Week 3 – Relational Algebra

Querying and Updating a Database
The Relational Algebra
Union, Intersection, Difference
Renaming, Selection and Projection
Join, Cartesian Product

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Relational Algebra - 1

Query Languages for Relational Databases

- →Operations on databases:
 - ✓ Queries read data from the database:
 - ✓ Updates change the content of the database.
- →In this lecture unit we discuss the relational algebra, a procedural language that defines database operations in terms of algebraic expressions.
- →[The Relational Calculus is a declarative language for database operations based on Predicate Logic; we will not discuss it here.]

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Relational Algebra — 2

Relational Algebra

- →A collection of algebraic operators that
 - ✓ Are defined on relations;
 - ✓ Produce relations as results, and therefore can be combined to form complex algebraic expressions.

Operators:

- ✓Union, intersection, difference;
- ✓ Renaming;
- ✓ Selection and Projection;
- ✓ Join (natural join, Cartesian product, theta join).

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Relational Algebra — 3

Union, Intersection, Difference

- → Relations are sets, so we can apply set-theoretic operators
- → However, we want the results to be relations (that is, homogeneous sets of tuples)
- →It is therefore meaningful to only apply union, intersection, difference to pairs of relations defined over the same attributes.

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Union

Graduates

| Number | Surname | Age |
|--------|----------|-----|
| 7274 | Robinson | 37 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

Managers

| managoro | | |
|----------|----------|-----|
| Number | Surname | Age |
| 9297 | O'Malley | 56 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

Graduates \cup **Managers**

| Number | Surname | Age |
|--------|----------|-----|
| 7274 | Robinson | 37 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |
| 9297 | O'Malley | 56 |

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Intersection

Graduates

| Number | Surname | Age |
|--------|----------|-----|
| 7274 | Robinson | 37 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

Managers

| Surname | Age |
|----------|----------------------|
| O'Malley | 56 |
| O'Malley | 39 |
| Darkes | 38 |
| | O'Malley O'Malley |

Graduates ∩ **Managers**

| Oradautos i imanagero | | |
|-----------------------|----------|-----|
| Number | Surname | Age |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

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Relational Algebra — 6

Difference

Graduates

| Number | Surname | Age |
|--------|----------|-----|
| 7274 | Robinson | 37 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

Managers

| Managers | | |
|----------|----------|-----|
| Number | Surname | Age |
| 9297 | O'Malley | 56 |
| 7432 | O'Malley | 39 |
| 9824 | Darkes | 38 |

Graduates - Managers

| Number | Surname | Age |
|--------|----------|-----|
| 7274 | Robinson | 37 |

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Relational Algebra — 7

A Meaningful but Impossible Union

Paternity

| aterinty | |
|----------|---------|
| Father | Child |
| Adam | Cain |
| Adam | Abel |
| Abraham | Isaac |
| Abraham | Ishmael |

Maternity

| Mother | Child |
|--------|---------|
| Eve | Cain |
| Eve | Seth |
| Sarah | Isaac |
| Hagar | Ishmael |

Paternity ∪ **Maternity** ???

- → The problem: **Father** and **Mother** are different names, but both represent a parent.
- →The solution: rename attributes!

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Renaming

- → This is a unary operator which changes attribute names for a relation without changing any values.
- → Renaming removes the limitations associated with set operators.
- → Notation: ρ_{OldName→NewName}(r)
- \rightarrow For example, $\rho_{\text{Father} \rightarrow \text{Parent}}$ (Paternity)
- →If there are two or more attributes involved in a renaming operation, then ordering is meaningful:

e.g., $\rho_{Branch,Salary \rightarrow Location,Pay}$ (Employees)

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Relational Algebra - 9

Example of Renaming

Paternity

| Father | Child |
|---------|---------|
| Adam | Cain |
| Adam | Abel |
| Abraham | Isaac |
| Abraham | Ishmael |

ρ_{Father-> Parent}(Paternity)

| r rather / rarent | |
|-------------------|---------|
| Parent | Child |
| Adam | Cain |
| Adam | Abel |
| Abraham | Isaac |
| Abraham | Ishmael |

- The textbook allows positions rather than attribute names, e.g., 1 → Parent
- Textbook also allows renaming of the relation itself,e.g.,Paternity,1→ Parenthood,Parent

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Relational Algebra — 10

Renaming and Union

Paternity

| Father | Child | |
|---------|---------|--|
| Adam | Cain | |
| Adam | Abel | |
| Abraham | Isaac | |
| Abraham | Ishmael | |

