
Lecture 18: Distributed Agreement

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A rose by any other name...

- Distributed Consensus has many names (depending on the assumptions and application)
 - Reliable multicast
 - Byzantine Generals Problem
 - Interactive agreement
 - Atomic broadcast

“This has resulted in a voluminous literature which, unfortunately, is not distinguished for its coherence. The differences in notation and the haphazard nature of the assumptions obfuscates the close relationship among these problems”

- Hadzilacos & Toueg, Distributed Systems.

Outline

- Distributed Algorithms
- Distributed Agreement
- Castro's BFT Library

Distributed Algorithms

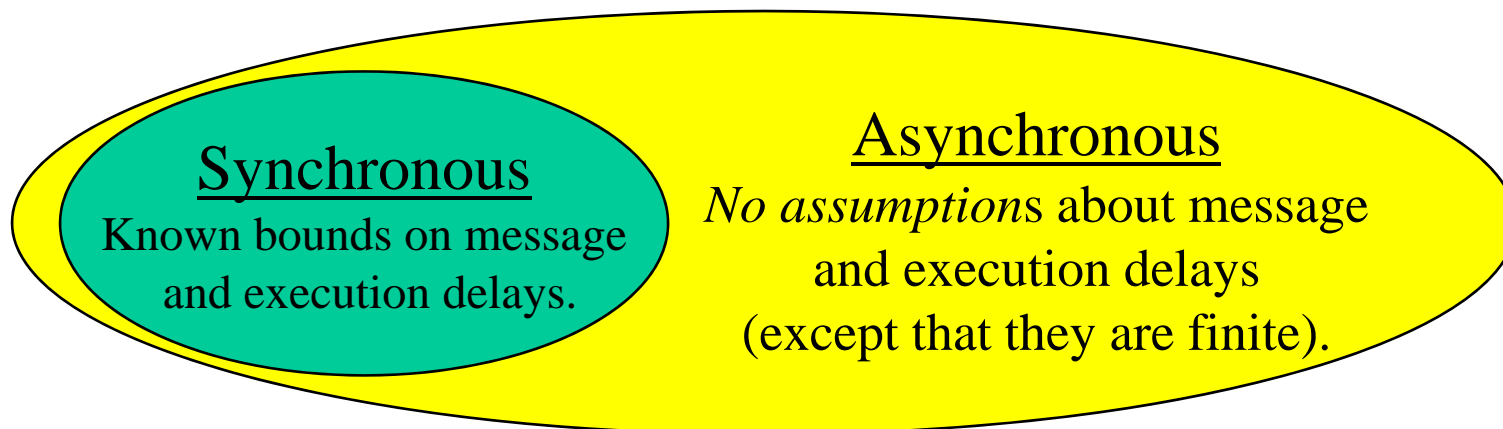
- System model from last lecture.
- Distributed system is composed of n processes
- A process executes a sequence of events
 - Local computation
 - Sending a message m
 - Receiving a message m
- A distributed algorithm is an algorithm that runs on more than one process.

Properties of Distributed Algorithms

- Safety
 - Means that some particular "bad" thing never happens.
- Liveness
 - Indicates that some particular "good" thing will (eventually) happen.
- Timing/failure assumptions affect how we reason about these properties and what we can prove

Timing Model

- Specifies assumptions regarding *delays* between
 - execution steps of a *correct* process
 - send and receipt of a message sent between *correct* processes
- Many gradations. Two of interest are:



- *Partial synchrony* is more realistic in distrib. system

Synchronous timing assumption

- Processes share a clock
- Timestamps mean something between processes
- Communication can be guaranteed to occur in some number of clock cycles

Asynchronous timing assumption

- Processes operate asynchronously from one another.
- No claims can be made about whether another process is running slowly or has failed.
- There is no time bound on how long it takes for a message to be delivered.

Partial synchrony assumption

- “Timing-based distributed algorithms”
- Processes have some information about time
 - Clocks that are synchronized within some bound
 - Approximate bounds on message-deliver time
 - Use of timeouts

Failure Model

- A process that behaves according to its I/O specification throughout its execution is called correct
- A process that deviates from its specification is faulty
- Many gradations of faulty. Two of interest are:

Fail-Stop failures

A faulty process halts execution prematurely.

Byzantine failures

No assumption about behavior of a faulty process.

