#### **Week 12: Normal Forms**

Database Design
Database Redundancies and Anomalies
Functional Dependencies
Entailment, Closure and Equivalence
Lossless Decompositions
The Third Normal Form (3NF)
The Boyce-Codd Normal Form (BCNF)
Normal Forms and Database Design



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Normal Forms — 1

# **Logical Database Design**

- We have seen how to design a relational schema by first designing an ER schema and then transforming it into a relational one.
- Now we focus on how to transform the generated relational schema into a "better" one.
- Goodness of relational schemas is defined in terms of the notion of normal form.

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#### **Normal Forms and Normalization**

- A *normal form* is a property of a database schema.
- When a database schema is un-normalized (that is, does not satisfy the normal form), it allows redundancies of various types which can lead to anomalies and inconsistencies.
- Normal forms can serve as basis for evaluating the quality of a database schema and constitutes a useful tool for database design.
- Normalization is a procedure that transforms an un-normalized schema into a normalized one.

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Normal Forms — 3

# **Examples of Redundancy**

<b>Employee</b>	Salary	<u>Project</u>	Budget	Function
Brown	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

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#### **Anomalies**

The value of the salary of an employee is repeated in every tuple where the employee is mentioned, leading to a *redundancy*. Redundancies lead to anomalies:

- If salary of an employee changes, we have to modify the value in all corresponding tuples (update anomaly.)
- If an employee ceases to work in projects, but stays with company, all corresponding tuples are deleted, leading to loss of information (*deletion anomaly*.)
- A new employee cannot be inserted in the relation until the employee is assigned to a project (insertion anomaly.)

  Normal Forms 5

# What's Wrong???

- We are using a single relation to represent data of very different types.
- In particular, we are using a single relation to store the following types of entities, relationships and attributes:
  - ✓ Employees and their salaries;
  - ✓ Projects and their budgets;
  - ✓ Participation of employees in projects, along with their functions.
- To set the problem on a formal footing, we introduce the notion of *functional* dependency (FD).

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# Functional Dependencies (FDs) in the Example

■ Each employee has a unique salary. We represent this dependency as

- This means that everywhere we have the same Employee attribute value, we also get the same salary attribute value.
- Likewise,

 $\mathtt{Project} o \mathtt{Budget}$ 

i.e., each project has a unique budget.

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Normal Forms — 7

# **Functional Dependencies**

- Given schema R(x) and non-empty subsets Y and Z of the attributes X, we say that there is a functional dependency between Y and Z ( $Y \rightarrow Z$ ), iff for every relation instance Y of R(X) and every pair of tuples  $t_1$ ,  $t_2$  of Y, if  $t_1 \cdot Y = t_2 \cdot Y$ , then  $t_1 \cdot Z = t_2 \cdot Z$ .
- A functional dependency is a statement about all allowable relations for a given schema.
- Functional dependencies have to be identified by understanding the semantics of the application.
- Given a particular relation  $r_0$  of R(x), we can tell if a dependency holds or not; but just because it holds for  $r_0$ , doesn't mean that it also holds for R(x)!

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# **Looking for FDs**

<b>Employee</b>	Salary	<u>Project</u>	Budget	Function
Brown	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55 )	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2 /	manager
Moore	48	Venus	15	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

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Normal Forms — 9

# **Non-Trivial Dependencies**

- A functional dependency  $\mathbf{Y} \rightarrow \mathbf{z}$  is *non-trivial* if no attribute in  $\mathbf{z}$  appears among attributes of  $\mathbf{Y}$ , e.g.,
  - ✓ Employee → Salary is non-trivial;
  - ✓ Employee, Project → Project is trivial.
- Anomalies arise precisely for the attributes which are involved in (non-trivial) functional dependencies:
  - √Employee → Salary;
  - $\checkmark$  Project → Budget.
- Moreover, note that our example includes another functional dependency:
- $\checkmark$  Employee, Project  $\rightarrow$  Function. CSC343 Introduction to Databases

# Dependencies Cause Anomalies, ... Sometimes!

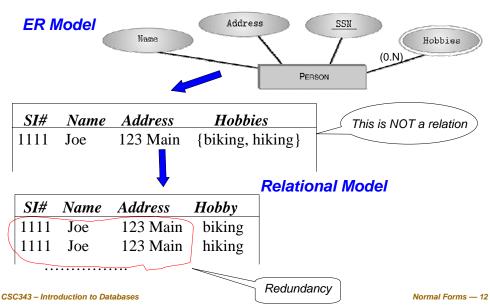
- The first two dependencies cause undesirable redundancies and anomalies.
- The third dependency, however, does not cause redundancies because {Employee,Project} constitutes a key of the relation (...and a relation cannot contain two tuples with the same values for the key attributes.)