Maternity

| Mother | Child |
|--------|---------|
| Eve | Cain |
| Eve | Seth |
| Sarah | Isaac |
| Hagar | Ishmael |

$\rho_{Father-Parent}(Paternity) \cup \rho_{Mother-Parent}(Maternity)$

| l | (1 atomicy) o pwotner-sparent | | | |
|---|-------------------------------|---------|--|--|
| | Parent | Child | | |
| | Adam | Cain | | |
| | Adam | Abel | | |
| | Abraham | Isaac | | |
| | Abraham | Ishmael | | |
| | Eve | Cain | | |
| | Eve | Seth | | |
| | Sarah | Isaac | | |
| | Hagar | Ishmael | | |

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Relational Algebra — 11

Renaming and Union, with Several Attributes

Employees

| Surname | Branch | Salary |
|-----------|--------|--------|
| Patterson | Rome | 45 |
| Trumble | London | 53 |

Staff

| Surname | Factory | Wages |
|-----------|---------|-------|
| Patterson | Rome | 45 |
| Trumble | London | 53 |

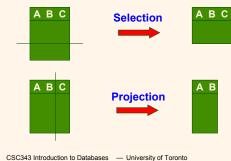
 $\rho_{Branch,Salary
ightarrow Location,Pav}$ (Employees) $\cup \rho_{Factory, Wages
ightarrow Location,Pav}$ (Staff)

| Surname | Location | Pay | |
|-----------|----------|-----|--|
| Patterson | Rome | 45 | |
| Trumble | London | 53 | |
| Cooke | Chicago | 33 | |
| Bush | Monza | 32 | |

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Selection and Projection

- →These are unary operators, in a sense orthogonal:
 - ✓ selection for "horizontal" decompositions;
 - ✓ projection for "vertical" decompositions.



Relational Algebra — 13

Selection

- →This is a unary operation which returns a relation
 - ✓ with the same schema as the operand;
 - ✓ but, with a **subset of the tuples** of the operand, i.e., only those that satisfy a condition.
- \rightarrow Notation: $\sigma_{F}(\mathbf{r})$
- \rightarrow Semantics: $\sigma_F(r) = \{t \mid t \in r \text{ s.t. } t \text{ satisfies } F, \text{ l.e., } F(t)\}$

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Relational Algebra — 14

Selection Example

Employees

| Surname | FirstName | Age | Salary |
|---------|-----------|-----|--------|
| Smith | Mary | 25 | 2000 |
| Black | Lucy | 40 | 3000 |
| Verdi | Nico | 36 | 4500 |
| Smith | Mark | 40 | 3900 |

σ Age<30 v Salary>4000 (Employees)

| Surname | FirstName | Age | Salary |
|---------|-----------|-----|--------|
| Smith | Mary | 25 | 2000 |
| Verdi | Nico | 36 | 4500 |

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Selection, Another Example

Citizens

| Surname | FirstName | PlaceOfBirth | Residence |
|---------|-----------|--------------|-----------|
| Smith | Mary | Rome | Milan |
| Black | Lucy | Rome | Rome |
| Verdi | Nico | Florence | Florence |
| Smith | Mark | Naples | Florence |

σ_{PlaceOfBirth=Residence} (Citizens)

| I | Surname | FirstName | PlaceOfBirth | Residence |
|---|---------|-----------|--------------|-----------|
| | Black | Lucy | Rome | Rome |
| | Verdi | Nico | Florence | Florence |

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Projection

- → Projection returns a relation which includes a **subset of the attributes** of the operand.
- → Notation: Given a relation r(X) and a subset Y of X: $\pi_Y(r)$
- →Semantics: $\pi_Y(r) = \{ t[Y] \mid t \in r \}$

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Relational Algebra — 17

Example of Projection

Employees

| Surname | FirstName | Department | Head |
|---------|-----------|------------|----------|
| Smith | Mary | Sales | De Rossi |
| Black | Lucy | Sales | De Rossi |
| Verdi | Mary | Personnel | Fox |
| Smith | Mark | Personnel | Fox |

 $\pi_{Surname, FirstName}$ (Employees)

| Surname | FirstName |
|---------|-----------|
| Smith | Mary |
| Black | Lucy |
| Verdi | Mary |
| Smith | Mark |