Errors as failure assumptions

- Specific types of errors are listed as failure assumptions
 - Communication link may lose messages
 - Link may duplicate messages
 - Link may reorder messages
 - Process may die and be restarted

Fail-Stop failure

- A failure results in the process, p , stopping
 - Also referred to as *crash failure*
 - p works correctly until the point of failure
- p does not send any more messages
- p does not perform actions when messages are sent to it
- Other processes can detect that p has failed

Fault/failure detectors

- A perfect failure detector
 - No false positives (only reports actual failures).
 - Eventually reports failures to all processes.
- Heartbeat protocols
 - Assumes partially synchronous environment
 - Processes send "I'm Alive" messages to all other processes regularly
 - If process i does not hear from process j in some time $T = T_{\text{delivery}} + T_{\text{heartbeat}}$ then it determines that j has failed
 - Depends on T_{delivery} being known and accurate

Other Failure Models

- We can classify some of the likely failure modes that lie between crash and Byzantine
 - Omission failure
 - Process fails to send messages, to receive incoming messages, or to handle incoming messages
 - Timing failure
 - process's response lies outside specified time interval
 - Response failure
 - Value of response is incorrect

Byzantine failure

- Process p fails in an arbitrary manner.
- p is modeled as a malevolent entity
 - Can send the messages and perform the actions that will have the worst impact on other processes
 - Can collaborate with other "failed" processes
- Common constraints on Byzantine assumption
 - Incomplete knowledge of global state
 - Limited ability to coordinate with other Byzantine processes
 - Restricted to polynomial computation (i.e., assume $P \neq NP$...)

Setup of Distributed Consensus

- N processes have to agree on a single value.
 - Example applications of consensus:
 - Performing a commit in a replicated/distributed database.
 - Collecting multiple sensor readings and deciding on an action
- Each process begins with a value
- Each process can irrevocably *decide* on a value
- Up to $f < n$ processes may be faulty
 - How do you reach consensus if no failures?

Properties of Distributed Consensus

- *Agreement*
 - If *any correct* process believes that V is the consensus value, then *all correct* processes believe V is the consensus value.
- *Validity*
 - If V is the consensus value, then some process proposed V .
- *Termination*
 - Each process decides some value V .
- *Agreement* and *Validity* are **Safety** Properties
- *Termination* is a **Liveness** property.

Synchronous Fail-stop Consensus

- FloodSet algorithm run at each process i
 - Remember, we want to tolerate up to f failures

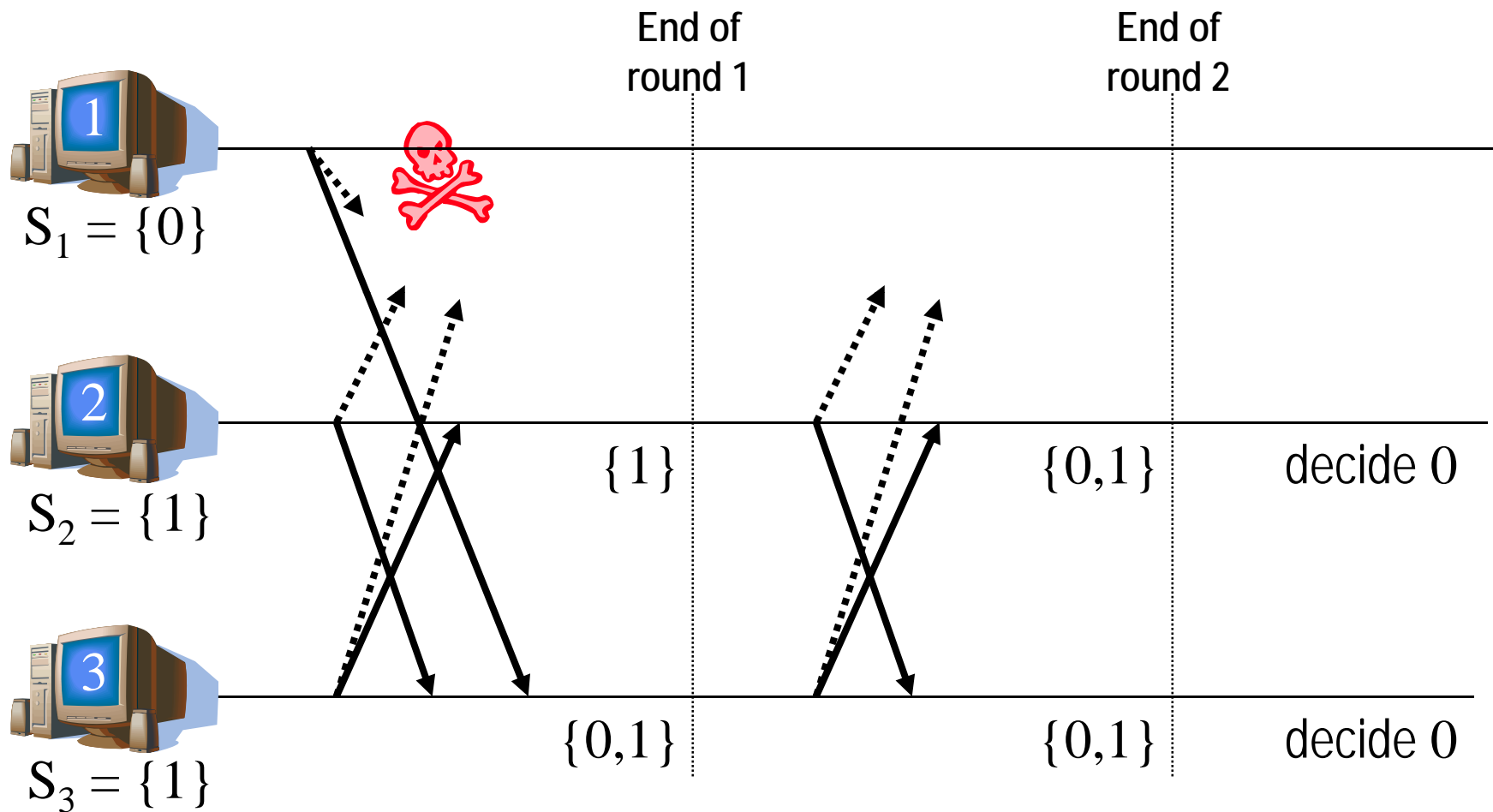
```
Si ← {initial value}
for k = 1 to f+1
  send Si to all processes
  receive Sj from all j ≠ i
  Si ← Si ∪ Sj (for all j)
end for
Decide(Si)
```