<u>Dependencies on keys are OK,</u> <u>other dependencies are not!</u>

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Normal Forms — 11

# **Another Example**



# **How Do We Eliminate Redundancy?**

- Decomposition: Use two relations to store Person information:
  - ✓ Person1 (SI#, Name, Address)
  - √ Hobbies (SI#, Hobby)
- The decomposition is more general: people hobbies with can now be described independently of their name and address.
- No update anomalies:
  - ✓ Name and address stored once;
  - ✓ A hobby can be separately supplied or deleted;
  - ✓ We can represent persons with no hobbies.

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Normal Forms — 13

# **Superkey Constraints**

- A superkey constraint is a special functional dependency: Let K be a set of attributes of R, and U the set of all attributes of R. Then K is a superkey iff the functional dependency  $K \to U$  is satisfied in R.
  - $\checkmark$  E.g., SI# → SI#, Name, Address (for a Person relation)
- $\blacksquare$  A *key* is a minimal superkey, I.e., for each  $X \subset K$ , X is not a superkey
  - ✓ SI#, Hobby → SI#, Name, Address, Hobby
  - $\checkmark$  SI# → 'S<sub>I</sub>I#, Name, Address, Hobby
- A key attribute is an attribute that is part of a Key. CSC343 – Introduction to Databases

### **More Examples**

- Address → PostalCode
  - ✓ DCS's postal code is M5S 3H5
- Author, Title, Edition → PublicationDate
  - ✓ Ramakrishnan, et al., Database Management Systems, 3<sup>rd</sup> publication date is 2003
- CourseID → ExamDate, ExamTime
  - √CSC343's exam date is December 18, starting at 7pm

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Normal Forms — 15

# When are FDs "Equivalent"?

- Sometimes functional dependencies (FDs) seem to be saying the same thing, e.g., Addr → PostalCode, Str# vs Addr → PostalCode, Addr → Str#
- Another example

  Addr → PostalCode, PostalCode → Province

  vs Addr → PostalCode, PostalCode →

  Province

  Addr → Province
- When are two sets of FDs equivalent? How do we "infer" new FDs from given FDs?

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### **Entailment, Closure, Equivalence**

- If F is a set of FDs on schema R and f is another FD on R, then F entails f (written F |= f) if every instance r of R that satisfies every FD in F also satisfies f.
  - ✓ Example:  $F = \{A \rightarrow B, B \rightarrow C\}$  and f is  $A \rightarrow C$ 
    - ✓If Phone# → Address and Address → ZipCode, then Phone# → ZipCode
- The *closure* of F, denoted  $F^+$ , is the set of all FDs entailed by F.
- F and G are equivalent if F entails G and G entails F.

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Normal Forms — 17

# **How Do We Compute Entailment?**

- Satisfaction, entailment, and equivalence are semantic concepts – defined in terms of the "meaning" of relations in the "real world."
- $\blacksquare$  How to check if F entails f, F and G are equivalent?

  - ✓ Find algorithmic, syntactic ways to compute these notions.
- Note: The syntactic solution must be "correct" with respect to the semantic definitions.
- Correctness has two aspects: soundness and completeness see later.

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  Normal Forms 18

# **Armstrong's Axioms for FDs**

- This is the syntactic way of computing/testing semantic properties of FDs
  - $\checkmark$  *Reflexivity*:  $Y \subseteq X \mid -X \rightarrow Y$  (trivial FD)

e.g., | - Name, Address → Name

✓ Augmentation:  $X \rightarrow Y \mid -XZ \rightarrow YZ$ 

e.g.,  $Address \rightarrow ZipCode \mid Address, Name \rightarrow ZipCode, Name$ 

 $\checkmark$  Transitivity:  $X \rightarrow Y$ ,  $Y \rightarrow Z \mid -X \rightarrow Z$ 

e.g., Phone#  $\rightarrow$  Address, Address  $\rightarrow$  ZipCode

| - Phone# → ZipCode

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Normal Forms — 19

#### Soundness

- Theorem: F |- f implies F |= f
- In words: If FD f: X → Y can be derived from a set of FDs F using the axioms, then f holds in every relation that satisfies every FD in F.
- Example: Given  $X \rightarrow Y$  and  $X \rightarrow Z$  then  $X \rightarrow XY$  Augmentation by X  $YX \rightarrow YZ$  Augmentation by Y  $X \rightarrow YZ$  Transitivity
- Thus, X o YZ is satisfied in every relation where both X o Y and X o Z are satisfied. We have derived the *union rule* for FDs.