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Relational Algebra — 18

Another Example

Employees

| Surname First | | FirstName | Department | Head |
|---------------|-------|-----------|------------|----------|
| Smith Mary | | Mary | Sales | De Rossi |
| | Black | Lucy | Sales | De Rossi |
| Verdi Mary | | Personnel | Fox | |
| | Smith | Mark | Personnel | Fox |

$\pi_{\text{Dep}\underline{\text{artment}}, \text{ Head}}$ (Employees)

| Department | Head |
|------------|----------|
| Sales | De Rossi |
| Personnel | Fox |

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Cardinality of Projection Operations

- →Note that the result of a projection contains at most as many tuples as the operand relation.
- → However, it may contain fewer, if several tuples collapse, i.e., they are identical in all their values.
- → Theorem: $\pi_Y(r)$ contains as many tuples as r if and only if Y is a superkey for r.
- → This property holds even if Y is "by chance" a superkey, i.e., it is not defined as a superkey in the schema, but it is a superkey for the current database, see the example.

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Tuples that Collapse

Students

| RegNum Surname | | FirstName | BirthDate | DegreeProg |
|----------------|-------|-----------|-----------|-------------|
| 284328 Smith | | Luigi | 29/04/59 | Computing |
| 296328 | Smith | John | 29/04/59 | Computing |
| 587614 | Smith | Lucy | 01/05/61 | Engineering |
| 934856 | Black | Lucy | 01/05/61 | Fine Art |
| 965536 | Black | Lucy | 05/03/58 | Fine Art |

π_{Surname, DegreeProg} (Students)

| Surname | DegreeProg |
|---------|-------------|
| Smith | Computing |
| Smith | Engineering |
| Black | Fine Art |

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Tuples that do not Collapse, "by Chance"

Students

| RegNum | RegNum Surname | | BirthDate | DegreeProg |
|--------|----------------|------|-----------|-------------|
| 296328 | Smith | John | 29/04/59 | Computing |
| 587614 | Smith | Lucy | 01/05/61 | Engineering |
| 934856 | Black | Lucy | 01/05/61 | Fine Art |
| 965536 | Black | Lucy | 05/03/58 | Engineering |

$\pi_{\text{Surname, DegreeProg}} \left(\text{Students} \right)$

| Surname | DegreeProg |
|---------|-------------|
| Smith | Computing |
| Smith | Engineering |
| Black | Fine Art |
| Black | Engineering |
| | |

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Join

- →The most used operator in the relational algebra.
- → Allows us to establish connections among data in different relations, taking advantage of the "value-based" nature of the relational model.
- →Two main versions of the join:
 - ✓"natural" join: takes attribute names into account;
 ✓"theta" join.
- →Both join operations are denoted by the symbol ⋈.

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Relational Algebra — 23

A Natural Join

11

| Employee | Department |
|-----------------|------------|
| Smith | sales |
| Black | production |
| White | production |

r

| <u>Department</u> | Head |
|-------------------|-------|
| production | Mori |
| sales | Brown |
| | |

$r_1 \bowtie r_2$

| Employee | Department | Head | |
|----------|------------|-------|--|
| Smith | sales | Brown | |
| Black | production | Mori | |
| White | production | Mori | |

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Definition of Natural Join

$$\rightarrow$$
 r₁ (X₁), r₂ (X₂)

 \rightarrow r₁ \bowtie r₂ (natural join of r₁ and r₂) is a relation on X₁X₂ (the union of the two sets):

$$\{ t \text{ on } X_1 X_2 \mid t [X_1] \in r_1 \text{ and } t [X_2] \in r_2 \}$$

or, equivalently

{ t on X_1X_2 | exist $t_1 \in r_1$ and $t_2 \in r_2$ with t $[X_1] = t_1$ and t $[X_2] = t_2$ }

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Relational Algebra — 25

Natural Join: Comments

- →The tuples in the resulting relation are obtained by combining tuples in the operands with equal values on the common attributes
- → The common attributes often form a key of one of the operands (remember: references are realized by means of foreign keys, and we join in order to follow references)
- * Not always! Consider Person(Name,Addr,PostalC) and let us define Neighbour(Name,Addr,Name1,Addr1,PostalC) by joining Person with ρ_{Name,Addr→Name1,Addr1}(Person); What is criterion for neighbourhood here?