- S is a set of values
- Decide(x) can be various functions
 - E.g. min(x), max(x), majority(x), or some default
- Assumes nodes are connected and links do not fail

Analysis of FloodSet

- Requires $f+1$ rounds because process can fail at any time, in particular, during send
- *Agreement*. Since at most f failures, then after $f+1$ rounds all correct processes will evaluate $\text{Decide}(S_i)$ the same.
- *Validity*. Decide results in a proposed value (or default value)
- *Termination*. After $f+1$ rounds the algorithm completes

Example with $f = 1$, $\text{Decide}() = \min()$



Synchronous/Byzantine Consensus

- Faulty processes can behave arbitrarily
 - May actively try to trick other processes
- Algorithm described by Lamport, Shostak, & Pease in terms of Byzantine generals agreeing whether to attack or retreat. Simple requirements:
 - All loyal generals decide on the same plan of action
 - Implies that all loyal generals obtain the same information
 - A small number of traitors cannot cause the loyal generals to adopt a bad plan
 - Decide() in this case is a majority vote, default action is "Retreat"

Byzantine Generals

- Use $v(i)$ to denote value sent by i^{th} general
- traitor could send different values to different generals, so can't use $v(i)$ obtained from i directly.
New conditions:
 - Any two loyal generals use the same value $v(i)$, regardless of whether i is loyal or not
 - If the i^{th} general is loyal, then the value that she sends must be used by every loyal general as the value of $v(i)$.
- Re-phrase original problem as *reliable broadcast*:
 - General must send an order ("Use v as my value") to lieutenants
 - Each process takes a turn as General, sending its value to the others as lieutenants
 - After all values are reliably exchanged, Decide()

Synchronous Byzantine Model

Theorem: There is no algorithm to solve consensus if only oral messages are used, unless *more than two thirds* of the generals are loyal.

- In other words, impossible if $n \leq 3f$ for n processes, f of which are faulty
- *Oral messages* are under control of the sender
 - sender can alter a message that it received before forwarding it
- Let's look at examples for special case of $n=3$, $f=1$