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## Completeness

- Theorem: F |= f implies F |- f
- In words: If *F* entails *f*, then *f* can be derived from *F* using Armstrong's axioms.
- A consequence of completeness is the following (naïve) algorithm to determining if F entails f:

**Algorithm:** Use the axioms in all possible ways to generate  $F^+$  (the set of possible FD's is finite so this can be done) and see if f is in  $F^+$ 

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Normal Forms — 21

#### Correctness

- The notions of *soundness* and *completeness* link the syntax (Armstrong's axioms) with semantics, I.e., entailment defined in terms of relational instances.
- This is a precise way of saying that the algorithm for entailment based on the axioms is ``correct" with respect to the definitions.

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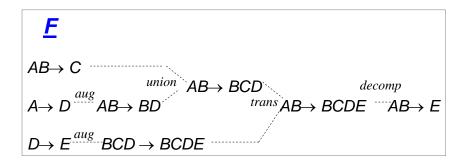
# **Decomposition Rule**

- Another example of a derivation rule we can use in generating F+:
- $\blacksquare$  X  $\rightarrow$  AB, AB  $\rightarrow$  A (refl), X  $\rightarrow$  A (trans)
- So, whenever we have X → AB, we can "decompose" this functional dependency to two functional dependencies X → A, X → B

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Normal Forms — 23

# **Generating F**+



Thus,  $AB \rightarrow BD$ ,  $AB \rightarrow BCD$ ,  $AB \rightarrow BCDE$ , and  $AB \rightarrow E$  are all elements of  $F^+$ .

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#### **Attribute Closure**

- Calculating <u>attribute closure</u> leads to a more efficient way of checking entailment.
- The *attribute closure* of a set of attributes X with respect to a set of FDs F, denoted  $X^+_{F}$ , is the set of all attributes A such that  $X \to A$   $\checkmark X^+_{F}$  is not necessarily same as  $X^+_{G}$  if  $F \ne G$
- Attribute closure and entailment:

Algorithm: Given a set of FDs, F, then  $X \rightarrow Y$  if and only if  $Y \subseteq X^+_F$ 

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Normal Forms — 25

# Computing Attribute Closure: An Example

$$F: AB \to C$$

$$A \to D$$

$$D \to E$$

$$AC \to B$$

$$A = \{A, D, E\}$$

$$AB = \{A, B, C, D, E\}$$

$$AC = \{A, C, B, D, E\}$$

$$B = \{B\}$$

$$D = \{D, E\}$$

Is  $AB \rightarrow E$  entailed by F? Yes Is  $D \rightarrow C$  entailed by F? No

*Result*:  $X_F^+$  allows us to determine all FDs of the form  $X \to Y$  entailed by F

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# Computing the Attribute Closure X+<sub>F</sub>

```
closure := X;  // since X \subseteq X^+_F

repeat

old := closure;

if there is an FD Z \to V in F such that

Z \subseteq closure and V \nsubseteq closure

then closure := closure \cup V

until old = closure

- If T \subseteq closure then X \to T is entailed by F
```

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Normal Forms — 27

#### **Normal Forms**

- Each normal form is a set of conditions on a schema that together guarantee certain properties (relating to redundancy and update anomalies).
- First normal form (1NF) is the same as the definition of relational model (relations = sets of tuples; each tuple = sequence of atomic values).
- Second normal form (2NF) has no practical or theoretical value – won't discuss.
- The two most used are *third normal form* (3NF) and *Boyce-Codd normal form* (BCNF).
- We will discuss in detail the 3NF.

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#### The Third Normal Form

- A relation R(X) is in *third normal form* (3NF) if, for each (non-trivial) functional dependency Y  $\rightarrow$  Z, at least one of the following is true:
  - √Y contains a key K of R(X);
  - ✓ Each attribute in Z is contained in at least one key of R(X).
- 3NF does not remove all redundancies.
- 3NF decompositions founded on the notion of *minimal cover*.