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Another Example

Offences

| , | Code | Date | Officer | Dept | Registartion |
|---|--------|------------|---------|------|--------------|
| | 143256 | 25/10/1992 | 567 | 75 | 5694 FR |
| | 987554 | 26/10/1992 | 456 | 75 | 5694 FR |
| | 987557 | 26/10/1992 | 456 | 75 | 6544 XY |
| | 630876 | 15/10/1992 | 456 | 47 | 6544 XY |
| | 539856 | 12/10/1992 | 567 | 47 | 6544 XY |

Cars

| Registration | | Dept | Owner | |
|--------------|---------|------|-----------------|--|
| | 6544 XY | 75 | Cordon Edouard | |
| | 7122 HT | 75 | Cordon Edouard | |
| | 5694 FR | 75 | Latour Hortense | |
| | 6544 XY | 47 | Mimault Bernard | |

Offences M Cars

| Code | Date | Officer | Dept | Registration | Owner | |
|--------|------------|---------|------|--------------|-----------------|--|
| 143256 | 25/10/1992 | 567 | 75 | 5694 FR | Latour Hortense | |
| 987554 | 26/10/1992 | 456 | 75 | 5694 FR | Latour Hortense | |
| 987557 | 26/10/1992 | 456 | 75 | 6544 XY | Cordon Edouard | |
| 630876 | 15/10/1992 | 456 | 47 | 6544 XY | Cordon Edouard | |
| 539856 | 12/10/1992 | 567 | 47 | 6544 XY | Mimault Bernard | |

Relational Algebra — 27

Yet Another Join

→In this example, join gives very different results from union (see earlier example)

Paternity

| | <u>i aterini</u> | · y | |
|--|------------------|------------|--|
| | Father | Child | |
| | Adam | Cain | |
| | Adam | Abel | |
| | Abraham | Isaac | |
| | Abraham | Ishmael | |

Maternity

| Mother | Child | |
|--------|---------|--|
| Eve | Cain | |
| Eve | Seth | |
| Sarah | Isaac | |
| Hagar | Ishmael | |

Paternity ⋈ Maternity

| | , , , | |
|---------|--------------|--------|
| Father | Child | Mother |
| Adam | Cain | Eve |
| Abraham | Isaac | Sarah |
| Abraham | Ishmael | Hagar |

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Joins can be Incomplete

→ If a tuple does not have a "counterpart" in the other relation, then it does not contribute to the join ("dangling" tuple)

r₁

Employee Department
Smith sales
Black production
White production

| | '2 | |
|--|------------|-------|
| | Department | Head |
| | production | Mori |
| | purchasing | Brown |
| | | |

 $\mathbf{r_1} \bowtie \mathbf{r_2}$

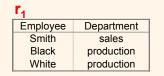
| Employee | Department | Head |
|----------|------------|------|
| Black | production | Mori |
| White | production | Mori |

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Relational Algebra - 29

Joins can be Empty

→ As an extreme, we might have that no tuple has a counterpart, and all tuples are dangling



| 12 | | | | |
|------------|-------|--|--|--|
| Department | Head | | | |
| marketing | Mori | | | |
| purchasing | Brown | | | |
| | | | | |

| $\mathbf{r_1} \bowtie \mathbf{r_2}$ | | |
|-------------------------------------|------------|------|
| Employee | Department | Head |
| | | |

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Relational Algebra - 30

Another Extreme

→If each tuple of each operand can be combined with all the tuples of the other, then the join has a cardinality that is the product of the cardinalities of the operands

| r ₁ | | | | |
|----------------|---------|--|--|--|
| Employee | Project | | | |
| Smith | Α | | | |
| Black | Α | | | |
| White | Α | | | |

| r ₂ | | | | |
|----------------|-------|--|--|--|
| Project | Head | | | |
| Α | Mori | | | |
| Α | Brown | | | |
| | | | | |

| $\mathbf{r_1} \bowtie \mathbf{r_2}$ |
|-------------------------------------|
| Employe |
| Smith |

| Employee | Project | Head |
|----------|---------|-------|
| Smith | Α | Mori |
| Black | Α | Brown |
| White | Α | Mori |
| Smith | Α | Brown |
| Black | Α | Mori |
| White | Α | Brown |

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Relational Algebra — 31

How Many Tuples in a Join?

→Given $r_1(X_1)$, $r_2(X_2)$ the join has cardinality $0 \le |r_1 \bowtie r_2| \le |r_1| \times |r_2|$

where | r | is the cardinality of relation r.

→Moreover:

✓ if the join is complete, then its cardinality is at least the maximum of $|r_1|$ and $|r_2|$.