Case 1

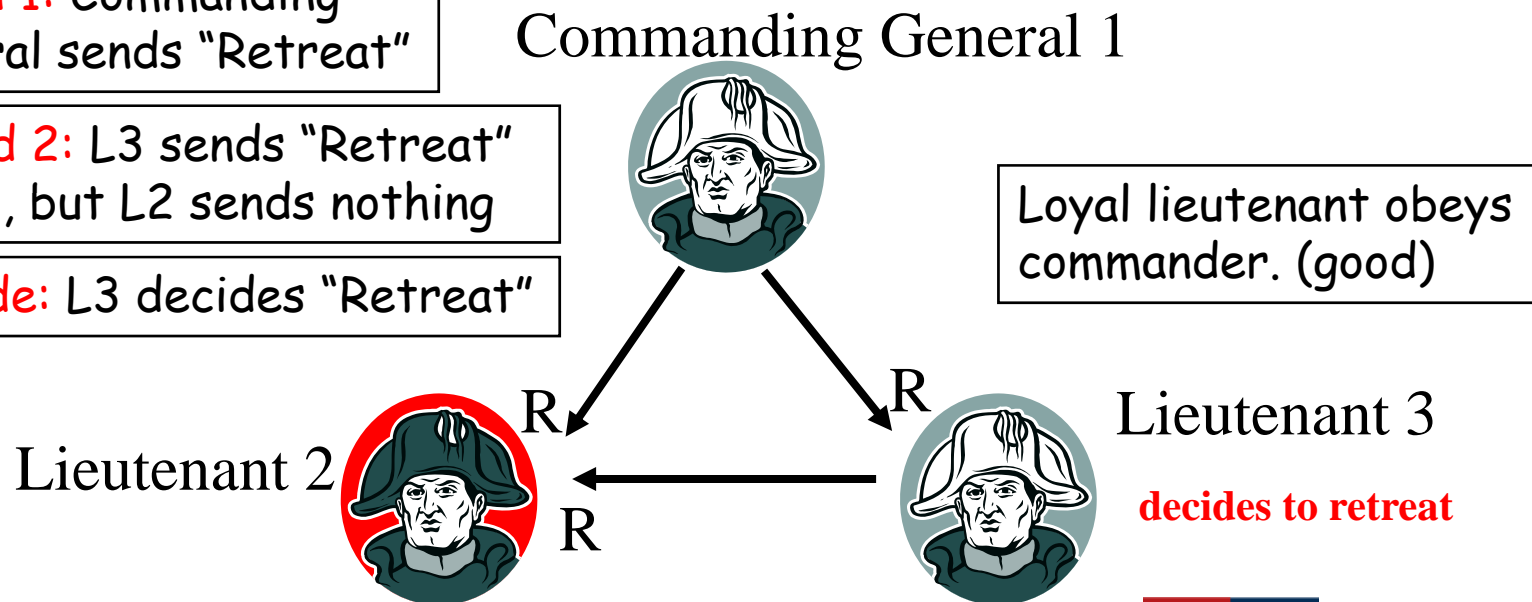
- Traitor lieutenant tries to foil consensus by refusing to participate

"white hats" == loyal or "good guys"
"black hats" == traitor or "bad guys"

Round 1: Commanding General sends "Retreat"

Round 2: L3 sends "Retreat" to L2, but L2 sends nothing

Decide: L3 decides "Retreat"