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Normal Forms — 29

# **Decomposition into 3NF: Basic Idea**

- Decomposition into 3NF can proceed as follows.
  - For each functional dependency of the form  $Y \to Z$ , where Y contains a subset of a key X of R(X), create a projection on all the attributes Y, Z (2NF).
  - For each dependency of the form  $Y \rightarrow Z$ , where Y, doesn't contain any key, and not all attributes of Z are key attributes, create a projection on all the attributes Y, Z (3NF).
- The new relations only include dependencies Y
  → z, where Y contains a key K of R(X), or Z contains only key attributes.

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#### **Basic Idea**

- R(<u>AB</u>CD), A --> D
- Projection:
  - √ R1(AD), A --> D
  - √ R2(<u>AB</u>C)

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Normal Forms — 31

# **Normalization Through Decomposition**

- A relation that is not in 3NF, can be replaced with one or more normalized relations using *normalization*.
- We can eliminate redundancies and anomalies for the example relation

Emp(Employee, Salary, Project, Budget, Function)

if we replace it with the three relations obtained by projections on the sets of attributes corresponding to the three functional dependencies:

- ✓Employee → Salary;
- $\checkmark$  Project  $\rightarrow$  Budget.
- $\checkmark$  Employee, Project  $\rightarrow$  Function.

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#### ...Start with...

<b>Employee</b>	Salary	<u>Project</u>	Budget	Function
Brown	20	Mars	2	technician
Green	35	Jupiter	15	designer
Green	35	Venus	15	designer
Hoskins	55	Venus	15	manager
Hoskins	55 )	Jupiter	15	consultant
Hoskins	55	Mars	2	consultant
Moore	48	Mars	2	manager
Moore	48	Venus	<del>15</del>	designer
Kemp	48	Venus	15	designer
Kemp	48	Jupiter	15	manager

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Normal Forms — 33

# **Result of Normalization**

<b>Employee</b>	Salary
Brown	20
Green	35
Hoskins	55
Moore	48
Kemp	48

<b>Employee</b>	Project	Function
Brown	Mars	technician
Green	Jupiter	designer
Green	Venus	designer
Hoskins	Venus	manager
Hoskins	Jupiter	consultant
Hoskins	Mars	consultant
Moore	Mars	manager
Moore	Venus	designer
Kemp	Venus	designer
Kemp	Jupiter	manager

<u>Project</u>	Budget
Mars	2
Jupiter	15
Venus	15

The keys of new relations are lefthand sides of functional dependencies; satisfaction of 3NF is therefore guaranteed for the new relations.

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# **Another Example**

<b>Employee</b>	<b>Project</b>	Branch
Brown	Mars	Chicago
Green	Jupiter	Birmingham
Green	Venus	Birmingham
Hoskins	Saturn	Birmingham
Hoskins	Venus	Birmingham

This relation satisfies the functional dependencies:

- ✓ Employee  $\rightarrow$  Branch
- ✓ Project → Branch

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Normal Forms — 35

# **A Possible Decomposition**

<b>Employee</b>	Branch
Brown	Chicago
Green	Birmingham
Hoskins	Birmingham

<u>Project</u>	Branch
Mars	Chicago
Jupiter	Birmingham
Saturn	Birmingham
Venus	Birmingham

...but now we don't know each employee's projects!

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# The Join of the Projections

<b>Employee</b>	<b>Project</b>	Branch
Brown	Mars	Chicago
Green	Jupiter	Birmingham
Green	Venus	Birmingham
Hoskins	Saturn	Birmingham
Hoskins	Venus	Birmingham
Green	Saturn	Birmingham
Hoskins	Jupiter	Birmingham

The result of the join is different from the original relation.

We lost some information during the decomposition!

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Normal Forms — 37

# **Lossless Decomposition**

- The decomposition of a relation R(X) on  $X_1$  and  $X_2$  is *lossless* if for every instance r of R(X) the join of the projections of R on  $X_1$  and  $X_2$  is equal to r itself (that is, does not contain *spurious* tuples).
- Of course, it is clearly desirable to allow only lossless decompositions during normalization.

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# A Condition for Lossless Decomposition

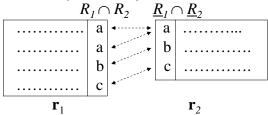
- Let R(x) be a relation schema and let  $x_1$  and  $x_2$  be two subsets of x such that  $x_1 \cup x_2 = x$ . Also, let  $x_0 = x_1 \cap x_2$ .
- If R(X) satisfies the functional dependency  $X_0 \to X_1$  or  $X_0 \to X_2$ , then the decomposition of R(X) on  $X_1$  and  $X_2$  is lossless.
- In other words, R(X) has a lossless decomposition on two relations if the set of attributes common to the relations is a *superkey* for at least one of the decomposed relations.