 \checkmark if $X_1 \cap X_2$ contains a key for r_2 ,

then
$$| r_1 \bowtie r_2 | \le | r_1 |$$

✓ if $X_1 \cap X_2$ is the primary key for r_2 , and there is a referential constraint between $X_1 \cap X_2$ in r_1 and such a key, then $|r_1 \bowtie r_2| = |r_4|$.

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Outer Join

- → A variant of the join, to keep all pieces of information from the operands.
- →An outer join operation "pads with nulls" the tuples in one operant relation that have no counterpart in the other relation.
- →Three variants:
 - ✓ LEFT only tuples of left operand are padded;
 - √RIGHT only tuples of right operand are padded;
 - √FULL tuples of both operands are padded.

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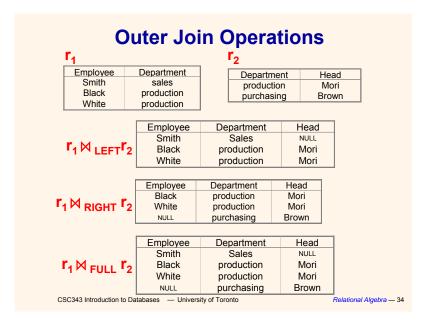
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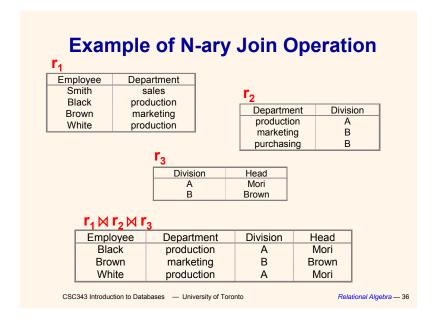
N-ary Join Operations

- →The natural join is
 - ✓ commutative: $r_1 \bowtie r_2 = r_2 \bowtie r_1$
 - ✓ associative: $(r_1 \bowtie r_2) \bowtie r_3 = r_1 \bowtie (r_2 \bowtie r_3)$
- →Therefore, we can write n-ary joins without ambiguity:

$$r_1 \bowtie r_2 \bowtie ... \bowtie r_n$$

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Join and Intersection

- →We have made no assumptions about the sets of attributes X₁ and X₂ on which the operands of a join operation are defined; the two sets could even be equal or disjoint.
- →If $X_1 = X_2$ then $r_1 \bowtie r_2 = r_1 \cap r_2$ since, by definition, the result is a relation which includes tuples t such that $t[X_1] \in r_1$ and $t[X_2] \in r_2$, and $X_1 = X_2$.

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Relational Algebra - 37

Natural Join as Cartesian Product

- →The natural join is defined also when the operands have no attributes in common.
- →In this case no condition is imposed on tuples, and therefore the result contains tuples obtained by combining the tuples of the operands in all possible ways.

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Relational Algebra — 38

Cartesian Product: Example

Employees

| Α |
|---|
| Α |
| В |
| |

Projects

| Code | Name |
|------|-------|
| Α | Venus |
| В | Mars |
| | |

Employes ⋈ **Projects**

| | , · | | |
|----------|---------|------|-------|
| Employee | Project | Code | Name |
| Smith | Α | Α | Venus |
| Black | Α | Α | Venus |
| Black | В | Α | Venus |
| Smith | Α | В | Mars |
| Black | Α | В | Mars |
| Black | В | В | Mars |

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Relational Algebra — 39

Theta-Join

→In most cases, a Cartesian product is meaningful only if followed by a selection:

√theta-join: a derived operator

$$r_1 \bowtie_F r_2 = \sigma_F(r_1 \bowtie r_2)$$

✓ if F is a conjunction of equalities, then we have an equi-join

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Equi-join: example

Employees

| Employee | Project |
|----------|---------|
| Smith | Α |
| Black | Α |
| Black | В |

Projects

| Code | Name |
|------|-------|
| Α | Venus |
| В | Mars |
| В | Mars |

Employes ⋈ Projects Projects

| Employee | Project | Code | Name |
|----------|---------|------|-------|
| Smith | Α | Α | Venus |
| Black | Α | Α | Venus |
| Black | В | В | Mars |

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Division

 \rightarrow Consider two relations A(x,y), B(y) and suppose we want to specify the query

"Find all A's that are associated with all B's"

→This can be expressed as

$$A/B = \pi_x(A) - \pi_x((\pi_x(A) \bowtie B) - A)$$

→This means that division does not extend the expressiveness of Relational Algebra, but it is a convenient operation to use in many situations.