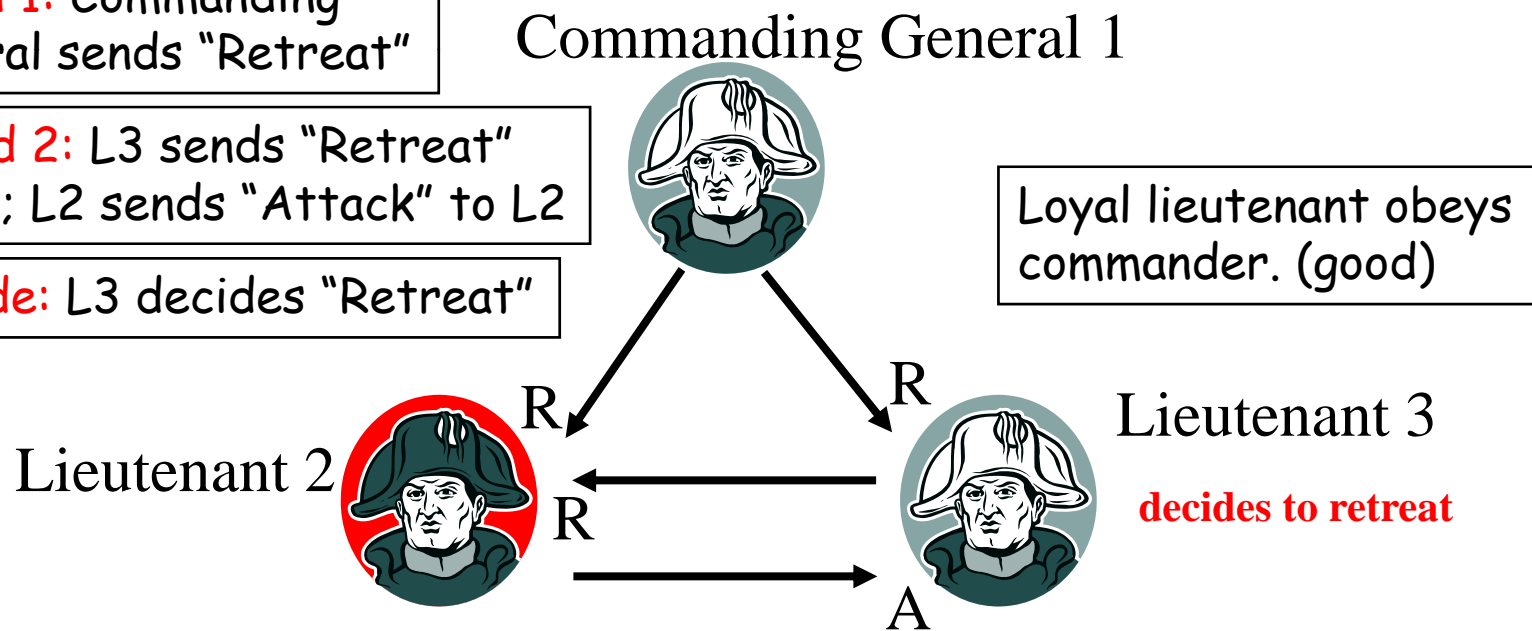
Case 2a

- Traitor lieutenant tries to foil consensus by lying about order sent by general

Round 1: Commanding General sends "Retreat"

Round 2: L3 sends "Retreat" to L2; L2 sends "Attack" to L2

Decide: L3 decides "Retreat"



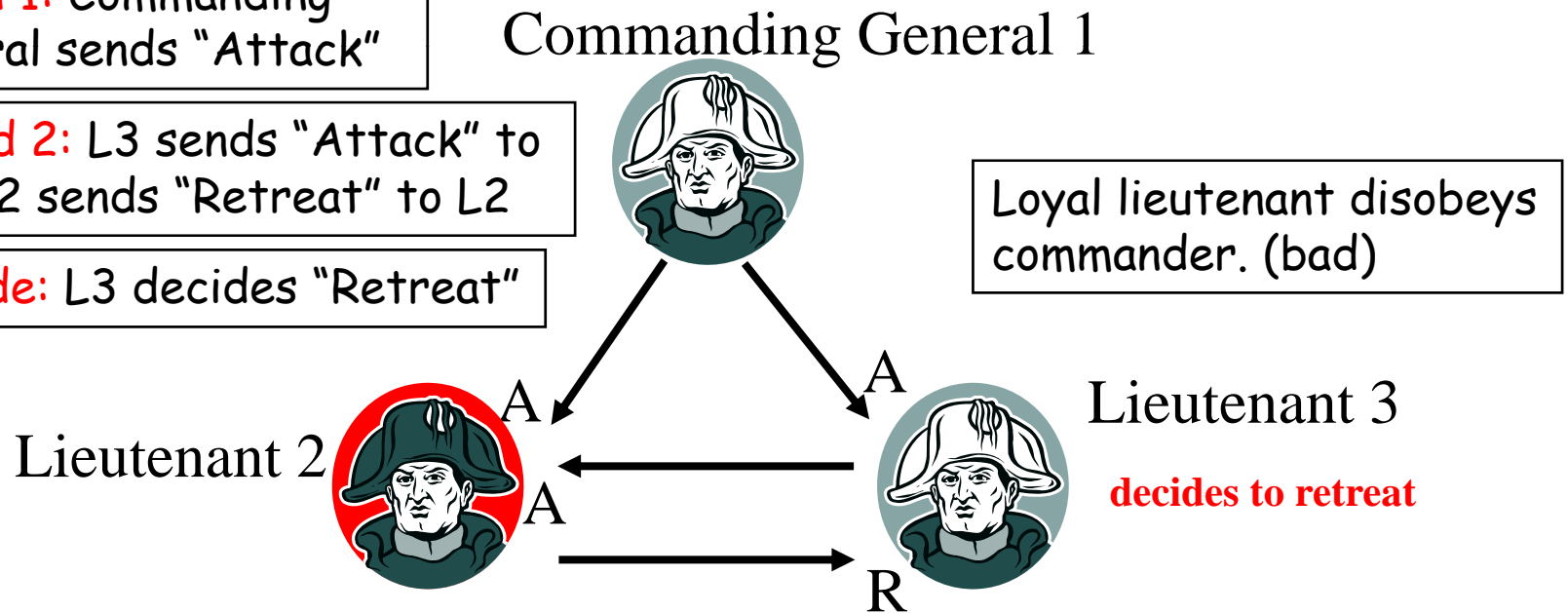
Case 2b

- Traitor lieutenant tries to foil consensus by lying about order sent by general

Round 1: Commanding General sends "Attack"

Round 2: L3 sends "Attack" to L2; L2 sends "Retreat" to L2

Decide: L3 decides "Retreat"