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Normal Forms — 39

# Intuition Behind the Test for Losslessness

■ Suppose  $R_1 \cap R_2 \rightarrow R_2$ . Then a row of  $r_1$  can combine with *exactly* one row of  $r_2$  in the natural join (since in  $r_2$  a particular set of values for the attributes in  $R_1 \cap R_2$  defines a unique row)



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# **A Lossless Decomposition**

<b>Employee</b>	Branch
Brown	Chicago
Green	Birmingham
Hoskins	Birmingham

<b>Employee</b>	Project	
Brown	Mars	
Green	Jupiter	
Green	Venus	
Hoskins	Saturn	
Hoskins	Venus	

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Normal Forms — 41

#### **Notation**

■ Instead of saying that we have relation schema R(X) with functional dependencies *F*, we will say that we have schema

$$\mathcal{R} = (R, F)$$

- , where R is a set of attributes and F is a set of functional dependencies.
- The 3NF normalization problem is then to generate a set of relation schemas  $\mathcal{R}_1 = (R_1, F_1), ..., \mathcal{R}_n = (R_n, F_n)$ , such that  $\mathcal{R}_i$  is in 3NF.

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### **Another Example**

■ Schema (R, F) where  $R = \{SI\#, Name, Address, Hobby\}$   $F = \{SI\# \rightarrow Name, Address\}$  can be decomposed into  $R_1 = \{SI\#, Name, Address\}$   $F_1 = \{SI\# \rightarrow Name, Address\}$  and  $R_2 = \{SI\#, Hobby\}$   $F_2 = \{\}$  since  $R_1 \cap R_2 = SI\#, SI\# \rightarrow R_1$  the decomposition is lossless.

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Normal Forms — 43

#### **Another Problem...**

- Assume we wish to insert a new tuple that specifies that employee Armstrong works in the Birmingham branch and participates in project Mars.
- In the original relation, this update would be identified as illegal, because it would cause a violation of the Project → Branch dependency.
- For the decomposed relations, however, this is not possible because the two attributes Project and Branch have been moved to different relations.

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## **Preserving Dependencies (Intuition)**

- A decomposition *preserves dependencies* if each of the functional dependencies of the original relation schema involves attributes that appear together in one of the decomposed relation schemas.
- It is clearly desirable that a decomposition preserves dependencies because then it is possible to ensure that the decomposed schema satisfies the same constraints as the original schema.

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Normal Forms — 45

# **Example**

```
Schema (R, F) where
    R = {SI#,Name,Address,Hobby}
    F = {SI# → Name,Address}
    can be decomposed into
    R<sub>1</sub> = {SI#, Name,Address}
    F<sub>1</sub> = {SI# → Name,Address}
    and
    R<sub>2</sub> = {SI#, Hobby}
    F<sub>2</sub> = { }

Since F = F<sub>1</sub> ∪ F<sub>2</sub> the decomposition is dependency preserving.
```

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# **Another Example**

- Schema: (ABC; F),  $F = \{A \rightarrow B, B \rightarrow C, C \rightarrow B\}$
- Decomposition:
  - $\checkmark$  (AC,  $F_1$ ),  $F_1 = \{A \rightarrow C\}$ [Note:  $A \rightarrow C \notin F$ , but in  $F^+$ ]  $\checkmark$  (BC,  $F_2$ ),  $F_2 = \{B \rightarrow C, C \rightarrow B\}$
- $A \rightarrow B \notin (F_1 \cup F_2)$ , but  $A \rightarrow B \in (F_1 \cup F_2)^+$ . ✓ So  $F^+ = (F_1 \cup F_2)^+$  and thus the decomposition is still dependency preserving

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Normal Forms — 47

# **Dependency Preservation**

- If f is a FD in F, but f is not in  $F_1 \cup F_2$ , there are two possibilities:
  - $\checkmark f \in (F_1 \cup F_2)^+$ 
    - ✓If the constraints in  $F_1$  and  $F_2$  are maintained, f will be maintained automatically.
  - $\checkmark f \notin (F_1 \cup F_2)^+$ 
    - $\checkmark f$  can be checked only by first taking the join of  $r_1$  and  $r_2$ . ... This is costly...

