division
Brown	Mars	Chicago	1
Green	Jupiter	Birmingham	1
Green	Mars	Birmingham	1
Hoskins	Saturn	Birmingham	2
Hoskins	Venus	Birmingham	2

Functional dependencies:

- Manager -> Branch, Division -- each manager works at one branch and manages one division;
- Project, Branch → Division, Manager -- for each branch, a project is allocated to a single division and has a sole manager responsible.

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BCNF Decomposition Algorithm

```
Input: \mathbf{R} = (R; F)
```

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```
Decomp := R

while there is \mathbf{S} = (S; \mathbf{F'}) \in Decomp and S not in BCNF do

Find X \rightarrow Y \in \mathbf{F'} that violates BCNF // X isn't a superkey in S

Replace S in Decomp with \mathbf{S_1} = (XY; \mathbf{F_1}), \mathbf{S_2} = (S - (Y - X); \mathbf{F_2})

// \mathbf{F_1} = all FDs of \mathbf{F'} involving only attributes of XY

// \mathbf{F_2} = all FDs of \mathbf{F'} involving only attributes of S - (Y - X)

end

return Decomp
```

A Good Decomposition

				Project	Branch	Division
Manager	Branch	Division	Ī	Mars	Chicago	1
Brown	Chicago	1	1	Jupiter	Birmingham	1
Green	Birmingham	1		Mars	Birmingham	1
Hoskins	Birmingham	2		Saturn	Birmingham	2
	· ·		•	Venus	Birmingham	2

- Note: The first relation has a second key {Branch,Division}.
- The decomposition is in 3NF but not in BCNF; moreover, it is lossless and dependencies are preserved.
- This example demonstrates that BCNF may be too strong a condition to impose on a relational schema.

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Normal Forms - 69

Database Design and Normalization

- The theory of normalization can be used as a basis for quality control operations on schemas, during both conceptual and logical design.
- Analysis of the relations obtained during the logical design phase can identify places where the conceptual design was inaccurate: such a validation of the design is usually relatively easy.
- Normalization can also be used during conceptual design for quality control of each element of a conceptual schema (entity or relationship).

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Some Functional Dependencies

- ✓ Student → DegreeProgramme (each student is enrolled in one degree programme)
- ✓ Student → Professor (each student writes a thesis under the supervision of a single professor)
- ✓ Professor → Department (each professor is associated with a single department and the students under her supervision are students in that department)
- The (unique) key of the relationship is Student (given a student, the degree programme, the professor and the department are identified uniquely)
- The third FD causes a violation of 3NF.

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Normal Forms - 75

Decomposing Thesis The following is a decomposition of Thesis where the two decomposed relationships are both in 3NF(also in BCNF) (0,1) (0,N) STUDENT PROFESSOR THESIS (0,N) (1,1) Degree **A**FFILIATION Programme (0,N) DEPARTMENT CSC343 – Introduction to Databases Normal Forms - 76

More Observations...

- The relationship Thesis is in 3NF, because its key is made up of the Student entity, and its dependencies all have this entity on the left hand side.
- However, not all students write theses, therefore not all students have supervisors.
- From a normal form point of view, this is not a problem.
- However, our conceptual schema should reflect the fact that being in a degree programme and having a supervisor are independent facts.

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Normal Forms — 77

Another Decomposition

(0,N)

Degree

Programe

(0,N)

DEPARTMENT

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39