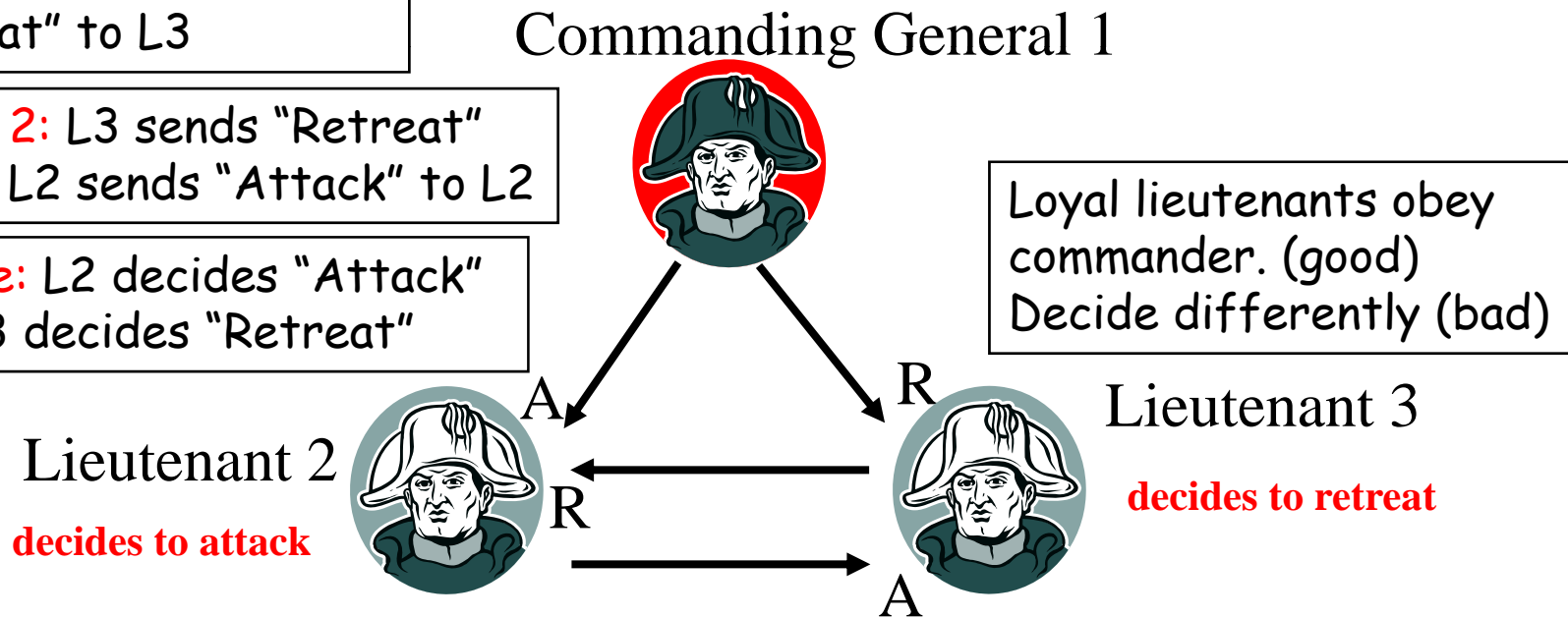
Case 3

- Traitor General tries to foil consensus by sending different orders to loyal lieutenants

Round 1: General sends "Attack" to L2 and "Retreat" to L3

Round 2: L3 sends "Retreat" to L2; L2 sends "Attack" to L3

Decide: L2 decides "Attack" and L3 decides "Retreat"



Byzantine Consensus: $n > 3f$

- Oral Messages algorithm, $OM(f)$
- Consists of $f+1$ "phases"
- Algorithm $OM(0)$ is the "base case" (no faults)
 - 1) Commander sends value to every lieutenant
 - 2) Each lieutenant uses value received from commander, or default "retreat" if no value was received
- Recursive algorithm handles up to f faults

OM(f): Recursive Algorithm

- 1) Commander sends value to every lieutenant
- 2) For each lieutenant i , let v_i be the value i received from commander, or "retreat" if no value was received. Lieutenant i acts as commander in Alg. OM(f-1) to send v_i to each of the $n-2$ other lieutenants
- 3) For each i , and each j not equal to i , let v_j be the value Lieutenant i received from Lieutenant j in step (2) (using Alg. OM(f-1)), or else "retreat" if no such value was received. Lieutenant i uses the value $\text{majority}(v_1, \dots, v_{n-1})$.