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# Desirable Qualities for Decompositions

Decompositions should always satisfy the properties of lossless decomposition and dependency preservation:

- Lossless decomposition ensures that the information in the original relation be can reconstructed based accurately on the information represented in the decomposed relations.
- Dependency preservation ensures that the decomposed relations have the same capacity to represent the integrity constraints as the original relations and therefore to reveal illegal updates.

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Normal Forms — 49

#### **Minimal Cover**

- A *minimal cover* for a set of dependencies *F* is a set of dependencies *U* such that:
  - ✓ *U* is equivalent to *F* (I.e.,  $F^+ = U^+$ )
  - ✓ All FDs in *U* have the form  $X \rightarrow A$  where *A* is a single attribute
  - ✓It is not possible to make U smaller (while preserving equivalence) by
    - ✓ Deleting an FD
    - ✓ Deleting an attribute from an FD (its LHS)
- FDs and attributes that can be deleted in this way are called *redundant*.

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# **Computing the Minimal Cover**

Example:  $F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E\}$ 

- Step 1: Make RHS of each FD into a single attribute: Use decomposition rule for FDs.
  - ✓ Example:  $L \rightarrow AD$  replaced by  $L \rightarrow A$ ,  $L \rightarrow D$ ;  $ABH \rightarrow CK$  by  $ABH \rightarrow C$ ,  $ABH \rightarrow K$
- Step 2: Eliminate redundant attributes from LHS: If B is a single attribute and FD  $XB \rightarrow A \in F$ ,  $X \rightarrow A$  is entailed by F, then B is unnecessary.
  - e.g., Can an attribute be deleted from  $ABH \rightarrow C$ ? Compute  $AB^+_F$ ,  $AH^+_F$ ,  $BH^+_F$ ; Since  $C \in (BH)^+_F$ ,  $BH \rightarrow C$  is entailed by F and A is redundant in  $ABH \rightarrow C$ .

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Normal Forms — 51

# **Computing the Minimal Cover (cont'd)**

- Step 3: Delete redundant FDs from F: If  $F \{f\}$  entails f, then f is redundant; if f is  $X \to A$  then check if  $A \in X^+_{F-\{f\}}$ 
  - e.g.,  $BGH \rightarrow L$  is entailed by  $E \rightarrow L$ ,  $BH \rightarrow E$ , so it is redundant
- Note: The order of steps 2, 3 can't be interchanged!! See textbook for a counterexample.

```
F_{1} = \{ABH \rightarrow C, ABH \rightarrow K, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}
F_{2} = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, BH \rightarrow L, L \rightarrow A, L \rightarrow D, E \rightarrow L, BH \rightarrow E\}
F_{3} = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, L \rightarrow A, E \rightarrow L\}
```

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# Synthesizing a 3NF Schema

Starting with a schema R = (R, F):

- Step 1: Compute minimal cover U of F. The decomposition is based on U, but since  $U^+ = F^+$  the same functional dependencies will hold.
  - ✓A minimal cover for

$$F = \{ABH \rightarrow CK, A \rightarrow D, C \rightarrow E, BGH \rightarrow L, L \rightarrow AD, E \rightarrow L, BH \rightarrow E\}$$
 is

$$U = \{BH \rightarrow C, BH \rightarrow K, A \rightarrow D, C \rightarrow E, L \rightarrow A, E \rightarrow L\}$$

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Normal Forms — 53

# Synthesizing ... Step 2

Step 2: Partition U into sets  $U_1$ ,  $U_2$ , ...  $U_n$  such that the LHS of all elements of  $U_i$  are the same:

$$✓ U_1 = \{BH \to C, BH \to K\}, U_2 = \{A \to D\},$$
 $U_3 = \{C \to E\}, U_4 = \{L \to A\}, U_5 = \{E \to L\}$ 

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# Synthesizing ... Step 3

- Step 3: For each  $U_i$  form schema  $R_i = (R_i, U_i)$ , where  $R_i$  is the set of all attributes mentioned in  $U_i$ 
  - ✓ Each FD of *U* will be in some R<sub>i</sub>. Hence the decomposition is *dependency preserving*:
  - $\checkmark R_1 = (BHCK; BH \rightarrow C, BH \rightarrow K),$
  - $\checkmark R_2 = (AD; A \rightarrow D),$
  - $\checkmark R_3 = (CE; C \rightarrow E),$
  - $\checkmark R_4 = (AL; L \rightarrow A),$
  - $\checkmark R_5 = (EL; E \rightarrow L)$

