CSC236 winter 2020, quiz week 11_1

Question.

Recall that for a language L, the Kleene star operation can be defined as $L^* = L^0 \cup L^1 \cup L^2 \cup \ldots$. We will define a similar operation $Oddstar(L) = L^1 \cup L^3 \cup L^5 \cup \ldots$, i.e. the union of all the odd powers of L.

Describe a procedure for constructing an FSA that accepts $Oddstar(\mathcal{L}(M))$ given an arbitrary DFSA M. (You may use non-determinism.)

Solution.

Observe that, by definition, $Oddstar(L) = L(LL)^*$. We can construct a machine that accepts $\mathcal{L}(M)\mathcal{L}(M)$ using the construction for concatenation shown in figure 7.18 of the course notes (i.e. we juxtapose two copies of M, make the accepting states of the first copy non-accepting, and join them to the start state of the second copy by ε transitions). We can then apply the construction from figure 7.19 of the course notes (marking the initial state as accepting, and adding epsilon transitions from accepting states to the start state) to that machine, to get an NFSA that accepts the Kleene star of the concatenated language, i.e. $(LL)^*$. Finally, we can apply the concatenation procedure once more to concatenate a copy of M with the previously formed machine, to create a machine accepting $L(LL)^*$.