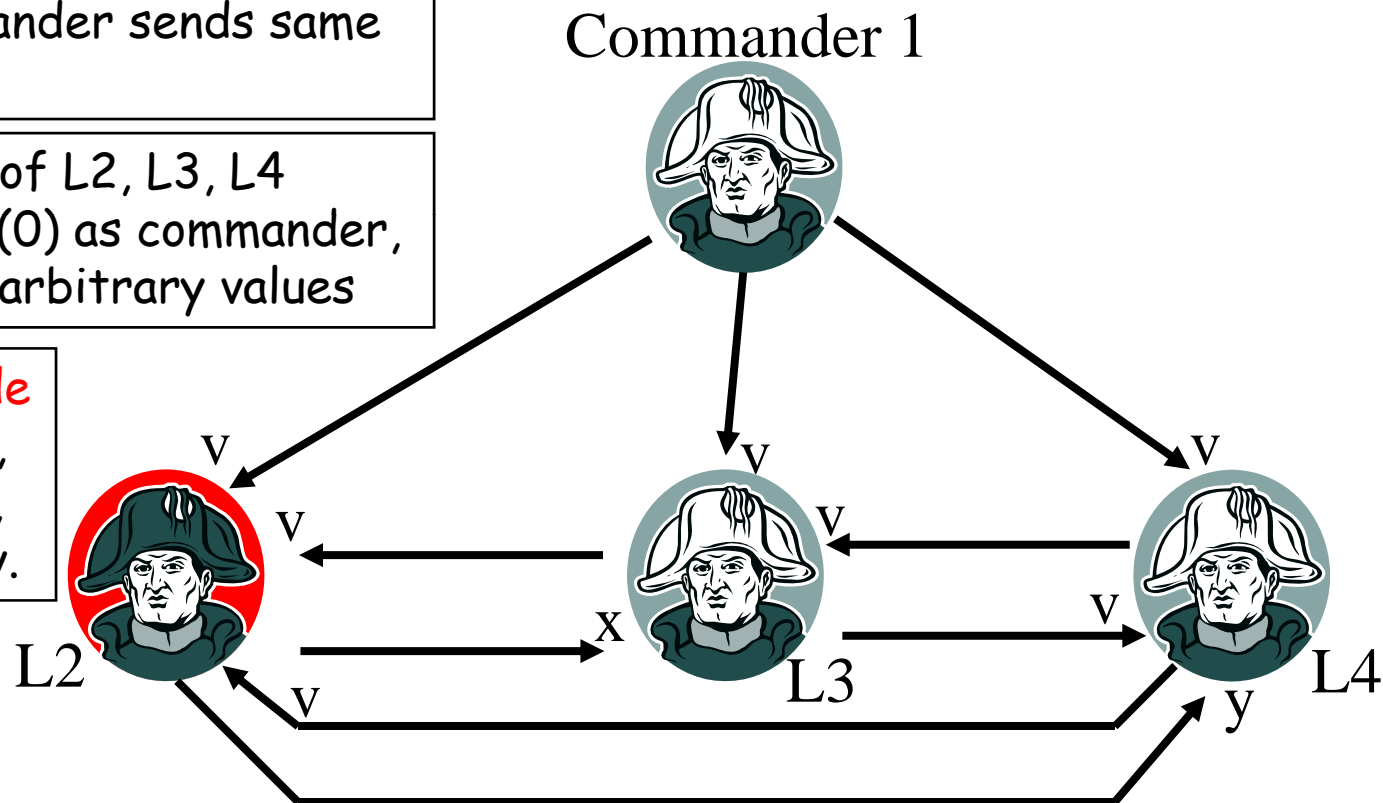
Example: $f = 1, n = 4$

- Loyal General, 1 traitor lieutenant

Step 1: Commander sends same value, v , to all

Step 2: Each of L2, L3, L4 executes $OM(0)$ as commander, but L2 sends arbitrary values

Step 3: Decide
L3 has $\{v, v, x\}$,
L4 has $\{v, v, y\}$,
Both choose v .