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Normal Forms — 55

# Synthesizing ... Step 4

- Step 4: If no  $R_i$  is a superkey of R, add schema  $R_0 = (R_{O'}\{\})$  where  $R_O$  is a key of R.
  - $\checkmark$ R<sub>0</sub> = (BGH, {}); R<sub>0</sub> might be needed when not all attributes are contained in R<sub>1</sub>∪R<sub>2</sub> ...∪R<sub>n</sub>;
  - ✓A missing attribute A must be part of all keys (since it's not in any FD of U, deriving a key constraint from U involves the augmentation axiom);
  - $\checkmark$ R<sub>0</sub> might be needed even if all attributes are accounted for in  $R_1 \cup R_2 \dots \cup R_n$

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# Synthesizing ... Step 4 (cont'd)

■ Example:  $(ABCD; \{A \rightarrow B, C \rightarrow D\})$ , with step 3 decomposition:  $R_1 = (AB; \{A \rightarrow B\}), R_2 = (CD; \{C \rightarrow D\})$ .

#### Lossy! Need to add (AC; { }), for losslessness

Step 4 guarantees lossless decomposition:
ABCD --decomp--> AB,ACD --decomp-->AB,AC,CD

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Normal Forms — 57

# **Boyce-Codd Normal Form (BCNF)**

- A relation R(X) is in *Boyce–Codd Normal Form* if for every non-trivial functional dependency  $Y \to Z$  defined on it, Y contains a key K of R(X). That is, Y is a superkey for R(X).
- Example: Person1(SI#, Name, Address)
  ✓The only FD is SI# → Name, Address
  ✓Since SI# is a key, Person1 is in BCNF
- Anomalies and redundancies, as discussed earlier, do not occur in databases with relations in BCNF.

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# **Non-BCNF Examples**

- Person(SI#, Name, Address, Hobby)
  - ✓ The FD  $SI\# \rightarrow Name$ , Address does **not** satisfy conditions for BCNF since the key is (SSN, Hobby)
- HasAccount(AcctNum, ClientId, OfficeId)
  - √The FD AcctNum → OfficeId does not satisfy BCNF conditions if we assume that keys for HasAccount are (ClientId, OfficeId) and (AcctNum, ClientId); rather than AcctNum.

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Normal Forms — 59

#### **Normalization Drawbacks**

- By limiting redundancy, normalization helps maintain consistency and saves space.
- But performance of querying can suffer because related information that was stored in a single relation is now distributed among several
- Example: A join is required to get the names and grades of all students taking CS343 in 2006F.

SELECT S.Name, T.Grade
FROM Student S, Transcript T
WHERE S.Id = T.StudId AND
T.CrsCode = 'CS343' AND T.Semester = '2006F'

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#### **Denormalization**

- Tradeoff: Judiciously introduce redundancy to improve performance of certain queries
- Example: Add attribute Name to Transcript
  - --> Transcript'

SELECT T.Name, T.Grade FROM Transcript' T WHERE T. CrsCode = 'CS305' AND T. Semester = 'S2002'

- ✓ Join is avoided;
- ✓ If gueries are asked more frequently than Transcript is modified, added redundancy might improve average performance;
- ✓ But, Transcript' is no longer in BCNF since key is (StudId, CrsCode, Semester)  $StudId \rightarrow Name.$  CSC343 - Introduction to Databases

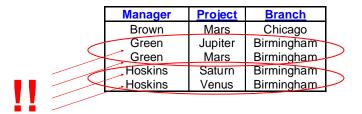
Normal Forms — 61

#### **BCNF** and 3NF

- The Project-Branch-Manager schema is not in BCNF, but it is in 3NF.
- In particular, the Project, Branch → Manager dependency has as its left hand side a key, while Manager → Branch has a unique attribute for the right hand side, which is part of the {Project, Branch} key.
- The 3NF is less restrictive than the BCNF and for this reason does not offer the same guarantees of quality for a relation; it has the advantage however, of always achievable.

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# 3NF Tolerates Some Redundancies!



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Normal Forms — 63

# **A Revised Example**

<u>Manager</u>	<b>Project</b>	Branch	Division
Brown	Mars	Chicago	1
Green	Jupiter	Birmingham	1
Green	Mars	Birmingham	1
Hoskins	Saturn	Birmingham	2
Hoskins	Venus	Birmingham	2

#### Functional dependencies:

- Manager → Branch, Division -- each manager works at one branch and manages one division;
- Branch, Division → Manager -- for each branch and division there is a single manager;
- Project, Branch Division, Manager -- for each branch, a project is allocated to a single division and has a sole manager responsible.