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Example of Division

- →Assume
 - √ Take(x,y) "student x has taken course y",
 - √CS(y) "y is a CS course"
- →We want "All students who have taken all CS courses"
 - $\checkmark \pi_x(Take) \bowtie CS -- ? Table of all students, CS$
 - \checkmark (π_x (Take) ⋈ CS) Take -- ?? Table of all
 - $\checkmark \pi_x((\pi_x(Take) \bowtie CS) Take) -- ???$ CSC343 Introduction to Databases -- University of Toronto

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Queries

- →A query is a function from database instances to relations.
- →Queries are formulated in relational algebra by means of expressions over relations.

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A Sample Database

Employees

| Lilipioyees | | | |
|-------------|--------------|-----|--------|
| Number | Name | Age | Salary |
| 101 | Mary Smith | 34 | 40 |
| 103 | Mary Bianchi | 23 | 35 |
| 104 | Luigi Neri | 38 | 61 |
| 105 | Nico Bini | 44 | 38 |
| 210 | Marco Celli | 49 | 60 |
| 231 | Siro Bisi | 50 | 60 |
| 252 | Nico Bini | 44 | 70 |
| 301 | Steve Smith | 34 | 70 |
| 375 | Mary Smith | 50 | 65 |
| | | | |

Supervision

| Head | Employee |
|------|----------|
| 210 | 101 |
| 210 | 103 |
| 210 | 104 |
| 231 | 105 |
| 301 | 210 |
| 301 | 231 |
| 375 | 252 |
| | |

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Relational Algebra — 45

Example 1

"Find the numbers, names and ages of employees earning more than 40k."

Employees(<u>Number</u>,Name,Age,Salary) Supervision(Head,<u>Emp</u>)

Try it!

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Relational Algebra — 46

Example 2

→ "Find the registration numbers of the supervisors of the employees earning more than 40M."

Employees(<u>Number</u>,Name,Age,Salary) Supervision(Head,<u>Emp</u>)

Try it!

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Relational Algebra — 47

Example 3

→ "Find the names and salaries of the supervisors of the employees earning more than 40M."

Employees(<u>Number</u>,Name,Age,Salary) Supervision(Head,<u>Emp</u>)

Try it! (this is a bit tougher)

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Example 4

→ "Find the employees earning more than their respective supervisors, return registration numbers, names and salaries of the employees and their supervisors."

Employees(<u>Number</u>,Name,Age,Salary) Supervision(Head,<u>Emp</u>)

Try it! Definitely challenging ©

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Relational Algebra — 49

Example 5

→ "Find registration numbers and names of supervisors, *all* of whose employees earn more than 40M."

Employees(<u>Number</u>, Name, Age, Salary) Supervision(Head, Emp)

Try it!

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Relational Algebra — 50

Another Series of Examples:

 $Films(\underline{Film\#}, Title, Director, Year, ProdCost)$

Artists(<u>Actor#</u>,Surname,FirsName,Sex,Birthday, Nationality)

Roles(Film#,Actor#,Character)

→ Find "The titles of films starring Henry Fonda

Try it!

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Relational Algebra — 51

Example 2

Films(Film#, Title, Director, Year, ProdCost)

Artists(<u>Actor#</u>,Surname,FirsName,Sex,Birthday, Nationality)

Roles(Film#, Actor#, Character)

→ Find "The titles of all films in which the director is also an actor"

Try it!

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Example 3

Films(Film#, Title, Director, Year, ProdCost)

Artists(<u>Actor#</u>,Surname,FirsName,Sex,Birthday, Nationality)

Roles(Film#, Actor#, Character)

→ Find "The actors who have played two characters in the same film; show the title of each such film, first name and surname of the actor and the two characters"

Try it!

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Relational Algebra — 53

Example 4

Films(Film#, Title, Director, Year, ProdCost)

Artists(<u>Actor#</u>,Surname,FirsName,Sex,Birthday, Nationality)

Roles(Film#, Actor#, Character)

→ "The titles of the films in which the actors are all of the same sex"

Try it!

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Relational Algebra - 54

Relational Algebra and Null Values

People

| Name | Age | Salary |
|--------|------|--------|
| Aldo | 35 | 15 |
| Andrea | 27 | 21 |
| Maria | NULL | 42 |

- \rightarrow Consider $\sigma_{Age>30}$ (People)
- →Which tuples belong to the result?
- →The first yes, the second no, but the third??

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Relational Algebra — 55

Lecture Example (for blackboard)

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