Example: $f = 1, n = 4$

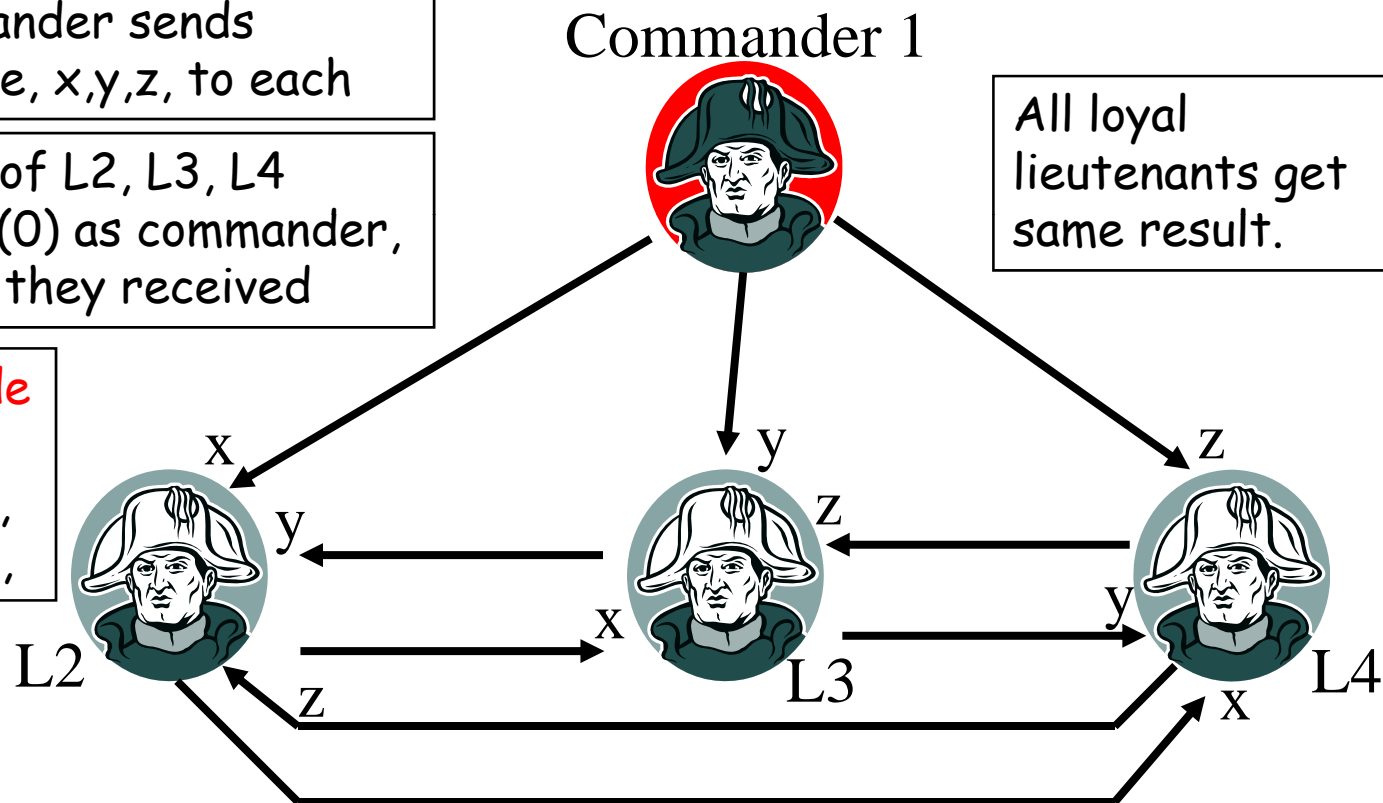
- Traitor General, all lieutenants loyal

Step 1: Commander sends different value, x, y, z , to each

Step 2: Each of L2, L3, L4 executes $OM(0)$ as commander, sending value they received

Step 3: Decide

L2 has $\{x, y, z\}$
L3 has $\{x, y, z\}$,
L4 has $\{x, y, x\}$,



Problem

- Lots of messages required to handle even 1 faulty process
- Need minimum 4 processes to handle 1 fault, 7 to handle 2 faults, etc.
 - But as system gets larger, probability of a fault also increases
- If we use *signed messages*, instead of oral messages, can handle f faults with $2f+1$ processes
 - Simple majority requirement
 - Still lots of messages sent though, plus cost of signing

Asynch. Distributed Consensus

- Fail-Stop/Byzantine → IMPOSSIBLE!
- FLP impossibility result
 - Fischer, Lynch and Patterson impossibility result
 - Asynchronous assumption makes it impossible to differentiate between failed and slow processes.
 - Therefore *termination (liveness)* cannot be guaranteed.
 - If an algorithm terminates it may violate *agreement (safety)*.
 - A slow process may decide differently than other processes thus violating the agreement property

Castro: Practical Byz. Fault Tolerance

- Uses various optimizations to combine messages, reduce total communication
- Relies on partially synchronous assumption to guarantee **liveness**.
- Therefore attacks on system can only slow it down - **safety** is guaranteed.
- Assumes that an attack on **liveness** can be dealt with in a reasonable amount of time.
- Suitable for wide area deployment (e.g., internet)
- Being used in Microsoft Research's *Farsite* distributed file system

Partially Synchronous Consensus Algs

- Relies on a Fault-Detector
- Synchronous/Fail-stop distributed consensus algorithms (e.g. FloodSet) can be transformed to run in the partially synchronous environment
- Byzantine is still a problem though...
 - DoS attacks on correct processes result in the identification of correct processes as failed, reducing the number of processes that must be compromised to breach the *safety* property (i.e. attackers can manipulate f which is **not** cool)