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### **A Good Decomposition**

<u>Manager</u>	Branch	Division
Brown	Chicago	1
Green	Birmingham	1
Hoskins	Birmingham	2

<u>Project</u>	<u>Branch</u>	Division
Mars	Chicago	1
Jupiter	Birmingham	1
Mars	Birmingham	1
Saturn	Birmingham	2
Venus	Birmingham	2

- Note: The first relation has a second key {Branch,Division}.
- The decomposition is in 3NF but not in BCNF; moreover, it is lossless and dependencies are preserved.
- This example demonstrates that BCNF is too strong a condition to impose on a relational schema.

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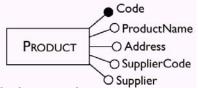
Normal Forms — 65

# **Database Design and Normalization**

- The theory of normalization can be used as a basis for quality control operations on schemas, during both conceptual and logical design.
- Analysis of the relations obtained during the logical design phase can identify places where the conceptual design was inaccurate: such a validation of the design is usually relatively easy.
- Normalization can also be used during conceptual design for quality control of each element of a conceptual schema (entity or relationship).

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# **Analysis of an Entity**



■ The functional dependency

SupplierCode → Supplier,Address holds here: all properties of a supplier are identified by its SupplierCode.

■ The entity violates 3NF since this dependency has a left hand side that does not contain the identifier and a right hand side made up of attributes that are not part of the key.

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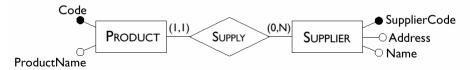
Normal Forms — 67

# **Decomposing Product**

- Supplier is (or should be) an independent entity, with its own attributes (code, surname and address)
- If Product and Supplier are distinct entities, they should be linked through a relationship.
- Since there is a functional dependency from Code to SupplierCode, we are sure that each product has at most one supplier (maximum cardinality 1).
- Since there is no dependency from SupplierCode to Code, we have an unrestricted maximum cardinality (N) for Supplier in the relationship.

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# **Decomposing Product**



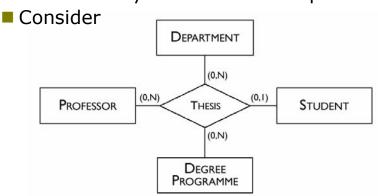
- This decomposition satisfies fundamental properties:
  - ✓It is a lossless decomposition, because of oneto-many relationship that allows us to recostruct the values of the attributes of the original entity;
  - ✓ Moreover, it preserves dependencies because each dependency is embedded in one of the entities or can be reconstructed from them.

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Normal Forms — 69

## **Analysis of a Relationship**

Now we show how to analyze n-ary relationships for n≥3, in order to determine whether they should be decomposed.



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### **Some Functional Dependencies**

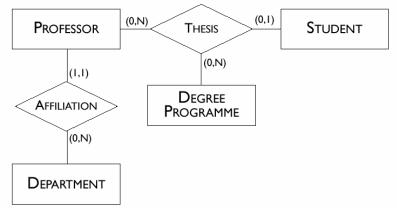
- ✓ Student → DegreeProgramme (each student is enrolled in one degree programme)
- ✓ Student → Professor (each student writes a thesis under the supervision of a single professor)
- ✓Professor → Department (each professor is associated with a single department and the students under her supervision are students in that department)
- The (unique) key of the relationship is Student (given a student, the degree programme, the professor and the department are identified uniquely)
- The third FD causes a violation of 3NF.

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Normal Forms — 71

### **Decomposing Thesis**

■ The following is a decomposition of Thesis where the two decomposed relationships are both in 3NF(also in BCNF)



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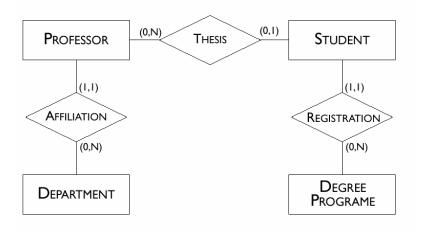
#### More Observations...

- The relationship Thesis is in 3NF, because its key is made up of the Student entity, and its dependencies all have this entity on the left hand side.
- However, not all students write theses, therefore not all students have supervisors.
- From a normal form point of view, this is not a problem.
- However, our conceptual schema should reflect the fact that being in a degree programme and having a supervisor are independent facts.

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Normal Forms — 73

# **Another Decomposition**



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